# From Computer-Aided to Intelligent Machining:

# **Recent Advances in CNC Machining Research**

Yingguang Li<sup>1,\*</sup>, Chen-Han Lee<sup>2</sup> and James Gao<sup>3</sup>

<sup>1</sup>College of Mechanical and Electrical Engineering, Nanjing University of Aeronautics and

Astronautics, Nanjing, 210016, China

<sup>2</sup>National NC System Engineering Research Center, Huazhong University of Science and

Technology, Wuhan, 430000, China

<sup>3</sup>Faculty of Engineering and Science, University of Greenwich, Chatham Maritime, Kent, ME4 4TB,

UK

#### **Abstract**

The aim of this paper is to provide an introduction and overview of recent advances in the key technologies and the supporting computerized systems, and to indicate the trend of research and development in the area of computational numerical control machining. Three main themes of recent research in CNC machining are simulation, optimization and automation, which form the key aspects of

\*Corresponding author, Email: welcome.li@nuaa.edu.cn

intelligent manufacturing in the digital and knowledge based manufacturing era. As the information and

knowledge carrier, feature is the efficacious way to achieve intelligent manufacturing. From the regular

shaped feature to freeform surface feature, the feature technology has been used in manufacturing of

complex parts, such as aircraft structural parts. The authors' latest research in intelligent machining is

presented through a new concept of multi-perspective dynamic feature (MpDF), for future discussion and

communication with readers of this special issue. The MpDF concept has been implemented and tested in

real examples from the aerospace industry, and has the potential to make promising impact on the future

research in the new paradigm of intelligent machining. The authors of this paper are the guest editors of

this special issue on computational numerical control machining. The guest editors have extensive and

complementary experiences in both academia and industry, gained in China, USA and UK.

Keywords: Digital manufacturing, Optimisation, Process modeling and planning, CNC machining,

Feature

1. Introduction

With conventional Computer Aided 'x' (CAx) technologies, including Computer Aided Design

(CAD), Manufacturing (CAM), Engineering (CAE), Process Planning (CAPP), and Computer Numerical

Control (CNC) in a more general sense, computerized programs serve the role of providing assistance

2

while engineering users are responsible for making process decisions. CAx systems produce process data (including product definitions, manufacturing process plans, cutting tool paths, and control commands) based on users' inputs. Although reliable results are produced, the degree of efficiency depends on the users providing process parameters. In recent years, the advances in computational power, algorithms, and better understanding of the physics and mathematical models of machining processes enabled computerized programs to automate some of the process decisions. The goal is to automate and optimize, as much as possible, the process decisions traditionally taken by engineers. These technologies would eventually make the users more productive and the machining processes more efficient and optimized.

This paper reports on state-of-the-art research in computerized intelligence, including automated decision-making and optimization, related to numerical control (NC) machining processes. As suggested in the title, the code name 'intelligent machining' is adopted to represent such computerized intelligence in machining processes. Computerized intelligence involves algorithm design, knowledge based engineering and computation activities. The scope of this paper is limited to aspects related to part machining covering most (but not all) of contemporary interests. This paper is not intended to be a historical review, but focus on recent trends, whilst some earlier publications were cited to provide contextual background. The reference list may leave out important (and older) papers that are corner stones of the topics. Section 2 of this paper provides an overview of advances in recent research from a specialized 'technology' point of view, while Section 3 provides review of research from an integrated

'systems' point of view. The authors' proposed dynamic feature concept and latest research in intelligent machining is presented in Section 4, to share with readers of this special issue, and to encourage further discussions and communications in this topic.

## 2. Advances in CNC Machining Technologies

This Section reviews and introduces specific key technologies in the area of Computational Numerical Control. Each sub-section describes recent progress on computerized intelligence in a particular topic, and provides citations of relevant research papers for further information.

#### 2.1 Work Step Planning and Optimization

Before the programming and execution of every machining operation (work step), it requires planning for the process operational conditions. The planning tasks include the selection of machine tools, cutters, and setup configurations. The decisions are made by experienced operators/engineers based on the existing resources/equipment in the shop floor. While the operators/engineers try to come up with best decisions, the results are not guaranteed to be optimal if the workers are not well trained, not given proper information, nor time to perform. Recent research attempted to perform some of the work step planning tasks with machine intelligence. The goal is to formulate the planning tasks as optimization problems that can be solved mathematically and numerically. This would enable automated solutions for work step planning, replacing some of the human decision-making tasks.

Setup planning involves making a lot of decisions such as the location and orientation of the

workpiece on the machine table, the (clamping) positions of the fixtures to the workpiece, and the selection of fixtures. Setup configuration tasks can be automated based on various optimization criteria, including global avoidance during machining [1], machine kinematic efficiency [2], machine kinematic induced tracking errors [3], and clamping force based spatial arrangement of fixtures [4]. Cutter (tool) selection is another important task of work step planning. There are several factors to be considered for cutter selection. Among them are the size (radius) of the cutter for fitting into narrow regions (accessibility) [5] and cutting profile (at the bottom of the cutter) for fitting workpiece surface concavity (curvature) [6-7].

## 2.2. Optimal Tool-axis Computation

When programming five-axis tool paths, the specification of tool-axis control is the most difficult task. The rotational motions are difficult to visualize and process mathematically. The fact that the workpiece and work table on the machine tool may rotate in some systems presents additional difficulty for the programmers to fully comprehend. There are two types of five-axis milling: Point and Flank. Point milling uses the tip (bottom) of the cutters to remove the material, whilst Flank milling, also known as Profile cutting and Peripheral milling, uses the side of the cutter to remove material. There are several key requirements to consider for tool-axis programming, as explained below:

i) Collision avoidance. The programmed tool-axis orientation shall never cause the cutter head to

- collide with any obstacles in the machine tool. This applies to both Point and Flank milling.
- i) Shape accuracy. When the cutter orientation affects the amount of material to be removed, the overcut and undercut must be controlled. This applies mainly to Flank milling.
- iii) Cutting condition. Tool-axis determines the orientation of the cutter relative to the workpiece surface, hence influencing the physical interaction between the cutter and the material. This applies mainly to Point milling.
- iv) *Machine kinematics/dynamics*. The change of tool-axis is controlled by the two rotary axes. It is important to consider the kinematic limits and dynamic stability of the rotary axes in tool-axis computation. This applies to both Point and Flank milling.

In state-of-the-art CAM systems, the tool-axis is specified according to the given spatial descriptions. The system provides many methods and the programmers choose one among them to describe the spatial definition of the tool-axis. The methods have no direct correlation to machining requirements so the programmer has to mentally work out the results and figure out which one is the best according to the requirements. It requires high-level understanding of the mathematics and geometry, plus many years of experiences in five-axis machining. Recently researchers began to compute the optimal orientation and positioning of tool-axis based on one or more of the above mentioned requirements, in lieu of user-controlled spatial specifications. The efforts are mainly for Flank milling, with different constraints

and optimization goals [8-9].

# 2.3. Path Shape Optimization

Tool path computation consists of mathematical models and algorithms, and the resulting tool paths depend on the limitations and characteristics of the computation methods. In reality, the "perfect" algorithm for tool-path generation doesn't exist. Consequently the tool paths usually don't meet the highest quality demands, and are further degraded by the common practice of G-code representation. As a result, the tool paths generated by today's leading commercial CAM systems suffer from several common deficiencies, such as:

- i) Sudden change of direction caused by the algorithm of pattern computation,
- ii) Noisy and even jagged paths caused by geometry discretization or numerical instability,
- iii) Built-in G<sup>1</sup> (tangent) discontinuity as a consequence of G01 (GOTO) code, and
- iv) Inconsistency among neighboring passes, due to the fact that the paths are usually computed one pass at a time without considering the neighboring passes.

The goal of path shape optimization is to handle the above problems. The typical strategy is to modify the tool path shape after the tool paths are generated from the CAM systems, in either the post processing stage (after CAM before CNC) or within the CNC during axis command processing (also

known as control interpolation). Due to the fact that the post modification is performed without knowing the original part geometry, the modification must be limited to minor deviations (meaning the deviations are within the specified machining tolerance) from the given tool paths.

One type of path shape optimization solution is to perform smoothing and B-spline or Non-Uniform Rational B-Spline (NURBS) fitting on the G01 code, to achieve continuous path trajectories and hence smooth surface finish and less speed fluctuation during machining. In the case of five-axis machining, it is common to represent a tool path with dual B-spline curves, one tracking the tool-end (bottom) point and the other tracking the upper end of the cutter. Examples were given by Yuen et al. [10] for 5-axis machining and Chen et al. [11] for 3-axis machining. Another type of path optimization solution is to perform corner rounding of the poly-line trajectories of G01. The deviations are confined to the neighborhood of each G01 points. Examples were given by Beudaert et al. [12] for 5-axis machining and Zhao et al. [13] for 3-axis machining.

Although the path modification is usually performed after the path generation, it can be applied during the generation. The modification is localized, that is, applied to nearby GOTO points, during the path computation. Bouard et al. [14] applied localized smoothing to 2D, 3-axis machining, while Beudaert et al. [15] applied localized smoothing to tool-axis, both during tool path generation.

