- ¹ Electrochemical synthesis and characterization of basic
- ² bismuth nitrate [Bi₆O₅(OH)₃](NO₃)₅·2H₂O: a potential highly
- ³ efficient sorbent for textile reactive dye removal

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9 Abstract

10 A new method of synthesis was developed for the preparation of basic bismuth 11 nitrate [Bi₆O₅(OH)₃](NO₃)₅·2H₂O (ECBBN). Electrochemical synthesis of the material was carried out by galvanostatic electrodeposition from an acidic Bi(III) 12 13 solution on a Ti substrate and further thermal treatment in air at 200 °C. Charac-14 terization of ECBBN was conducted by employing SEM-EDX, N2 adsorption, XRD 15 and FTIR, and its pI was also determined. The analyses showed that the material 16 obtained was pure [Bi₆O₅(OH)₃](NO₃)₅·2H₂O. Morphologically, ECBBN aggre-17 gates were composed of crystals, some smaller than 50 nm. Electrochemically syn-18 thesized sorbent (ECBBN) was used for the removal of the textile dye Reactive Blue 19 19 (RB19) from deionized water and model solutions of polluted river water, and 20 it showed considerably superior sorption performance compared to other inorganic 21 sorbents synthesized by conventional methods reported in the literature. A kinetic 22 study suggests that the sorption process is both under reaction and diffusion con-23 trol. Equilibration of the sorption process was attained in several minutes, i.e. the 24 sorption process is very fast. The sorption equilibrium data were well interpreted by 25 the Langmuir, Redlich-Peterson and Brouers-Sotolongo isotherm. Using Langmuir 26 isotherm, the maximum sorption capacity of ECBBN was reached at pH 2 and was 27 $1049.19 \text{ mg g}^{-1}$.

Keywords Basic bismuth nitrate · Electrochemical synthesis · Sorption · Textile
 dye · Reactive Blue 19

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30 Abbreviations

31	BBN	Basic bismuth nitrate
32	ECBBN	Electrochemically synthesized [Bi ₆ O ₅ (OH) ₃](NO ₃) ₅ ·2H ₂ O

- 33 RB19 Reactive Blue 19
- 34 pI Isoelectric point

35 Introduction

Synthetic dyes are major industrial pollutants and water contaminants due to their 36 large-scale production and extensive applications [1]. Many industries, such as dye, 37 textile, cosmetic, paper, plastics, leather, rubber, food and pharmaceuticals use dyes 38 to colour their products [2-4]. Significant quantities of synthetic dyes are 39 discharged into the environment from industrial effluents [5]. They give an intense 40 colour to the water and are toxic to the aquatic environment. Hence, wastewater 41 from dye produc-tion and industrial applications presents a serious threat to the 42 environment [6, 7]. Reactive Blue 19 (RB19) is an anthraquinone dye, and because 43 it is highly stabi-lized by resonance, it is very resistant to chemical oxidation [8]. 44 Several techniques such as chemical oxidation, biodegradation, photodegradation, 45 electrocoagulation, membrane separation and reverse osmosis have been developed 46 for treating water pollutants [9–13]. There are many studies of photocatalytic 47 degradation of RB19 by different bismuth compounds used as photocatalyst [14-48 19]. Relative to the forego-ing techniques adsorption is considered to be simple, 49 highly efficient and relatively inexpensive, and in a lot of studies, various organic 50 and inorganic compounds are successfully used for removal of RB19 dye [9, 20-51 271. 52

Basic bismuth nitrates (BBNs) in recent works are used as photocatalysts [28– 30] and in rare cases as sorbents [31] for pollutants removal from water. They are also used in medicine for the treatment of gastric and duodenal ulcers, gastritis, dyspep-sia, inflamed skin and functional disorders of the large intestine, stomach and duode-num [32]. Typical synthetic methods for the preparation of BBNs include precipita-tion [31], hydrolysis [30], hydrothermal [28] and microwaveassisted hydrothermal methods [29].

Electrodeposition, as one of the most common methods of electrochemical synthesis, is very attractive for material synthesis due to its simplicity and ability to easily control of deposition rate, thickness and uniformity of deposit by changing of the electrodeposition process parameters [33]. To our knowledge, electrochemical synthesis of BBNs has not been reported in the scientific literature.

