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**Microstrip Triplexer using a common triple-mode resonator**

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Abstract: An all-resonator based triplexer is presented using a double-stub-loaded resonator (DSLR) that acts as a common resonator at the junction of the three channels. The open stub DSLR has been analysed using even and odd-mode method to reveal the relationship between the three resonant modes. The design offers flexibility of frequency selection. The DSLR resonator is coupled with three sets of hairpin resonators to form the triplexer at 1.8, 2.1, and 2.6 GHz for mobile communication applications. The measurement results are in very good agreement with the simulations.

1. Introduction

As wireless communication technology advances, devices supporting multiple standards and multiple bands are increasingly desired in mobile communications and satellite systems. For instance, a triplexer may be required to connect the stack of filters for the DCS1800 band, UMTS2100 band and some LTE bands. Traditionally a multiplexer is formed of channel filters which are designed separately and then combined using a transmission-line based junction. Different types of junctions have been used over the years, such as T-junctions, manifolds or star junctions [1]. Recently a new concept, the so-called multi-port filtering network (MPFN), has been developed [2]. The main difference between the conventional two-port filter and the MPFN is the junction resonators, which are responsible for directing the signal to multiple ports. It has been the focus of many researches, as it provides an additional frequency band to achieve a dual-band microwave and optical technology letters system.

The junction resonator, or as also called the common resonator, has a major role to play in the MPFN design. It can be a single [4] or multi-mode [5] resonator. A single-mode resonator is relatively easy to implement but often restricted on the achievable overall bandwidth of the device. For diplexers or multiplexers with widely separate channels, it is desirable to use multi-mode resonators that are capable of producing multiple resonances. It is a particular advantage to have controllable resonance frequencies. One of the most used is the stub loaded resonator (SLR). It consists of a half-wavelength resonator and an open or a shorted stub. The stub provides an additional frequency band to achieve a dual-band resonator. This gives the advantage of controlling the frequencies flexibly by tuning the lengths of the stubs [6-8].

To achieve triple modes, two open stubs form a cross-shape stub loaded resonator as shown in Fig. 1(a). The half wavelength resonator (2xL1) resonates at 1.8 GHz. The two stubs are located in the middle of the half wave resonator. The lower longer stub (L2) helps to realise the 2.1 GHz resonance, whereas the shorter upper stub (L3) to realise the 2.6 GHz resonance. $\theta_1$, $\theta_2$, and $\theta_3$ are the corresponding electrical lengths. Due to the symmetric structure of the resonator, odd and even mode analysis has been used as shown in Fig. 1.

2. Design of tri-mode DSLR

The single open stub loaded resonator has been studied extensively [16] as a dual-mode resonator. The tri-mode resonator with three resonant frequencies is designed here based on the double SLR (DSLR).

This letter presents an all-resonator based triplexer that uses a folded double stub-loaded-resonator (DSLR) as it replaces the junction and distributes the signal into three paths. Previous works used mixed open and short stubs to give isolation, but limited the structural topology. Different from previous work, all stubs used in this paper are open for the ease of implementation in microstrip lines.
Due to the open circuit boundary condition at the symmetric T-shaped single stub loaded resonator as shown in Fig. 1(c). The odd mode frequency is designed to be 1.8 GHz.

The even mode equivalent circuit layout, Fig. 1(b) shows the equivalent circuit for the odd mode, when the junction represents a short circuit. (1) can be used to obtain the odd mode frequency.

\[ f_{\text{odd}} = \frac{(2n - 1)c}{2L_1\sqrt{\varepsilon_e}} \]  

where \( c \) is the speed of light and \( \varepsilon_e \) is the effective dielectric constant. The odd mode frequency is designed to be 1.8 GHz.

For the even mode, the equivalent circuit is reduced to a T-shaped single stub loaded resonator as shown in Fig. 1(c). Due to the open circuit boundary condition at the symmetric plane, the impedances of the stubs (with \( \theta_1 \) and \( \theta_2 \)) are doubled to \( 2Z_0 \) and \( 2Z_2 \). There is no symmetry in this stub loaded resonator structure and its dual mode resonant property has been studied in [5]. The input admittance can be expressed as

\[ Y_{in} = -jY_1\frac{Y_2\tan(R_f\theta_1)+Y_2\tan(R_f\theta_2)+Y_3\tan(R_f\theta_3)}{\tan(R_f\theta_1)\tan(R_f\theta_2)\tan(R_f\theta_3)-Y_1} \]  

where \( Y_1=1/Z_1 \), \( Y_2=1/(2Z_2) \), \( Y_3=1/(2Z_3) \). \( R_f \) is the ratio between the first two resonance frequencies of the single SLR. In this design, it is also the ratio between the second (2.1 GHz) and the third (2.6 GHz) resonance of the DSLR. Therefore, the resonant condition is:

\[ \frac{\tan R_f\theta_1}{Z_1} + \frac{\tan R_f\theta_2}{2Z_2} + \frac{\tan R_f\theta_3}{2Z_3} = 0 \]  

This design assumes equal line width of the DSLR, i.e. \( Z_1 = Z_2 = Z_3 \). The targeted two resonances are 2.1 and 2.6 GHz in this work.