#### 2.4. Net Shape Simulation

Optimization of tool paths requires the computation of the net shape of the workpiece after the material has been removed by the cutter. The geometric net shape simulation is used to derive surface quality and volume removal rate. The former is important for finishing operation optimization, while the latter is the key to optimizing the material removal rate of roughing operations. Net shape simulation has two competing (and contradicting) requirements: accuracy and speed of computation. Satisfying both is particularly difficult for five-axis tool paths. Recent efforts focused on new algorithms to improve accuracy and computation speed for the net shape simulation of five-axis machining.

Workpiece net shape is the complement of the swept volume of the cutter that is the core of the problem. There are two major approaches to computing cutter swept volume. One is computing the sweeping envelopes [16] and integrating them to form the surface of the swept volume [17-19]. This method is more suitable for surface finishing simulation. The other method is to use a global spatial structure (or spatial directory) to describe the shape, with one reported by Sullivan et al. [20] being an example. The second method is commonly used for volume removal computation.

### 2.5. Optimized Feed Planning and Interpolation

Tool paths generated from CAM systems come in two forms: either poly-line-based G-code or NURBS-based trajectories (see Section 4 - Path Shape Optimization, for more information). In either form, the tool-paths contain only the shape information, but no feed (velocity) function, at most the upper

bound of the feed is provided. The job of feed planning (feed scheduling) is left for the controllers to fulfill during real-time control, including the following two major tasks:

- i) Feed function: Given an axis-position path, P(u), compute the desirable (based on various constraints and goals) feed function,  $\frac{dP}{dt}$ , which is then used to derive the time derivative of the path parameter,  $\frac{du}{dt} = \left|\frac{dP}{dt}\right| \left|\frac{dP}{du}\right|^{-1}$ .
- ii) Subdivision: Compute the parameter interval that corresponds to the cycle time  $(\Delta t)$  of the drive,  $\Delta u = \int_{t_0}^{t_0 + \Delta t} \frac{du}{dt} dt$ , then use it to get the sampling parameter,  $u_i = u_{i-1} + \Delta u$ , and sampling data,  $P(u_i)$ , to be sent to the drive.

Ideally the feed value should be as large as possible (to achieve least machining time), but it is limited by the following constraints: upper bound of axis speeds, upper bound of axis accelerations, upper bound of jerks, tracking errors from sampling (subdivision), and tracking errors due to the dynamic response characteristics of the servo drives. Mathematically speaking, computing feed function is a constrained optimization problem. The main challenge is to solve such constrained optimization problem in real time, with usually limited CPU speed and storage capacity.

Compared to feed function, the task of subdivision is less demanding. The main work load is the numerical computation of the integral,  $\Delta u = \int_{t_0}^{t_0+\Delta t} \frac{du}{dt} dt$ . It has to be fast and accurate.

In commercial CNC systems, it is common to simplify the model and target a near-optimal (better solution), instead of the absolute optimal (best solution), in order to cope with real-time requirement and limited resources. To approach the best solution, the goal of recent research efforts is to come up with new algorithms that can solve the constrained optimization problem in real time.

Beudaert et al. [21] and Guo et al. [22] proposed new algorithms to improve the accuracy and performance of feed function computation. Annoni et al. [23] combined feed function and subdivision tasks in the proposed algorithm to obtain better result. Other efforts focused on new subdivision method for improvement [24-25]. Instead of real-time computation, Lee et al. [26] proposed moving the feed function computation to non-real-time (ahead of actual machining) to eliminate the real-time limitations.

#### 2.6. Automated Contour Error Compensation

When machining a part, the actual trajectory of the cutter relative to the workpiece is called the realized tool path. In theory, the realized tool path should coincide with the tool path generated from the CAM system. However, the realized tool path is never the same as the nominal tool path, and the differences between them are called contour errors. At this point, it is useful to briefly clarify the difference between tracking and contour errors. As explained in the previous Section, contour errors are defined in the workpiece coordinate system (WCS), which is also used by CAM-generated tool paths. Meanwhile, the tracking errors are defined in the axis-position space of the machine tool. Tracking errors

are sources of contour errors and a contour error caused by a tracking error is the forward kinematic transformation of the tracking error.

This sub-section only covers the contour errors that are related to the characteristics and condition of the machine tool and its components. That is, the errors that depend on the machining process and the workpiece being machined (such as chip formation and cutting forces) are excluded. The following are the common sources of equipment-based contour errors:

- i) Kinematic errors due to the geometrical deviations of the machine tool components. The geometrical deviations could come from the dimensional errors or the fact that the components are not perfectly rigid. The dimensional errors are intrinsic and can be measured when the machine tool is stationary while the deformation from non-rigid-body effect depends on the acceleration of the machine tool components.
- ii) Tracking errors due to the dynamic response of the servo drives. When the servo drives are moving, they have to deal with the inertia of the moving components and friction at the junctions and tracking errors are unavoidable. The dynamic servo drive errors usually cease when the drives come to a complete stop.
- iii) Thermal deformation of machine tool components. Spindles operate at very high speed and generate considerable heat. The heat causes thermal deformation of the components near the

spindles and hence dimensional errors. Obviously, thermal deformation-induced contour errors are temperature dependent.

iv) Axis position interpolation errors of five-axis machines. As discussed previously, subdivision (sampling) of axis-position paths causes tracking errors and hence contour errors. Furthermore, usually G-code paths are interpolated in the axis-position space (except some advanced CNC systems that offer the capability to interpolate in the WCS) and linear interpolation in the axis-position space produces non-linear errors in WCS.

Study of contour errors and its compensation methods has been a popular topic in recent years. This is a complete reversal from the lack of progress previously. Most of the recent research work shares the common trait that covers three steps: the first step builds a (simplified) mathematical model to represent the contour errors; the second step performs measurements to populate the error model, and the final step modifies the tool paths based on the error model to compensate for the contour errors. This same trait applies to the research work of all four error sources listed above.

Among the four major sources of contour errors, static machine tool geometrical deviation (dimension errors) is the easiest to study, because it can be measured when the machine tool is stationary.

This topic also generates the most interest from researchers [27-32]. They experimented with various error models and measurement methods, but followed the same model-measurement-compensation

paradigm. Touch probing, ball-bar, and laser are the common choices for static contour error measurement. Since the contour errors are measured in WCS, it is easier to compensate the tool paths in WCS as well. If the compensation is made to the axis-position commands, its value must be brought to WCS via forward kinematic transformation for validation.

The dynamic portion of geometrical deviation, i.e., the deformation from non-rigid-body effects, is harder than static geometrical deviation and little research [33] are found in this area. The topic of tracking error from dynamic servo response also generates popular interest lately. This topic is more difficult than geometrical deviation because (a) servo dynamic errors can't be measured when the machine is stationary and (b) the source is tracking error but the manifestation is contour error. To overcome the difficulty of measurement, it is common to rely on the mathematical model of servo drive response behavior. The second difficulty is dealt with using forward kinematic transformation and inverse kinematic transformation during validation. Zhang et al. [34] and Lin and Wu [35] provided the compensation solutions for dynamic servo tracking errors of five-axis machines.

To improve the accuracy of modeling and compensating dynamic servo tracking errors, some researchers applied cross-coupling among different axes [36-38]. Presently these efforts are limited to the simple case of 2D machining (two axes only). There is considerably less research in thermal deformation [39] and five-axis interpolation errors [40].

### 2.7. Prediction of Process-dependent Machining Errors

Contour errors studies in the previous sub-section haven't included the physical interactions between the cutter and workpiece. Only machine tool characteristics and conditions were taken into account. During machining, the cutter-workpiece interaction produces forces on the cutter and workpiece (and the chips broken away from the workpiece). These forces cause additional machining errors beyond the no-load contour errors discussed previously. The cutting forces depend on the cutting conditions, and the corresponding form errors depend on the material and shape of the workpiece. That is, the cutter-workpiece interaction-induced machining errors are process dependent. These machining errors cannot be computed without knowing the details of the machining process, including the tool path, cutter, and workpiece.

When the cutting forces are present, both cutter and workpiece are deformed by the forces. On the workpiece side, there are elastic deformations and rigid-body position shift. Elastic deformation is significant when the portion of the workpiece being machined is thin (such as blades and pocket walls) or the material is highly elastic. The rigid-body shift of the workpiece is of importance if the machine tool has backlash problems or poor rigidity, or if the clamping of the fixture is not stable. For a very thin-walled workpiece, there could be a third type of deformation: plastic. Plastic deformation is smaller in magnitude than elastic deformation and also less studied. Similarly the force on the cutter causes elastic deformation and rigid-body shift. The elastic deformation on the cutter is known as tool deflection that is

usually much more significant than the rigid-body shift and of the tool assembly.