The aim of the study reported herein was to develop a new method for the syn-65 thesis (electrochemical) of basic bismuth nitrate (ECBBN) and to characterize the 66 product by scanning electron microscopy/energy-dispersive X-ray spectroscopy 67 (SEM-EDX), nitrogen sorptometry, X-ray diffraction (XRD) and Fourier trans-68 form infrared spectroscopy (FTIR) analysis. In addition, the isoelectric point (pI) of 69 the ECBBN was determined. In order to investigate its applicability for textile dye 70 removal, removal of RB19 as a model pollutant in aqueous solutions was evalu-71 ated, as well as the removal of RB19 from model solutions of polluted river water. 72 The influence of pH, sorbent dose and initial dye concentration was also examined. Reaction and diffusion kinetics models (pseudo-first-order, pseudo-second-order
and intraparticle diffusion), as well as isotherm models (Langmuir, Freundlich,
Redlich–Peterson and Brouers–Sotolongo) were examined for a better understanding of the sorption process.

77 Experimental methods

78 Materials

Bismuth (III) nitrate pentahydrate was purchased from Acros Organics (USA).
Nitric acid, sodium hydroxide, ethanol and RB19 were purchased from SigmaAldrich (Germany). All chemicals used in this study were of analytical grade and
used without any further purification. Deionized water was used in all experiments.

83 Synthesis of basic bismuth nitrate

Basic bismuth nitrate was synthesized by electrodeposition from acidic bismuth 84 nitrate solution (0.1 mol dm⁻³ Bi(NO₃)₃ in 1.0 mol dm⁻³ HNO₃). Electrodeposition 85 was conducted in a galvanostatic regime at a current density of 150.0 mA cm^{-2} for 86 5.0 min at ambient temperature (25.0 ± 0.5 °C). A conventional two-electrode cell 87 was used for electrodeposition. A sheet of titanium $(10 \times 20 \text{ mm})$ was used as the 88 working electrode (cathode), while stainless-steel sheet (10×20 mm) was used as 89 the counter electrode (anode). The working and counter electrodes were at a dis-90 tance of 15 cm. All the electrodes were cleaned before the electrodeposition by pol-91 ishing with different abrasive papers and ultrasonic cleaning in ethanol and deion-92 ized water. Electrodeposition was carried out using an Amel 510 DC potentiostat 93 (Materials Mates, Italy) and a VoltaScope software package. After electrodeposi-94 tion, the titanium sheet with deposited material was dried at room temperature for 95 120 min. Finally, basic bismuth nitrate was obtained by thermal treatment at 200 °C 96 for 90 min. After cooling in air, the synthesized material was removed from the tita-97 nium sheet and powdered. 98

99 Characterization of sorbent

For SEM-EDX analysis, samples were attached to aluminium stubs using Leit-C car-100 bon cement. A cold FEG-SEM (SU8030, Hitachi, Japan) was used for imaging the 101 samples with Noran NSS system 7 ultra-dry X-ray detector (Thermo-scientific, USA) 102 for semi-quantitative EDX analysis. Samples were imaged uncoated. Nitrogen adsorp-103 tion measurements were performed on a Gemini 5 Surface Area Analyser (Micromer-104 itics, Norcross, Georgia, USA). Before the measurement, the samples were degassed 105 under flowing nitrogen at 40 °C for 20 h. The specific surface area was determined 106 using the Brunauer-Emmett-Teller (BET) method [34]. The Barret-Joyner-Halenda 107 (BJH) method was used for pore volume, area and diameter analysis [35]. The crys-108 tal structure was identified by X-ray diffraction (XRD) using a powder X-ray 109