Fig. 2(a) illustrates the relationship between the resonance ratio \( R_f \) and the electrical length of \( \theta_3 \) when the rest of the parameters are fixed. It should be noted that the three electrical lengths \( \theta_1 \), \( \theta_2 \) and \( \theta_3 \) are defined at the first resonance of the even-mode equivalent circuit, i.e. 2.1 GHz. Since \( \theta_3 \) is 90° at 1.8 GHz, it is fixed at 105° for 2.1 GHz. Also, \( \theta_2 \) is varied at 80°, 90°, 100° and 110° at 2.1 GHz. The ratio \( R_f \) varies against \( \theta_3 \), illustrating the degree of freedom that the design has to resonate at controllable frequencies as shown in Table 1. From Fig. 2(a), when the desired \( R_f = 2.6/2.1 = 1.23 \), \( \theta_3 \) is found to be 64.2° at 2.1 GHz. The calculated \( L_1 \), \( L_2 \) and \( L_3 \) from (3) are 105° (25.03 mm), 90° (21.44 mm), and 64.2° (15.28 mm) at 2.1 GHz. Table 2 shows the solutions for \( \theta_3 \) as \( \theta_2 \) changes for \( R_f = 1.23 \).

<table>
<thead>
<tr>
<th>( \theta_3 ) (°)</th>
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<th>( L_2 ) (mm)</th>
<th>( L_3 ) (mm)</th>
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<tr>
<td>80</td>
<td>68.1</td>
<td>19.06</td>
<td>16.23</td>
</tr>
<tr>
<td>90</td>
<td>64.2</td>
<td>21.44</td>
<td>15.28</td>
</tr>
<tr>
<td>100</td>
<td>61.8</td>
<td>23.82</td>
<td>14.71</td>
</tr>
<tr>
<td>110</td>
<td>60.0</td>
<td>26.20</td>
<td>14.29</td>
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Based on the \( R_f \sim \theta \) relationship, a DSLR resonator is designed using Sonnet. The S-parameter responses show the three modes in Fig. 2(b). Roger 3004C substrate with \( \varepsilon_r = 3.55 \) and a thickness of 1.524 mm is chosen. The DSLR achieved the targeted frequencies with \( L_1 = 25 \) mm, \( L_2 = 21.1 \) mm, and \( L_3 = 15.3 \) mm after optimization. These values are in good agreement with the calculations as shown in Table 1.

The triple-mode DSLR physical lengths analysis and its simulated resonances.

(a) \( R_f \) as a function of the electrical length \( \theta_2 \) and \( \theta_3 \). (b) The simulated resonances of the DSLR.
Fig. 3 shows the simulated current distributions of the DSLR showing the current concentration in the lower stub at 2.1 GHz and in the upper stub at 2.6 GHz. At 1.8 GHz, no current flows into the two stubs.

Fig. 3. Simulated current distribution of the DSLR.
(a) 1.8 GHz, (b) 2.1 GHz, and (c) 2.6 GHz

3. Design of triplexer

The triplexer is designed using an all-resonator based topology. A folded DSLR is used to replace the conventional impedance matching junction and distribute the signal into three paths. The first path is via the odd mode of the DSLR which is coupled with a half wavelength hairpin resonator. The second path is via the longer open stub coupled with a hairpin resonator at 2.1 GHz. The third path is via the shorter open stub of the DSLR. The topology is shown in Fig. 4. The white circles represent the resonators. The circle marked with XR represents the common triple-mode DSLR resonator while the circles with R are the single mode hairpin resonators.

Fig. 4. The proposed triplexer coupling topology.

Fig. 5. Layout of the proposed triplexer.

In this topology, the input port P1 is designed to couple to the three modes of the DSLR respectively. So, the coupling structure can be characterised using three independent 2nd-order filters all with a return loss of 20 dB. So corresponding coupling matrix and external quality factor calculated as follows:

\[
M^1 = \begin{bmatrix}
0 & 0.023 & 0 \\
0.023 & 0 & 0.023 \\
0 & 0.0316 & 0
\end{bmatrix}
\]

\[
M^2 = \begin{bmatrix}
0.0316 & 0 & 0.0316 \\
0 & 0.0265 & 0 \\
0 & 0.0265 & 0
\end{bmatrix}
\]

\[
M^3 = \begin{bmatrix}
0.0265 & 0 & 0.0265 \\
0 & 0.0265 & 0 \\
0 & 0.0265 & 0
\end{bmatrix}
\]

and \( Q_{\text{ex}} = 47.5, 34.12, 41.69 \)

After a process of Q and M extraction for each resonator individually; the final stage is to assemble all the resonators as illustrated in Fig. 5. A fork shape input feed has been used to reach the required external quality factor for each of the three modes. It should also be noted that non-uniform impedance lines have been used in the DSLR to facilitate coupling.

4. Simulated and Measured Results

Fig. 6 shows the simulated results using Sonnet in comparison with the measurements from a N5230A Network analyser. Very good agreement has been achieved. There is a slight shift in frequencies because of fabrication tolerance. The central frequencies are 1.88, 2.1, and 2.6 GHz; The FBW achieved are 0.86%, 1.4%, 0.96% respectively. The return losses are better than 15 dB for all three channels.

The 2.1 GHz passband from Port 2 has an insertion loss of 1.3 dB and rejects the other two bands to below -43 dB. Likewise, the third band was extracted at Port 3 with 2.3 dB insertion loss while rejecting the other two bands to below -48 dB. For the first band, the insertion loss is 3.2 dB. The rejection is 21 dB to the 2.1 GHz band and 36 dB to the 2.6 GHz band.

Regarding ports isolation, the isolation between Ports 3 and 4 is found to be over 43 dB. This is over 42 dB between Port 2 and 3. The isolation between Port 4 and 2 is the worst at around 1.88 GHz, which is at 27 dB. The isolation performance in Fig. 6 (c) shows that, although the design used all open circuits, reasonably good isolation is still achieved.
This letter proposes and analyses a double-stub-loaded resonator (DSLR) and uses it as the common resonator at a four-port triplexer. The analytical analysis and simulations have demonstrated the flexible control of the three resonances. Replacing the short stubs used in previous works with open stubs eases the implementation using microstrip technologies and still provides reasonably good isolation between the three bands. The simulated and measured results were found to be in good agreement.

**References**