The study of process-dependent errors involves the following four tasks:

- Computing the chip formation from the process data (tool path, cutter geometry, and workpiece shape),
- ii) Estimating the cutting forces from the chip formation and cutting condition,
- iii) Predicting the deformation on the cutter and/or workpiece from the estimated cutting forces, usually with the help of finite element (FE) simulation, and
- iv) Offering a compensation solution to offset the predicted deformation of cutter/workpiece.

Several recent papers covered one or more of the above tasks. The effect of cutting forces induced machining errors is most severe in the situation of Flank milling on thin walls. Habibi et al. [41] and Wan et al. [42] provided the compensation solutions for, and the prediction of the form errors, from cutter and thin wall elastic deformation. Kang and Wang [43] also addressed the same cutter-thin wall elastic deformation problem, but only worked out the deformation prediction without offering the compensation solution. Wei et al. [44] introduced cutting force calculation using Z-map approximation. Liang and Yao [45] targeted chip formation calculation for ball-end cutters.

### 2.8. Optimization for Machine Tool Stability

In the previous sub-section, the emphasis was on the value of cutting forces and the resulting machining errors. There is another aspect of cutting forces that requires careful study: periodicity. The periodicity of cutting forces is tied to machine chatter problems. Due to the geometrical symmetry of milling cutters, the cutting forces are periodic functions of time, and the frequency is the spindle rate (revolutions per second) times the number of teeth in the cutter. If the cutting force frequency is in harmonic with the natural frequency of the machine tool, then vibration occurs, known as chatter.

The occurrence of chatter depends on two factors: spindle speed and depth of cut of the cutter in the axial direction. For a given cutter tooth configuration, the spindle speed determines frequency that in turn determines whether the harmonic with the machine tool takes place. Depth of cut in the axial direction is proportional to the chip volume and force. Hence, stability is a function of spindle speed and depth of cut, and can be illustrated as a curve in the depth of cut vs spindle speed diagram that divides the stable and unstable regions, known as stability lobe diagram (see Figure 1).

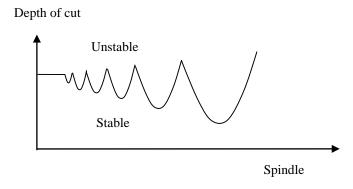


Figure 1. A typical stability lobe diagram.

Experimental measurements to obtain the stability lobe diagram of a machine tool are expensive and time-consuming. It's desirable to use mathematical models to predict it, although this is a complex and difficult computational problem. An example of stability prediction can be found in [46-48]. When the stability diagram is available, the stable region of the diagram can be applied as the constraint and optimize the machining parameters, to achieve optimal material removal rate [49], or surface variation [50].

#### 3. Advances in CNC Machining Systems

This Section reviews and introduces advances in CNC research from a systems and integration point of view. There are broadly three stages in the development of CNC machining systems, i.e., computer aided manufacturing, automatic manufacturing and intelligent manufacturing. As this paper focuses on part machining, the word 'manufacturing' is replaced by 'machining' in this paper. Research and

development in feature technology has played an important role in the CNC machining from both technological and system integration point of view. Therefore some emphasis is given to the latest research in feature technology.

## 3.1 Computer Aided Machining

The introduction of computers frees engineers from manual drafting of parts and process planning. A distinguishing feature of this stage is the assistance of computers. Before the advent of CAD technology, engineering drawings were the most commonly used technological documents for product design and manufacturing. The shapes and sizes of the machining features are represented by the orthographic views and the cross-section views. And the manufacturing requirements of machining features are represented by symbols and notes. In order to prepare a process plan, engineers need to interpret the geometry and manufacturing information from 2D drawings. Apparently, the quality of process planning depends upon the experience of the engineers. The machining process knowledge is hard to be stored and re-used.

In the mid-1960s, the first generation of CAD system was developed. Because it only provided 2D drafting function, strictly speaking early CAD systems should be called computer-aided drafting systems [51]. The digital files of 2D drawings have opened up the possibility of extracting machining features by computer programs. As an experiment, 2D drawings of the rotational parts were selected to verify the feasibility [52]. The application was extended to the prismatic parts gradually [53]. Then isolated and

non-intersecting features were extracted [54]. However, the intersecting features became the main obstacle [55]. Meanwhile, limited by the orthographic views, the features constructed by freeform surfaces were hard to extract. When the geometrical information was extracted, the dimensions of the machining features could be assigned automatically [56]. At present industrial practice, as the legacy data, 2D drawings of older products are still useful. Some researchers developed technologies for the reconstruction of 3D part models from 2D drawings [57].

When the machining features are extracted from 2D drawings, they can be used for process planning. Considering the similarity of the parts, Group Technology (GT) has been applied to code mechanical parts in variant computer-aided process planning system. Indexing rules were built to retrieve previous similar process plans according to the codes. Apart from GT technology, parametric process plan templates were widely used to store and represent the machining process of features. Process plans were generated by engineers who retrieve and modify the template library and solve related constraints according to the parameters of machining features [58-59]. Then, the tool paths can be generated according to the machining feature parameters and the process information.

Because the interpretation of 2D drawings is bound by the experience of the engineers, 3D CAD systems were later developed. Firstly, wireframe-based models were provided. The research work on feature extraction, process planning and NC programming based on wireframe model were reported

[60-61]. However, the 3D wireframe models were ambiguous, and were only suitable for quick display and verification of the geometry of simple feature models [62].

With the advances in CAD technology, solid models such as boundary representation (B-Rep) model and constructive solid geometry (CSG) models were proposed. A B-Rep model is capable of representing the lower-level geometric entities such as faces, edges and vertices for attaching dimensions, tolerances and other attributes. The CSG model is good at representing the higher-level primitives such as removal volumes and easy performance of feature operations such as add, delete and modify. Combining the advantages of the two models, hybrid CSG/B-Rep schemes were adopted in modern CAD/CAM systems. However, these models concentrate on the representation of geometry information. The machining process information were not properly stored and maintained in these models.

## 3.2. Automatic Machining

In the later stages of system development, automation is the goal of research in CNC systems. The representative technologies include feature recognition, data exchange between CAD/CAPP/CAM, and feature-based NC programming.

#### 3.2.1 Feature Recognition

As an efficient and practical CAD/CAPP/CAM integration methodology, feature recognition methods can be categorized into graph-based method, volume-decomposition method, hint-based method,

artificial intelligence-based method and hybrid method, since the concept was first proposed. Some earlier research in the development of feature recognition methods before 2005 have been reviewed by Han et al. [63] and Corney et al. [64], more recent research on feature recognition is introduced below.

Woo et al. [65] integrated graph-based, cell-based maximal volume decomposition and negative feature decomposition using convex decomposition into a hybrid feature recognition method. These three methods construct a sequential workflow in order to reduce the solution space gradually, to achieve relatively optimized recognition results. Dimov et al. [66] developed a hybrid feature recognition method which was mainly composed of feature learning and feature recognition. Knowledge acquisition techniques were applied for generating feature recognition rules and feature hints from training data. Then these rules and hints were used to identify machining features from the boundary representation model. The machining features that could be recognized can be extended to other domains using different training data.

Arivazhagan et al. [67] depicted a machining volume identification method for finishing machining based on STEP AP 203-214. The machining volumes of the machining features defined in STEP AP 203-214 were calculated by their proposed algorithm. Obviously, the universality of the method was limited by the specific machining processes of rough machining. Marchetta and Forradellas [68] presented an easily customized manufacturing feature recognition method through stripping the feature

definition and hints from the feature recognition algorithms. A knowledge-based model generator was built to describe the solid model of an input part by the declarative logic language. The features and their hints were also expressed by the declarative logic language. A general purpose artificial intelligence planner called Graphplan + was applied to recognize the manufacturing features from the knowledge-based representation of the part model.

Heo et al. [69] presented a methodology to recognize pocket features, and to partition the machining regions of pockets. The attributes of pocket features were defined for high speed machining planning. They used the slicing method which was similar to the method mentioned in [70] to generate multiple layers. Each layer has the same type of machining parameters to plan for high speed machining. Chu et al. [71] presented a machining feature recognition method made up of two phases based on available resources of cutting tools. The machining surfaces which are machined by the same cutting tool form a machining feature. Rule-based reasoning is applied to optimize the recognized machining features which have the minimum number of setups.

Yu et al. [70] described a feature recognition method for an aircraft integral panel generalized pocket.

The approach imitates the slice-machining process to use several planes whose orientation is the Z-axis direction to slice the part model into multiple layers. A feature profile is the intersection of the slicing plane and the part, which is used for tool path generation. This is inaccurate and time-consuming when a

part consists of freeform surfaces. To improve this method, they proposed a principal face-based machining feature recognition approach [72]. The principal faces are extracted for defining the machining domains. The topological relationships between the principal face and its adjacent faces are used to identify the feature type of the machining domain. The number of types of machining features that could be recognized was extended.