diffractometer (Ultima IV, Rigaku, Japan). XRD studies of all the powders were con-110 ducted using Cu K α radiation ($\lambda = 1.5406$ nm) produced at 40 kV and 40 mA. Experi-111 ments were performed in the scan range $2\theta = 5^{\circ} - 90^{\circ}$ under 40 kV, 40 mA, using a scan 112 speed 5 ° min⁻¹ and step size of 0.02° . Before the measurements, angular corrections 113 were undertaken by using a reference Si standard. FTIR (Fourier transform infrared 114 spectrometer) spectra were recorded using KBr discs in the range of 400–4000 $\rm cm^{-1}$ 115 using a BOMEM MB-100 (Hartmann & Braun, Canada) FTIR spectrometer. The num-116 ber of scans was 16. The isoelectric point of the sorbent was determined by the salt 117 addition method [36]. NaNO₃ solution (0.1 mol dm^{-3}) was used as an inert electrolyte 118 and a series of test solutions were prepared by adjusting the pH of 50.0 cm³ of electro-119 lyte in the range 2.0–11.0 using 0.01 mol dm⁻³ HNO₃ and 0.01 mol dm⁻³ NaOH. Then 120 0.2 g of sorbent was added to each solution, sealed and stirred for 24 h, and the final pH 121 (pH_f) was measured. The pH_f values were plotted against the initial pH (pH_i), and the 122 pI was determined from the data where $pH_i = pH_f$. 123

124 Batch sorption experiments

Batch sorption experiments were performed to study the effect of parameters such as 125 contact time, pH, sorbent dose and initial dye concentration, as well as to determine 126 maximum sorption capacity. The experiments were carried out at ambient temperature 127 in a Petri dish by adding the desired amount of sorbent in prepared solutions of RB19 128 and stirred using a magnetic stirrer, and a series of sorption experiments were done 129 at different operating conditions by changing initial dye concentrations, initial sorb-130 ent doses, reaction times and pH of the solution. The pH of the experimental solutions 131 was adjusted by adding HNO₃ or NaOH. Residual RB19 concentration was determined 132 through the measurement of the dye solution absorbance at 592 nm by UV-visible 133 spectrophotometer (UV-1800, Shimadzu, Japan). Before the measuring of absorbance. 134 sorbent was separated from the solution by filtration using regenerated cellulose mem-135 brane filters with a 0.45 µm pore size (Agilent Technologies, Germany). The following 136 equations were utilized for determining the sorbed amount of dye q_t (mg g⁻¹) and the 137 dye removal efficiency (RE): 138

139

$$q_t = \frac{c_0 - c_t}{m} \cdot V \tag{1}$$

140

$$RE = \frac{c_0 - c_t}{c_0} \cdot 100\%$$
(2)

where c_0 and c_t (mg dm⁻³) are the initial and final concentrations of the RB19, *m* (g) is the mass of the sorbent and *V* (dm³) is the solution volume.

143 Relative mean deviation (*RMD*) was calculated by the following equation:

144

$$RMD = \frac{\sum_{i=1}^{n} \left| q_{i, \exp} - q_{i, \operatorname{cal}} \right|}{\overline{q_{\exp}} \cdot n} \cdot 100\%$$
(3)

where $q_{i, \exp} \pmod{(\text{mg g}^{-1})}$ is experimentally obtained amount of sorbed dye at the experimental point *i*, $q_{i, \text{ cal}} \pmod{(\text{mg g}^{-1})}$ is calculated amount of sorbed dye at the experimental point *i* by some kinetic or isotherm model and *n* is a number of the experimental points.

In order to find out whether there is any adsorption on the Petri dish walls, control experiments were carried out in the absence of sorbent, and it was concluded that sorption is negligible. The sorption experiments were conducted in triplicate. All calculations of the experimental data and statistical analysis were performed using OriginPro 2016 software (OriginLab Corporation, USA).

154 **Results and discussion**

155 Characterization of sorbent

156 SEM analysis

Figure 1 shows SEM images of the electrochemically synthesized material at different magnifications. Figure 1a shows that ECBBN sorbent consists of aggregates below 40 μ m, and it exhibits various shapes and sizes. Some of the aggregates are basically polyhedrons with relatively plane facets, and it is hard to distinguish the particular aggregates. However, there is also a significant part of the surface, which



Fig. 1 SEM images of ECBBN at a magnifications of a ×500, b ×10,000, c ×70,000 and d ×50,000

appears to be monolithic. Aggregates have porous morphology (Fig. 1b), composed of crystals which are smooth in texture and have a variety of forms. Many of them seem to be sintered, forming much bigger structures. A certain part of the crystals has an irregular structure with plane surface structures which thickness varies between 200 and 800 nm. In Fig. 1c, nanometric crystals with diameter 30–50 nm can be observed. Also, pores smaller than 40 nm in diameter can be detected (Fig. 1d).

169 Textural properties

The textural properties of ECBBN sorbent have been studied by the nitrogen adsorp-170 tion measurements. The nitrogen adsorption/desorption isotherms of ECBBN are 171 shown in Fig. 2. According to IUPAC classification, they belong to the isotherm 172 type II, with a type H3 hysteresis loop in the relative pressure range of 0.9–1.0. 173 Such shape of isotherm indicates unrestricted monolayer adsorption on nonporous 174 or macroporous adsorbents. Hysteresis loop of H3 type is characteristic of non-175 rigid aggregates of plate-like particles and materials, whose pore network consists 176 of macropores [37]. The BET specific surface area of ECBBN is 0.95 m² g⁻¹. The 177 BJH analysis shows narrow pores with an average pore diameter of 9.99 nm. The 178 mesopore surface area of ECBBN amounts to 0.69 m² g⁻¹, while the volume of 179 pores is $0.0017 \text{ cm}^3 \text{ g}^{-1}$. 180

181 XRD analysis

The XRD spectrum of the synthesized ECBBN is presented in Fig. 3. It shows diffraction peaks at 11.64°, 12.96°, 20.22°, 23.47°, 27.06°, 34.07°, 41.24° and 52.54° 2θ values, which can be indexed to $[Bi_6O_5(OH)_3](NO_3)_5 \cdot 2H_2O$ according to the



Fig. 2 The N₂ adsorption/desorption isotherm of ECBBN



Fig. 3 XRD pattern of ECBBN

185 XRD database JCPDS-ICDD: PDF-2 00-054-0627. The obtained material is com-186 posed of trigonal $[Bi_6O_5(OH)_3](NO_3)_5 \cdot 2H_2O$ (space group P-3, a=b=15.187 Å, 187 c=15.838 Å, $\alpha=\beta=90^\circ$, $\gamma=120^\circ$). Sharp peaks indicate that the synthesized 188 $[Bi_6O_5(OH)_3](NO_3)_5 \cdot 2H_2O$ displays high crystallinity. No other phases were found. 189 By using the Williamson–Hall method [38], it is estimated that the crystallite size of 190 the material is 11.3 ± 0.2 nm.

191 EDX analysis

EDX analysis (Fig. 4) of electrochemically synthesized material shows the presence of Bi, O and N, which corresponds to typical BBN composition. The weight percentage of elements for ECBBN determined by EDX analysis are given in Table 1, and the results are in good agreement with the theoretical weight percentages for $[Bi_6O_5(OH)_3](NO_3)_5 \cdot 2H_2O$.

197 FTIR analysis

The FTIR spectral analysis is important to identify the characteristic functional 198 groups of material. Figure 5 shows the FTIR spectra of ECBBN sorbent. The broad 199 absorption peak centred at 3421 cm⁻¹ is assigned to the stretching vibrations of 200 -OH groups [39]. The -OH bending vibration mode of lattice water corresponds to 201 the band at 1626 cm⁻¹ [40, 41]. The bands appearing at 718, 811, 1036, 1327, 1354 202 and 1384 cm^{-1} originate from the NO₃⁻ vibrations and fit well to the data from the 203 literature [42–44]. The absence of IR bands at 736, 803 and 1297 cm⁻¹ is character-204 istic for hydrated nitrates [43]. Thus, synthesized ECBBN contains water molecules 205 in its structure. The bands observed at 563 and 442 cm^{-1} are assigned to the Bi–O 206



Fig. 4 EDX spectrum of ECBBN

Element	Experimental weight percentage (%) of elements in ECBBN	Theoretical weight percentage (%) of elements in [Bi ₆ O ₅ (OH) ₃](NO ₃) ₅ ·2H ₂ O
Bi	73.26	72.43
0	20.73	23.11
Ν	6.01	4.04
Н	-	0.41

 Table 1
 Weight percentages of elements in ECBBN by EDX analysis



Fig. 5 FTIR spectrum of ECBBN

bond stretching vibrations [45, 46]. The FTIR spectrum obtained for the ECBBN corresponds to the spectrum of $[Bi_6O_5(OH)_3](NO_3)_5 \cdot 2H_2O$ reported by Christensen et al. [47].