Zeng et al. [73] put forward a simulated rolling method for the recognition of outer profile faces of aircraft structural parts. A vertical, infinite and elastic revolving roller was imagined, and moved towards the part under the gravitation of the part. When the roller touch the part with rotation, the pressure force and frictional force are generated. The resultant force drove the roller to roll along the outer profile of the part until it reached the position where the roller touches the part for the first time. Then, the outer profile faces of the part were extracted. As a type of machining feature of aircraft structural parts, the machining of the outer profile was closely related to the fix method of the part. The bosses distributed around the outer profile of the part used for clamping divided the outer profile into multiple sections which were machined separately. Therefore, the practicality of the method still needed to be improved.

Li et al. [74] proposed a feature recognition method based on a new concept called holistic attribute adjacency graph (HAAG) for aircraft structural parts. The HAAG extended the nodes and the attributes of the nodes in order to represent the geometrical and topological information of the part accurately.

Benefitting from the HAAG, the intersecting features, convex features and features consisted of freeform surface were able to be recognized. More research about feature recognition can be found in [75-77].

### 3.2.2 Data Exchange between CAD/CAPP/CAM

Although the feature concept has been proposed for a long time, it is still difficult to give a uniform machining feature definition. International Standards Organization (ISO) tried to create a machining feature definition standard. The definitions or descriptions of different machining features are given in one of its application protocol (AP). ISO 10303 is an ISO standard for the computer-interpretable representation and exchange of product manufacturing information. It is known informally as STEP, which stands for Standard for the Exchange of Product data model. It follows the feature definitions of AP 224. Recently STEP-NC has been proposed as a machine tool control language that extends the ISO 10303 STEP standards. Many researchers took advantage of STEP and STEP-NC to generate tool paths automatically [78-80].

#### 3.2.3 Feature-based NC programming

In order to improve the control and information integration capability of an NC machining system, Zhang et al. [81] suggested an NC feature unit (NCFU), which was a feature-based basic control unit. The NCFU processed geometric form and control parameters so that they were used as an information exchange hub between NC systems and other manufacturing execution systems. Meanwhile, NCFU used a geometrically defined closed and non-gouging machined area. In such a way, a machining volume

object could be divided into a set of NCFUs to generate tool path in real-time. Hou and Faddis [82] discussed the automation of tool path generation in an integrated CAD/CAPP/CAM system based on machining features. An integration layer between FBMach and Unigraphics was implemented to achieve CAD/CAPP/CAM integration based on machining features. Li et al. [83] developed a feature-based rapid programming system for aircraft structural parts. Machining feature was employed as carrier of process knowledge to drive tool path generation automatically.

## 3.3 Intelligent Machining

The most recent research after automatic machining is intelligent machining. More knowledge with artificial intelligence technologies were applied to process planning, and to the prediction of on-line situations, and make real time decisions. The intermediate states of the machining features are considered in the process planning. And more complex situations such as machining of freeform surfaces were studied. The representative technologies include intelligent process planning, freeform surface feature machining, close-loop machining and definition of dynamic features.

#### 3.3.1 Computer Aided Process Planning

Benefiting from the development of feature technology, process planning has made much progress.

Automatic or semi-automatic process planning was made possible through machining features as semantic carrier of machining process. Process planning can be divided into three levels: multi-domain process planning, macro process planning and micro process planning [84]. Most previous research about

process planning focused on macro process planning and micro process planning. In macro level planning, the best sequence of multiple different processing steps and set-ups as well as the machines are selected. In micro level planning, the details of each individual machining operations are optimized to determine the best process parameters. Some researchers optimized the machining process by integrating macro and micro levels.

Kafashi [85] presented a generative system and genetic algorithm (GA) to improve integrated setup planning and operation sequencing by adding tolerance relationships analysis in the problem constraints.

Azab and ElMaraghy [86] gave a mathematical modeling method for reconfigurable process planning. Zhang and Ge [87] proposed an approach to determining optimal cutting tool sequences for machining multiple features in a single setup. Banerjee et al. [88] described an integrated process planning approach for optimal corner machining which combined tool path generation and machining parameter selection tasks. Rauch and Hascoet [89] proposed an approach to enhancing the implementation of plunge milling tool paths by computing the achievable material removal rate according to the tool path parameterization, the machine tool dynamics, and the machined feature properties.

Harik et al. [90] developed a computer aided process planning system for aircraft manufacturing. A finer granularity machining feature called elementary manufacturing feature was proposed in their system.

One elementary manufacturing feature consisting of a face or a face chain was associated with one

machining operation. However, it was difficult to optimize the global process plan. Villeneuve et al. [91] presented a strategy and two models to perform a CAPP system. A feature model was developed to match machining processes adapted to aircraft knowledge. An activity model was developed to identify and clarify the tasks to be performed and the process data involved in making planning decisions. A more comprehensive review of process planning is given in [92].

#### 3.3.2 Freeform Surface Feature Machining

Research on freeform surface feature machining can be divided into process planning and tool path optimization. Process planning for FSF focused on the optimization of machining operation sequencing and the selected manufacturing resources, such as machine tools and cutters. For different machining stages, different optimization criteria should be applied. Because roughing strives for the highest material removal rate, normally 3-axis machine tools combined with the flat-bottomed cutter is applied. Lee et al. [93] proposed a method to combine the cutters for machining different levels to improve the machining efficiency of roughing operations. Chen et al. [94] developed an integer programming (IP) method and a dynamic programming (DP) method to automate the traditional, experience-based cutter selection tasks and to reduce the total machining time in NC machining operations.

Semi-finishing aims to achieve even machining allowance for finishing stage. Finishing is intended to achieve the high machining quality with high machining efficiency. For 3-axis machining, the cutter is

selected according to the curvature of freeform surface. For multiple-axis machining, Lee and Chang [95] represented the effective cutting radius of a cutter by a function of the cutter size and the cutter orientation angles, and selected the optimal cutter by geometric evaluation through the maximum effective cutting radius approach. Li and Zhang [96] developed a search algorithm which was able to find the accessible posture range for a given cutter in terms of the tilting and rotational angles. Then, the optimal cutter was selected to finish the entire surface without any interference.

Tool path optimization for freeform surface features can be classified into cutting width optimization, feedrate optimization, cutting force optimization, cutter orientation, and the combination according to different objectives. Cutting width optimization is also called strip-width maximization machining which is intended to increase the effective cutting width as long as possible to achieve the shortest tool path and highest machining efficiency. Lee and Ji [97] established the relationship between the strip width and the cutter orientation, cutting direction and the geometrical parameters of the cutter to optimize the tool path. Cutting direction optimization indicated that the feedrate direction of every cutter location point was opimized under the limitation of the machine tool. Sencer et al [98] expressed the variation of the feed along the five-axis tool path in a cubic B-spline form and adjusted the feed control points of the B-spline to maximize the feed along the tool path without violating the programmed feed and the drives' physical limits.

The cutting force should also be optimized to improve the machining stability. Guzel and Lazoglu [99] presented an mathematical model for the prediction of cutting force system in ball-end milling of sculpture surfaces, which was used for selecting varying and appropriate feed values along the tool path in order to reduce the cycle time in sculpture surface machining. Through optimizing the cutter orientation, the interference and the smoothness of cutter orientation change were improved. Wang and Tang [100] presented an algorithm which could automatically generate a 5-axis toolpath that was not only interference-free but also guaranteed the angular-velocity compliance. Sun et al. [101] proposed a cutter orientation adjustment method to obtain an optimized tool path which made best use of the kinematic characteristics of angular feed for five-axis machining.

#### 3.3.3 Closed-loop Machining

Efforts have been made in on-line adjustment of cutting parameters and emergency actions, and on-line tool path compensation. Katz et al. [102] presented a closed-loop machining cell for turbine blade finishing that integrated a robotic surface finishing device with an electro-optical, non-contact precision measuring system. Lasemi [103] developed a manufacturing method by integrating inspection and tool path generation to improve manufacturing quality while reducing manufacturing efforts. Some error compensation models were established based on the on-line inspection results and the positive errors were compensated by adjusting the tool path [104-105] (Bohez et al., 2000, Ye and Xiong, 2008). Ridwan et al. [106] (2012) proposed a system that consisted of an optimization module, a process control module and a

knowledge-based evaluation module, where STEP-NC was the underlying data model for optimization.

# 3.3.4 Dynamic Features

In order to optimize the process plan of complex parts, the intermediate status of machining features need to be modeled [107]. Ramesh et al. [108] established a feature template library for automotive components. Each type of feature template defined the removal volume. When designing a part using the feature template library, the intermediate status of machining features could be generated automatically. Park [109-111] extracted the boundary of the machined face and extruded the boundary to generate the removal volume of the machined surface. The intersection of the removal volume and the swept volume of cutter was the actual removal volume. The actual removal volumes were subtracted from the workpiece to generate the intermediate status of machining features. Li et al. [112] presented a dynamic feature representation method for high value parts consisting of complex and intersecting features. The method first extracted features from the CAD model of a complex part. Then the dynamic status of each feature was established between various operations to be carried out during the whole manufacturing process. Each manufacturing and verification operation could be planned and optimized using the real conditions of a feature, thus enhancing accuracy, traceability and process control. The authors' latest research in intelligent manufacturing based on a new dynamic feature concept is presented in Section 4 below.

# 4. A Multi-perspective Dynamic Feature Concept for Intelligent Machining

This Section presents the latest research outcome of the Authors' research team in intelligent machining. The authors' most important contribution to this research domain is a new concept of multi-perspective dynamic feature (MpDF) that has been implemented and applied to the aerospace industry. The authors recognised that, in current commercial and reported research prototype systems, features once defined normally remain unchanged in the whole manufacturing cycle, which are referred to as *static features* in this paper. Machining planning and optimisation based on static features often need manual corrections in response to various changes in dynamic production situations. Using the Multi-perspective Dynamic Feature (MpDF) concept, changes in feature geometry and associated technical information can be represented within and complementary to existing feature-based CAD models so that adaptive machining planning and optimisation can be carried out with accurate and actual component and resource information.

#### 4.1 Definition of Multi-perspective Dynamic Features

Changes of a feature during machining are defined in three perspectives as shown in Figure 2: (i) the geometry of a feature in the depth-of-cut direction changes during different machining operations such as roughing, semi-finishing and finishing; (ii) changes across the surface: a surface may be divided into different machining regions (effectively sub-features) for the selection of appropriate manufacturing methods for each region such as different cutting tools, parameters, set-ups or machine tools; and (iii)

changes in resources or manufacturing capabilities may require the re-planning of depth-of-cuts, division of machining regions and manufacturing operations (machines, tools, set-ups and parameters). The MpDF concept could be used to support machining decision making of complex parts with complex structures (and with freeform surfaces), and can be formulated as:

$$\begin{cases} MpDF = \bigcup_{i=1}^{N} IF_{i} \\ IF_{i} = \Gamma_{(OO_{T}, MR_{T})}^{i}(P) = \bigcup_{j=1}^{M} SF_{j} \end{cases}$$

Where IF refers to an interim feature with its sub-feature (SF) on part (P).  $\Gamma$  refers to the feature division algorithm.  $OO_T$  and  $MR_T$  are the optimisation objectives and manufacturing resources. With the MpDF concept, a feature information model in CAD systems can be defined dynamically in the whole manufacturing cycle, thus supporting on-line adaptive machining planning.

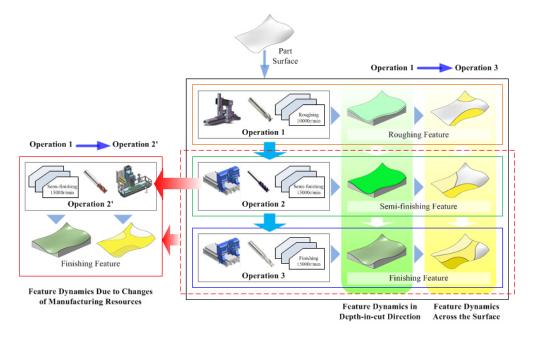


Figure 2. Changes of a feature defined in MpDF.

### **4.2** Feature Dynamics in the Depth-of-cut Direction

Feature dynamics in the depth-of-cut direction defines interim features to represent the information about real feature status and changes in its geometry between different machining operations [112]. Undesired machining effects like overcut and undercut in interim features are detected to evaluate existing process plans. Machining effects transition (MET) are then carried out by considering certain validity constraints to optimise the process plan in a much more global way. Moreover, interim features provide a possibility to define features for different machining stages like roughing, semi-finishing and finishing. By considering feature dynamics in this perspective, each manufacturing and verification operation can be planned and optimised using the real conditions of a feature, thus enhancing accuracy, traceability and process control.

#### 4.3 Feature Dynamics across the Feature Surface

Feature dynamics across a surface indicates that the surface may have to be further divided into several machining regions (effectively sub-features) for the selection of appropriate manufacturing methods for individual machining regions including cutters, parameters, set-ups and machine tools. Surface subdivision aims for better machining results, for example, flat-end cutters may be chosen to machine convex and relatively flat regions, while ball-end cutters may be used to machine concave regions with small curvature to avoid gouging/overcutting. The authors' developed a surface subdivision method based on tensor field and a boundary point classification principle. Existing freeform surface

machining optimisation methods are mainly based on scalar or vector which only represents the machining information in one feed direction at a time as shown in Figure 3. For example, only the directions with maximal cutting width are defined in Machining Potential Field [113]. Since the complex nature of geometry and machining operation, optimised results cannot be achieved everywhere in the freeform surface. Thus most of these methods are greedy, and only local optimised machining results can be achieved.

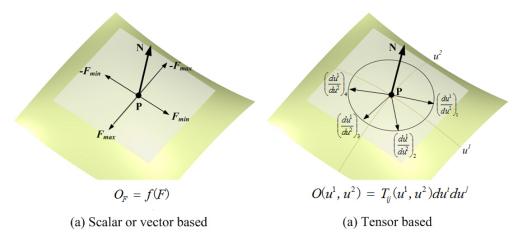


Figure 3. Representations of optimisation objectives.

To overcome the shortcoming, optimization objectives are represented based on a second-order tensor, i.e.,

$$O(\mathbf{u})=T_{ij}(\mathbf{u})du^idu^j,(i,j=1 \text{ or } 2)$$

Where  $\mathbf{u} \equiv [\mathbf{u}^1 \ \mathbf{u}^2]^T$ ,  $O(\mathbf{u})$  is the second order tensor with which a complete and continuous

representation of solutions at every cutter location could be obtained. Each  $T_{ij}(\mathbf{u})$  has two eigenvalues:  $e_{max}$  and  $e_{min}$ . The eigenvectors of  $e_{max}$  and  $e_{min}$  refer to the directions with the maximum and minimum  $O(\mathbf{u})$  respectively. The sub-feature boundaries within the surface could be machined using both cutting methods of the adjacent features like cutters, parameters, set-ups or feed directions according to the optimisation objectives. Thus points located at sub-feature boundaries could be classified into two classes:

- The adjacent sub-features have different cutting methods to machine the point. However, both methods are optimised at this point. In this condition, e<sub>max</sub> equals to e<sub>min</sub>. Thus O(**u**) at every feasible feed direction refers to optimised machining result. This kind of boundary point is called degenerate boundary point (DBP);
- The adjacent sub-features have the same cutting method to machine this point. In this condition, the maximum or minimum eigenvector at the point is coincident with the tangent vector of the tensor line crossing the point. This kind of boundary points is named as normal boundary point (NBP).

A two-step procedure is developed to construct sub-feature boundaries as shown in Figure 4. DBPs in the surface are generated as the starts to construct sub-feature boundaries. Firstly, a tensor is selected based on the current  $\{MO_i, OO^i_T, MR^i_T\}$  from a predefined tensor base. Then points with only one eigenvalue  $(e_{max} \equiv e_{min})$  are extracted as DBPs. DBPs could be classified into trisector points, wedge points and merge wedge points [114]. Only trisector points are selected since there are no sub-feature

boundaries crossing the other two types of DBPs. Points surrounding each trisector point are first extracted and potential sub-feature boundaries are constructed by connecting the surrounding points and the trisector point.  $\theta$  is defined as the angle between the maximal eigenvector at the surrounding point and its potential sub-feature boundary. The surrounding points (where  $\theta \cong 0$ ) are selected as NBPs. For each trisector point, there are three NBPs which will be selected as the second points of the three sub-feature boundaries that start from this trisector point. Then NBP searching with minimal  $\theta$  for each sub-feature boundary will be continued from the generated NBP.

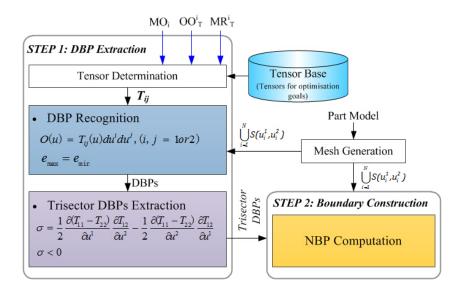


Figure 4. Procedure for sub-feature boundaries construction.

Currently, the authors have obtained the tensor metrics for cutting width and machining time considering machine kinematics. Figure 5 shows two examples for cutting width maximisation in surface

finishing. The test surface is first divided into several sub-regions using the proposed tensor based method. Then in each sub-surface, tool paths will be generated by offseting the initial tool path curve which follows the optimal feed direction (with maximal machining strip width) at every discrete point. Compared with the iso-parametric tool paths, both the tool path length and machining time are much reduced by applying MpDF concept.

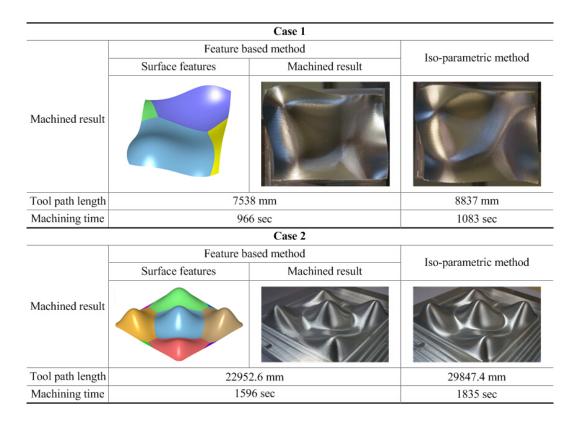


Figure 5. Two cases for cutting width maximisation in surface finishing.