210 The isoelectric point

The isoelectric point (pI) of the synthesized ECBBN sorbent determined by the salt addition method is 2.12, which shows that the sorbent is strongly acidic. The sorbent surface is positively charged at pH < 2.12 and negatively charged at pH > 2.12.

214 The ability of ECBBN to remove RB19

The ability of the sorbent ECBBN to remove RB19 was studied as a function of 215 time, using an initial sorbent dose of 500.0 mg dm⁻³, initial RB19 concentration 216 of 500.0 mg dm⁻³ and at native pH. The results (Fig. 6) show that the sorption 217 process occurs in two phases. In the first, initial phase, rapid uptake of RB19 mol-218 ecules occurs, and during this phase (1 min), more than 95% of the total amount 219 of sorbed dye was removed. The second phase is much slower, and the amount of 220 sorbed dye was less than 5% of the total sorbed amount. From these results, it can 221 be concluded that equilibrium was reached in several minutes, and the maximum 222 amount of sorbed dye at native pH was 838.56 mg g⁻¹. Electrochemically synthe-223 sized sorbent (ECBBN) exhibits much higher sorption capacity for RB19 than other 224 sorbents, especially than inorganic sorbents synthesized by conventional methods, 225 such as precipitation, coprecipitation and hydrothermal methods, reported in previ-226 ous studies (Table 2) [20-27]. Another advantage of the electrochemically synthe-227 sized sorbent is much lower sorption equilibrium time, which makes the sorption 228



Fig.6 Effect of contact time on the removal efficiency of RB19. c_{RB19} 500.0 mg dm⁻³, c_{sorbent} 500.0 mg dm⁻³, temperature 25.0±0.5 °C, pH native

Sorbent	Synthesis method	рН	Sorption capacity (mg g ⁻¹)	Equilibrium time (min)	Reference
Magnetite/graphene oxide	Coprecipitation	3.0	62.50	67	[21]
Nanohydroxyapatite	Precipitation	3.0	90.09	180	[20]
NiO nanoparticles	Precipitation	6.5	98.83	15	[22]
Polypyrrole-coated Fe ₃ O ₄	Coprecipitation	3.0	112.36	10	[26]
MgO nanostructures	Hydrothermal	7.8	250.00	20	[23]
Chitosan hollow fibres	_	3.5	454.50	90	[25]
FeCuNi-280	Coprecipitation	2.0	480.80	120	[27]
Chitosan	-	6.8	822.40	150	[24]
ECBBN	Electrochemical	Native pH	838.56	2	This study
ECBBN	Electrochemical	2.0	1046.24	2	This study

Table 2 Comparison of sorption capacity of different sorbents for the removal of RB19



Fig. 7 Effect of pH on the removal efficiency of RB19; $c_{\rm RB19}$ 700.0 mg dm⁻³, $c_{\rm sorbent}$ 500.0 mg dm⁻³, temperature 25.0±0.5 °C

229 process considerably faster. Also, ECBBN has substantially higher sorption ability

in comparison with BBN reported by Abdullah et al. [31] which is synthesized with

precipitation method and has a sorption capacity of 31 and 24 mg g^{-1} for Methyl

232 Orange and Sunset Yellow, respectively.

233 Effect of pH on the removal efficiency of RB19

The solution pH is another important parameter in sorption controlling because it affects the surface charge of the sorbent and the degree of ionization of the adsorbate