## 4.3 Feature Dynamics due to Changes of Manufacturing Resources

Feature dynamics due to changes of manufacturing resources is important for intelligent machining

in todays' manufacturing industry which faces more and more uncertainties. Machine tools, cutters, fixtures as well as cutting parameters may have to be changed frequently due to factors like product changeover, urgent job insertion and broken tools. Normally machining operations and optimisation objectives, once planned, remain unchanged during the whole manufacturing cycle. However, the selected manufacturing resources in initial planning stage are often changed by engineers in real production. If the changes are due to re-scheduling of resources or machine breakdown, the planned machining operations as well as optimisation objectives may need to be re-planned which can lead to changes in both the interim features and the way sub-features are generated for each interim feature as shown in Figure 6. As a result, the MpDF information model would be updated, and thus adaptive machining planning is supported with the timely accurate information in the MpDF model.

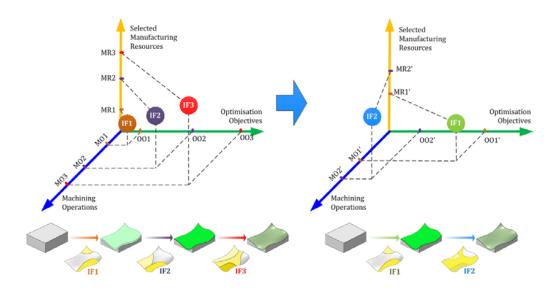


Figure 6. Feature changes due to changes of machining resources.

## 5. Summary and Future Outlook

Section 2 of this paper provides an overview of the main theories, methods and technologies addressing a range of key engineering aspects of recent research in CNC machining, focusing on three themes, i.e. simulation, optimization and automation. Various physical aspects (including geometry and dynamics) are simulated in order to predict the results before actual machining takes place; using advanced mathematical models, algorithms and computing technologies to tackle complex problems and produce more reliable predictions, and improve process data (including tool paths) to achieve better machining outcome.

There are various process (machining) parameters, and selecting the best set of parameters is an almost impossible task. Taking advantage of simulation, optimization, and automation, 'near' optimal machining processes may be derived, instead of merely usable processes. The optimization problems are usually solved numerically. These efforts substitute human decision making with mathematical reasoning. However, the technology is still at the early stage of intelligent machining, and there is still significant work to be done.

Section 3 of this paper provides an introduction to the enabling information and computing technologies (ICT) that bring the methods and technologies in CNC together into integrated systems with various modeling and decision making modules to support intelligent machining. As the information and knowledge carrier, feature is the efficacious way to achieve intelligent manufacturing. From the regular

shaped feature to freeform surface feature, the feature technology has been used in manufacturing of complex parts, such as aircraft structural parts. Meanwhile, the dynamic feature definition provides a very efficient and effective mean of optimizing the complex machining process.

To summarize this review, the authors believe that the research in CNC machining has entered a new phase: intelligent machining. It will be a flourishing research area and exciting new results and progress will be seen in the forth-coming years. Section 4 of this paper presented a comprehensive multi-perspective dynamic feature concept proposed by the authors, which has the potential to model the actual status of features during different operations in real production situations, thus supporting more accurate prediction, planning and optimization. As an initial contribution to the intelligent machining research, the authors anticipate more international research into this important research area.

## Acknowledgement

This work was funded by the National Natural Science Foundation Project of China (No.51375239), the National Science and Technology Major Project of China (No.2012ZX04010041) and the Jiangsu Province Outstanding Youth Fund (No. BK20140036). International collaboration was supported and included in these projects.

## References

- [1] Hu P, Tang K and Lee C-H. Global obstacle avoidance and minimum workpiece setups in five-axis machining. *Computer-Aided Design* 2013; 45: 1222-1237.
- [2] Hu P and Tang K. Improving the dynamics of five-axis machining through optimization of workpiece setup and tool orientations. *Computer-Aided Design* 2011; 43: 1693-1706.
- [3] Anotaipaiboon W and Makhanov SS. Minimization of the kinematics error for five-axis machining.

  \*Computer-Aided Design 2011; 43: 1740-1757.
- [4] Nelaturi S, Rangarajan A, Fritz C and Kurtoglu T. Automated fixture configuration for rapid manufacturing planning. *Computer-Aided Design* 2014; 46: 160-169.
- [5] Redonnet J-M, Djeball S, Segonds S, Senatore J and Rubio W. Study of the effective cutter radius for end milling of free-form surfaces using a torus milling cutter. *Computer-Aided Design* 2013; 45: 951-962.
- [6] Chen ZC and Fu Q. An optimal approach to multiple tool selection and their numerical control path generation for aggressive rough machining of pockets with free-form boundaries. *Computer-Aided Design* 2011; 43: 651-663.
- [7] Senatore J, Segonds S, Rubio W and Dessein G. Correlation between machining direction, cutter geometry and step-over distance in 3-axis milling: Application to milling by zones. *Computer-Aided Design* 2012; 44: 1151-1160.

- [8] Zhu L, Ding H and Xiong Y. Simultaneous optimization of tool path and shape for five-axis flank milling. Computer-Aided Design 2012a; 44: 1229-1234.
- [9] Gong H and Wang N. 5-axis flank milling free-form surfaces considering constraints. *Computer-Aided Design* 2011; 43: 563-572.
- [10] Yuen A, Zhang K and Altintas Y. Smooth trajectory generation for five-axis machine tools.

  \*International Journal of Machine Tools and Manufacture 2013; 71: 11-19.
- [11] Chen ZC, Dong Z and Vickers GW. 2003. Automated surface subdivision and tool path generation for -axis CNC machining of sculptured parts. *Computers in Industry* 2003; 50: 319-331.
- [12] Beudaert X, Lavernhe S and Tournier C. 5-axis local corner rounding of linear tool path discontinuities. *International Journal of Machine Tools and Manufacture* 2013; 73: 9-16.
- [13] Zhao H, Zhu L and Ding H. A real-time look-ahead interpolation methodology with curvature-continuous B-spline transition scheme for CNC machining of short line segments.

  International Journal of Machine Tools and Manufacture 2013; 65: 88-98.
- [14] Bouard M, Pateloup V and Armand P. Pocketing toolpath computation using an optimization method.
  Computer-Aided Design 2011; 43: 1099-1109.
- [15] Beudaert X, Pechard P-Y and Tournier C. 2011. 5-Axis tool path smoothing based on drive constraints. *International Journal of Machine Tools and Manufacture* 2011; 51: 958-965.
- [16] Blackmore D, Leua MC and Wang LP. The sweep-envelope differential equation algorithm and its

- application to NC machining verification. Computer-Aided Design 1997; 29: 629-637.
- [17] Plakhotnik D and Lauwers B. Computing of the actual shape of removed material for five-axis flat-end milling. *Computer-Aided Design* 2012; 44: 1103-1114.
- [18] Wu W, Li J and Feng Q. Simulation of the surface profile of the groove bottom enveloped by milling cutters in single screw compressors. *Computer-Aided Design* 2011; 43: 67-71.
- [19] Lee SW and Nestler A. Complete swept volume generation, Part I: Swept volume of a piecewise C1-continuous cutter at five-axis milling via Gauss map. *Computer-Aided Design* 2011; 43: 427-441.
- [20] Sullivan A, Erdim H, Perry RN and Frisken SF. High accuracy NC milling simulation using composite adaptively sampled distance fields. *Computer-Aided Design* 2012; 44: 522-536.
- [21] Beudaert X, Lavernhe, S and Tournier C. Feedrate interpolation with axis jerk constraints on 5-axis NURBS and G1 tool path. *International Journal of Machine Tools and Manufacture* 2012; 57: 73-82.
- [22] Guo J-X, Zhang K, Zhang Q and Gao XS. Efficient time-optimal feedrate planning under dynamic constraints for a high-order CNC servo system. *Computer-Aided Design* 2013; 45: 1538-1546.
- [23] Annoni M, Bardine A, Campanelli S, Foglia P and Prete CA. A real-time configurable NURBS interpolator with bounded acceleration, jerk and chord error. *Computer-Aided Design* 2012; 44: 509-521.
- [24] Giri V, Bezbaruah D, Bubna P and Roy CA. Selection of master cutter paths in sculptured surface machining by employing curvature principle. *International Journal of Machine Tools and*

- Manufacture 2005; 45: 1202-1209.
- [25] Qiao Z, Wang T, Wang Y, Hu M and Liu Q. Bézier polygons for the linearization of dual NURBS curve in five-axis sculptured surface machining. *International Journal of Machine Tools and Manufacture* 2012; 53: 107-117.
- [26] Lee A-C, Lin M-T, Pan Y-R and Lin W-Y. The feedrate scheduling of NURBS interpolator for CNC machine tools. *Computer-Aided Design* 2011; 43: 612-628.
- [27] Peng FY, Ma JY, Wang W, Duan XY, Sun PP and Yan R. Total differential methods based universal post processing algorithm considering geometric error for multi-axis NC machine tool. *International Journal of Machine Tools and Manufacture* 2013; 70: 53-62.
- [28] Tsutsumi M, Tone S, Kato N and Sato R. Enhancement of geometric accuracy of five-axis machining centers based on identification and compensation of geometric deviations. *International Journal of Machine Tools and Manufacture* 2013; 68: 11-20.
- [29] Ibaraki S, Iritani T and Matsushita T. Error map construction for rotary axes on five-axis machine tools by on-the-machine measurement using a touch-trigger probe. *International Journal of Machine Tools and Manufacture* 2013; 68: 21-29.
- [30] Zhu S, Ding G, Qin S, Lei J, Zhuang L and Yan K. Integrated geometric error modeling, identification and compensation of CNC machine tools. *International Journal of Machine Tools and Manufacture* 2012b; 52: 24-29.

- [31] Vahebi Nojedeh M, Habibi M and Arezoo B. Tool path accuracy enhancement through geometrical error compensation. *International Journal of Machine Tools and Manufacture* 2011; 51: 471-482.
- [32] Soori M, Arezoo B and Habibi M. Dimensional and geometrical errors of three-axis CNC milling machines in a virtual machining system. *Computer-Aided Design* 2013; 45: 1306-1313.
- [33] Andolfatto L, Lavernhe S and Mayer JRR. Evaluation of servo, geometric and dynamic error sources on five-axis high-speed machine tool. *International Journal of Machine Tools and Manufacture* 2011; 51: 787-796.
- [34] Zhang K, Yuen A and Altintas Y. Pre-compensation of contour errors in five-axis CNC machine tools.

  International Journal of Machine Tools and Manufacture 2013; 74: 1-11.
- [35] Lin M-T and Wu S-K. Modeling and improvement of dynamic contour errors for five-axis machine tools under synchronous measuring paths. *International Journal of Machine Tools and Manufacture* 2013; 72: 58-72.
- [36] Zhu L, Zhao H and Ding H. Real-time contouring error estimation for multi-axis motion systems using the second-order approximation. *International Journal of Machine Tools and Manufacture* 2013; 68: 75-80.
- [37] Huo F and Poo A-N. Improving contouring accuracy by using generalized cross-coupled control.

  International Journal of Machine Tools and Manufacture 2012; 63: 49-57.
- [38] Huo F, Xi X-C and Poo A-N. Generalized Taylor series expansion for free-form two-dimensional

- contour error compensation. *International Journal of Machine Tools and Manufacture* 2012; 53: 91-99.
- [39] Shen H, Fu J, He, Y. and Yao X. On-line Asynchronous Compensation Methods for static/quasi-static error implemented on CNC machine tools. *International Journal of Machine Tools and Manufacture* 2012; 60: 14-26.
- [40] Tutunea-fatan, OR and Bhuiya MSH. Comparing the kinematic efficiency of five-axis machine tool configurations through nonlinearity errors. *Computer-Aided Design* 2011; 43: 1163-1172.
- [41] Habibi M, Aerzoo B and Vahebi Nojedeh M. Tool deflection and geometrical error compensation by tool path modification. *International Journal of Machine Tools and Manufacture* 2011; 51: 439-449.
- [42] Wan X-J, Hua L, Wang X-F, Peng Q-Z and Qin X-P. An error control approach to tool path adjustment conforming to the deformation of thin-walled workpiece. *International Journal of Machine Tools and Manufacture* 2011; 51: 221-229.
- [43] Kang Y-G and Wang Z-Q. Two efficient iterative algorithms for error prediction in peripheral milling of thin-walled workpieces considering the in-cutting chip. *International Journal of Machine Tools and Manufacture* 2013; 73: 55-61.
- [44] Wei ZC, Wang MJ, Zhu JN and Gu LY. Cutting force prediction in ball end milling of sculptured surface with Z-level contouring tool path. *International Journal of Machine Tools and Manufacture* 2011; 51: 428-432.

- [45] Liang X-G and Yao Z-Q. An accuracy algorithm for chip thickness modeling in 5-axis ball-end finish milling. *Computer-Aided Design* 2011; 43: 971-978.
- [46] Huang T, Zhang X, Zhang X and Ding H. An efficient linear approximation of acceleration method for milling stability prediction. *International Journal of Machine Tools and Manufacture* 2013; 74: 56-64.
- [47] Quo Q, Sun Y and Jiang Y. On the accurate calculation of milling stability limits using third-order full-discretization method. *International Journal of Machine Tools and Manufacture* 2012; 62: 61-66.
- [48] Liu Y, Zhang D and Wu B. An efficient full-discretization method for prediction of milling stability.

  International Journal of Machine Tools and Manufacture 2012; 63: 44-48.
- [49] Zhang X and Ding H. Note on a novel method for machining parameters optimization in a chatter-free milling process. *International Journal of Machine Tools and Manufacture* 2013; 72: 11-15.
- [50] Zhang X, Zhu L, Zhang D, Ding H and Xiong Y. Numerical robust optimization of spindle speed for milling process with uncertainties. *International Journal of Machine Tools and Manufacture* 2012; 61: 9-19.
- [51] Bok AY and Mansor MSA. Generative regular-freeform surface recognition for generating material removal volume from stock model. *Computers & Industrial Engineering* 2013; 64: 162-178.
- [52] Sundararajan V and Wright PK. Volumetric feature recognition for machining components with

- freeform surfaces. Computer-Aided Design 2004; 36: 11-25.
- [53] Meeran S and Pratt MJ. Automated feature recognition from 2D drawings. *Computer-Aided Design* 1993; 25: 7-17.
- [54] Tyan L-W and Devarajan V. Automatic identification of non-intersecting machining features from 2D CAD input. Computer-Aided Design 1998; 30: 357-366.
- [55] Meeran S and Taib JM. A generic approach to recognising isolated, nested and interacting features from 2D drawings. *Computer-Aided Design* 1999; 31: 891-910.
- [56] Chen K-Z, Feng X-A and Lu Q-S. Intelligent dimensioning for mechanical parts based on feature extraction. *Computer-Aided Design* 2001; 33: 949-965.
- [57] Wang J, Wang Z, Zhu W and Ji Y. Recognition of Freeform Surface Machining Features. *Journal of Computing and Information Science in Engineering* 2010; 10: 041006.
- [58] Alam MR, Lee KS, Rahman M and Zhang YF. Automated process planning for the manufacture of sliders. *Computers in Industry* 2000; 43: 249-262.
- [59] Hayasi MT and Asiabanpour B. A new adaptive slicing approach for the fully dense freeform fabrication (FDFF) process. *Journal of Intelligent Manufacturing* 2011; 24: 683-694.
- [60] Zhao Z, Ghosh SK and Link D. Recognition of machined surfaces for manufacturing based on wireframe models. *Journal of Materials Processing Technology* 1990; 24: 137-145.
- [61] Vosniakos G. An intelligent software system for the automatic generation of NC programs from

- wireframe models of 2-1/2D mechanical parts. *Computer Integrated Manufacturing Systems* 1998; 11: 53-65.
- [62] Langerak TR. Local parameterization of freeform shapes using freeform feature recognition.

  \*Computer-Aided Design 2010; 42: 682-692.
- [63] Han J-H, Pratt M and Regli W. Manufacturing feature recognition from solid models a status report. *IEEE Transactions on Robotics and Automation* 2000; 16: 782-796.
- [64] Corney J, Hayes C, Sundararajan V and Wright P. The CAD/CAM Interface: A 25-Year Retrospective. *Journal of Computing and Information Science in Engineering* 2005; 5: 188-197.
- [65] Woo Y, Wang E, Kim YS and Rho HM. A Hybrid Feature Recognizer for Machining Process Planning Systems. *CIRP Annals Manufacturing Technology* 2005; 54: 397-400.
- [66] Dimov SS, Brousseau EB and Setchi R. A hybrid method for feature recognition in computer-aided design models. *Proceedings of the Institution of Mechanical Engineers, Part B: Journal of Engineering Manufacture* 2007; 221: 79-96.
- [67] Arivazhagan A, Mehta NK and Jain PK. A STEP AP 203-214-based machinable volume identifier for identifying the finish-cut machinable volumes from rough-machined parts. The *International Journal* of Advanced Manufacturing Technology 2009; 42: 850-872.
- [68] Marchetta MG and Forradellas RQ. An artificial intelligence planning approach to manufacturing feature recognition. *Computer-Aided Design* 2010; 42: 248-256.