[48]. The effect of pH on the removal efficiency of RB19 was evaluated by changing 236 the pH from 1.5 to 9.0. All the experiments were carried out with extremely high con-237 centration of RB19 (700 mg dm^{-3}) in order to make it easier to see the difference in 238 the removal efficiency of RB19 at different pH values. From the data in Fig. 7, it can 239 be seen that the maximum removal efficiency of RB19 is achieved at pH 1.5 and 2.0. 240 and it decreases with increasing pH. The removal efficiency decreases from 77.73 to 241 46.11%, from pH 2.0 to pH 9.0. At pH 1.5, removal efficiency of ECBBN sorbent is 242 slightly lower than at pH 2.0; therefore, experiments were not conducted at pH values 243 lower than 1.5. Under high acidic conditions (pH 1.5-2.0), the surface of the sorb-244 ent is positively charged, because the pI of the sorbent is 2.12, and thus the electro-245 static attraction between the anionic dve RB19 and the sorbent surface is the strong-246 est at that pH [22]. Therefore, ECBBN has the highest sorption capacity for RB19 at 247 $pH \leq 2.0$, and it decreases with increasing pH (Fig. 8). The maximum sorption capac-248 ity at pH 2.0 is 1046.24 mg g^{-1} . Furthermore, the data in Fig. 8 show that in the 249 whole pH range investigated, i.e. at pH 1.5, 2.0, 3.0, 5.0, 7.0 and 9.0, the sorption 250 capacity is high, being 1034.63, 1046.24, 917.47, 838.56, 714.22 and 645.59 mg g^{-1} . 251 respectively. The minimum sorption capacity is 645.59 mg g^{-1} at pH 9.0, which is 252 still much higher when compared with inorganic sorbents reported in the literature 253 (Table 2). Thus, the high sorption capacity for ECBBN, over the whole investigated 254 pH range, can be considered a beneficial characteristic for the application of the sorb-255 ent in water treatment, enabling it to be used without the necessity for pH adjustment 256 and the addition of any other chemical component to the sorption system. 257

258 Effect of sorbent dose on the removal efficiency of RB19

The effect of variation in the sorbent dose from 250.0 to 1000.0 mg dm⁻³ on the removal of RB19 at a constant concentration of RB19 (700.0 mg dm⁻³) and pH 2



Fig. 8 Sorption capacity of ECBBN at different pH values

was studied. The removal efficiency of RB19 (Fig. 9) at the lowest dose of sorb-261 ent (250.0 mg dm⁻³) is low (36.36%). For higher sorbent doses of 500.0, 750.0 262 and 1000.0 mg dm⁻³, the removal efficiency of RB19 increases up to 74.73, 99.54 263 and 99.65%, respectively. A rapid increase in the efficiency of dye removal with 264 increasing sorbent dose occurs due to an increase in the surface area of the sorbent 265 and availability of more binding sites for RB19 [8, 49, 50]. Taking into considera-266 tion sorption efficiency, sorption amount of dye and the cost of sorbent, a dose of 267 500.0 mg dm^{-3} of the sorbent is took as optimum and used for further experiments. 268

269 Effect of initial dye concentration on removal efficiency of RB19

Pollutant concentration is one of the most important parameters that can affect 270 the adsorption process. The effect of the initial dye concentration on the removal 271 efficiency was investigated by varying the concentration of RB19 from 100.0 to 272 700.0 mg dm⁻³ at constant sorbent dose (500.0 mg dm⁻³) and pH 2. The results are 273 presented in Fig. 10, and they show that the removal efficiency decreases from 99.65 274 to 74.73% with increasing initial concentration of dye from 100.0 to 700.0 mg dm $^{-3}$. 275 The decrease in removal efficiency with increasing dye concentration occurs due to 276 the saturation of the limited available binding sites when using a constant sorbent 277 dose [51]. 278

279 Kinetics study

Sorption kinetics study is very important for a complete understanding of the sorption behaviour. To evaluate the sorption mechanisms and identify the potential rate-controlling steps, reaction and diffusion kinetic models were used to test the



Fig.9 Effect of sorbent dose on the removal efficiency of RB19. c_{RB19} 700.0 mg dm⁻³, temperature 25.0 ± 0.5 °C, pH 2.0



Fig. 10 Effect of initial concentration of dye on the removal efficiency of RB19; c_{sorbent} 500.0 mg dm⁻³, temperature 25.0±0.5 °C, pH 2.0

experimental data. Pseudo-first-order and pseudo-second-order reaction kinetics models nonlinear form of equations are expressed as follows:

285

$$q_t = q_e \left(1 - e^{-k_1 t} \right) \tag{4}$$

286

293

$$q_t = \frac{q_{\rm e}^2 k_2 t}{1 + k_2 q_{\rm e} t} \tag{5}$$

where q_t is amount of dye sorbed at time $t \pmod{g^{-1}}$, $q_e \pmod{g^{-1}}$ is amount of dye sorbed at equilibrium state, $k_1 \pmod{1}$ and $k_2 \pmod{g^{-1} \min^{-1}}$ are pseudo-first and pseudo-second-order reaction rate constants, respectively [52, 53].