- [69] Heo E-Y, Kim D-W, Lee J-Y, Lee C-S and Chen F. High speed pocket milling planning by feature-based machining area partitioning. *Robotics and Computer-Integrated Manufacturing* 2011; 27: 706-713.
- [70] Yu F, Du B, Ren W, Zheng G and Chu H. Slicing Recognition of Aircraft Integral Panel Generalized Pocket. *Chinese Journal of Aeronautics* 2008; 21: 585-592.
- [71] Chu X, Tang C, Xue D, Su Y and Sun X. Identification of machining features based on available resources of cutting tools. *International Journal of Production Research* 2012; 50: 4141-4157.
- [72] Yu F, Zheng G, Rao Y, Du B and Chu H. Principal Face-based Recognition Approach for Machining Features of Aircraft Integral Panels. *Chinese Journal of Mechanical Engineering* 2011; 24: 976-982.
- [73] Zeng D, Zeng C, Zhao H and Zheng G. Simulated rolling method for the recognition of outer profile faces of aircraft structural parts. *Advances in Engineering Software* 2012; 47: 51-61.
- [74] Li YG, Ding YF, Mou WP and Guo H. Feature recognition technology for aircraft structural parts based on a holistic attribute adjacency graph. *Proceedings of the Institution of Mechanical Engineers,*Part B: Journal of Engineering Manufacture 2010; 224: 271-278.
- [75] Babic BR, Nesic N and Miljkovic Z. Automatic feature recognition using artificial neural networks to integrate design and manufacturing: Review of automatic feature recognition systems. *Artificial Intelligence for Engineering Design, Analysis and Manufacturing* 2011; 25: 289-304.
- [76] Verma AK and Rajotia S. A review of machining feature recognition methodologies. International

- Journal of Computer Integrated Manufacturing 2010; 23: 353-368.
- [77] Babic B, Nesic N and Miljkovic Z. A review of automated feature recognition with rule-based pattern recognition. *Computers in Industry* 2008; 59: 321-337.
- [78] Xu XW, Wang L and Rong Y. STEP-NC and function blocks for interoperable manufacturing. *IEEE Transactions on Automation Science and Engineering* 2006; 3: 297-308.
- [79] Cuenca S, Jimeno-Morenilla A, Mart Nez A and Maestre R. Hardware approach to tool path computation for STEP-NC enabled CNC: A case study of turning operations. *Computers in Industry* 2011; 62: 509-518.
- [80] Kretz D, Teich T, Militzer J and Neumann T. Implementing ISO standard 10303 application protocol 224 for automated process planning. *Robotics and Computer-Integrated Manufacturing* 2011; 27: 729-734.
- [81] Zhang L, Deng J and Chan SC-F. A Next Generation NC Machining System Based on NC Feature Unit and Real-Time Tool-Path Generation. *The International Journal of Advanced Manufacturing Technology* 2000; 16: 889-901.
- [82] Hou M and Faddis TN. Automatic tool path generation of a feature-based CAD/CAPP/CAM integrated system. *International Journal of Computer Integrated Manufacturing* 2006; 19: 350-358.
- [83] Li YG, Fang TL, Cheng SJ and Liao WH. Research on Feature-Based Rapid Programming for Aircraft NC Parts. Applied Mechanics and Materials 2008; 10-12: 682-687.

- [84] Elmaraghy HA. Reconfigurable Process Plans for Responsive Manufacturing Systems. In: CUNHA,
  P. F. & MAROPOULOS, P. G. (eds.) *Digital Enterprise Technology*. New York, USA: Springer-Verlag,
  2007.
- [85] Kafashi S. Integrated setup planning and operation sequencing (ISOS) using genetic algorithm. *The*International Journal of Advanced Manufacturing Technology 2011; 56: 589-600.
- [86] Azab A and Elmaraghy HA. Mathematical Modeling for Reconfigurable Process Planning. *CIRP Annals Manufacturing Technology* 2007; 56: 467-472.
- [87] Zhang Y and Ge L. Selecting optimal set of tool sequences for machining of multiple pockets. *The International Journal of Advanced Manufacturing Technology* 2009; 42: 233-241.
- [88] Banerjee A, Feng HY and Bordatchev EV. Process planning for corner machining based on a looping tool path strategy. *Proceedings of the Institution of Mechanical Engineers, Part B: Journal of Engineering Manufacture* 2011; 225: 1578-1590.
- [89] Rauch M and Hascoet J-Y. Selecting a milling strategy with regard to the machine tool capabilities: application to plunge milling. *The International Journal of Advanced Manufacturing Technology* 2012; 59: 47-54.
- [90] Harik RF, Derigent WJE and Ris G. Computer Aided Process Planning in Aircraft Manufacturing.

  \*Computer-Aided Design and Applications 2008; 5: 953-962.
- [91] Villeneuve F, Brissaud D, Zirmi O and Capponi V. Computer Aided Process Planning, Strategy, and

- Models in the Aircraft Industry. *Proceedings of the Institution of Mechanical Engineers, Part B:*Journal of Engineering Manufacture 2006; 220: 541-553.
- [92] Xu X, Wang L and Newman ST. Computer-aided process planning A critical review of recent developments and future trends. *International Journal of Computer Integrated Manufacturing* 2011; 24: 1-31.
- [93] Lee YS, Choi BK and Chang TC. Cut distribution and cutter selection for sculptured surface cavity machining. *International Journal of Production Research* 1992; 30: 1447-1470.
- [94] Chen Y-H, Lee Y-S and Fang S-C. Optimal cutter selection and machining plane determination for process planning and NC machining of complex surfaces. *Journal of Manufacturing Systems* 1998; 17: 371-388.
- [95] Lee YS and Chang TC. Automatic cutter selection for 5-axis sculptured surface machining.

  \*International Journal of Production Research 1996; 34: 977-984.
- [96] Li LL and Zhang YF. Cutter selection for 5-axis milling of sculptured surfaces based on accessibility analysis. *International Journal of Production Research* 2006; 44: 3303-3323.
- [97] Lee YS, Choi BK and Chang TC. Cut distribution and cutter selection for sculptured surface cavity machining. *International Journal of Production Research* 1992; 30: 1447-1470.
- [98] Sencer B, Altintas Y and Croft E. Feed optimization for five-axis CNC machine tools with drive constraints. *International Journal of Machine Tools and Manufacture* 2008; 48: 733-745.

- [99] Guzel BU and Lazoglu I. Increasing productivity in sculpture surface machining via off-line piecewise variable feedrate scheduling based on the force system model. *International Journal of Machine Tools and Manufacture* 2004; 44: 21-28.
- [100] Wang N and Tang K. Automatic generation of gouge-free and angular-velocity-compliant five-axis toolpath. *Computer-Aided Design* 2007; 39: 841-852.
- [101] Sun Y, Bao Y, Kang K and Guo D. A cutter orientation modification method for five-axis ball-end machining with kinematic constraints. *The International Journal of Advanced Manufacturing Technology* 2013; 67: 2863-2874.
- [102] Katz R, Srivatsan V and Patil L. Closed-loop machining cell for turbine blades. The *International Journal of Advanced Manufacturing Technology* 2011; 9–12: 869-881.
- [103] Lasemi A. An integrated approach for precision machining of freeform surfaces, PhD Thesis, University of Calgary, 2014.
- [104] Bohez E, Makhanov SS and Sonthipermpoon K. Adaptive nonlinear tool path optimization for five-axis machining. *International Journal of Production Research* 2000; 38: 4329-4343.
- [105] Ye T and Xiong C-H. Geometric parameter optimization in multi-axis machining. *Computer-Aided Design* 2008; 40: 879-890.
- [106] Ridwan F, Xu X and Liu G. A framework for machining optimisation based on STEP-NC. *Journal of Intelligent Manufacturing* 2012; 23: 423-441.

- [107] Zhang S, Shi Y, Fan H, Huang R and Cao J. Serial 3D model reconstruction for machining evolution of rotational parts by merging semantic and graphic process planning information. Computer-Aided Design 2010; 42: 781-794.
- [108] Ramesh M, Dutta D, Belludi N, Yip-hoi D and Wascher P. Application of feature technology to modeling and dimensioning the intermediate geometry of automotive powertrain components. In: SEIDEL, H.-P., SHAPIRO, V., LEE, K. & PATRIKALAKIS, N., eds. *The seventh ACM Symposium on Solid Modeling and Applications*, Saarbrücken, Germany. ACM, 2002, 313-320.
- [109] Park SC, Mukundan G, Gu S and Olling GJ. In-process model generation for the process planning of a prismatic part. *Journal of Advanced Manufacturing Systems* 2003; 2: 147-162.
- [110] Park SC. Associating a Design Model and its Machining Process Plan. *Computer-Aided Design & Applications* 2005; 2: 665-673.
- [111] Park S. Generating intermediate models for process planning. *International Journal of Production Research* 2006; 44: 2169-2182.
- [112] Li YG, Liu X, Gao JX and Maropoulos PG. A dynamic feature information model for integrated manufacturing planning and optimization. *CIRP Annals Manufacturing Technology* 2012; 61: 167-170.
- [113] Chiou C-J and Lee Y-S. A machining potential field approach to tool path generation for multi-axis sculptured surface machining. *Computer-Aided Design* 2002; 34: 357-371.

[114] Delmarcelle T. *The visualization of second-order tensor field*, PhD Thesis, Stanford University, 1994.