The intraparticle diffusion model proposed by Weber and Morris was used for the description of the diffusion mechanism, and it is expressed by the following equation:

$$q_t = k_{\rm id} t^{1/2} + C \tag{6}$$

where k_{id} (mg g⁻¹ min^{-1/2}) is the intraparticle diffusion rate constant, q_t (mg g⁻¹) is the amount of RB19 sorbed at time *t* and *C* is the constant varied directly with the boundary layer thickness [54].

All the parameters, which characterize these models, were determined by nonlinear regression analysis of experimental data for pseudo-first-order and pseudo-second-order models and linear for the intraparticle diffusion model. Regression analysis was done using software OriginPro 2016, and results are presented in Table 3.

The determination coefficients for both reactions kinetic models are higher than 0.999, which indicates that both models can be successfully applied for the sorption process. Similar values of the calculated q_e with experimentally determined $q_{e, exp}$

$c (\text{mg dm}^{-3})$	100	200	300	400	500	600	700
$q_{\rm e, exp} ({\rm mg \ g^{-1}})$	199.32	398.63	597.27	796.58	959.02	1043.00	1046.24
Pseudo-first-order mode	el						
$q_{\rm e} ({\rm mg \ g^{-1}})$	197.92	396.48	593.93	790.82	949.59	1027.01	1028.02
$k_1 ({\rm min}^{-1})$	12.88	12.09	11.35	10.65	9.71	8.53	7.09
r^2	0.9999	0.9998	0.9998	0.9996	0.9995	0.9986	0.9981
RMD (%)	0.30	0.39	0.44	0.57	0.71	1.20	1.63
Pseudo-second-order m	nodel						
$q_{\rm e} ({\rm mg \ g^{-1}})$	200.96	403.95	607.22	811.93	981.47	1074.13	1093.96
$k_2 (g mg^{-1} min^{-1})$	0.36	0.15	0.08	0.05	0.03	0.02	0.01
r^2	0.9999	0.9999	0.9999	0.9998	0.9997	0.9996	0.9993
RMD (%)	0.27	0.28	0.37	0.44	0.53	0.65	0.76
Intraparticle diffusion n	nodel						
$k_{i1} (\mathrm{mg \ g^{-1} \ min^{-1/2}})$	296.40	591.45	882.33	1168.17	1391.82	1472.57	1437.58
$C_1 ({\rm mg \ g^{-1}})$	9.50	18.53	26.88	34.66	39.01	39.79	32.90
r^2	0.9060	0.9115	0.9181	0.9140	0.9259	0.9229	0.9393
$k_{i2} (\mathrm{mg \ g^{-1} \ min^{-1/2}})$	1.06	1.80	2.70	4.61	9.12	13.50	22.62
$C_2 ({\rm mg \ g^{-1}})$	197.20	395.43	592.50	788.26	942.45	1018.06	1005.96
r^2	0.9207	0.9297	0.9297	0.9388	0.9223	0.9301	0.9381

Table 3 Kinetic parameters for RB19 sorption onto ECBBN sorbent

also confirms the applicability of these kinetic models. The obtained q_e values for 304 the pseudo-first-order model are in slightly better agreement with experimental data 305 in comparison with results obtained for the pseudo-first-order model. However, for 306 all tested concentrations lower *RMD* values for the pseudo-second-order than for the 307 pseudo-first-order model were obtained, which indicates that pseudo-second-order 308 model fitted the experimental data slightly better. Thus, obtained results suggest that 309 the rate-controlling step in the sorption process might be surface reaction through 310 electron sharing/exchange between RB19 and active sites of sorbent, ion exchange 311 reaction, complexation, coordination and/or chelation [55, 56]. A small specific 312 surface area of the sorbent also indicates that the above-mentioned processes have 313 a greater impact on the sorption process than the physical sorption. The values of 314 pseudo-second-order reaction rate constants, k_2 , decrease with increasing initial 315 RB19 concentration, because almost all available binding sites at the sorbent surface 316 317 are free at lower initial dye concentrations, resulting in high reaction rate constant values. With higher dye concentrations, saturation of binding sites occurs, which 318 leads to a decrease of the k_2 values. 319

The results of linear regression analysis for the intraparticle diffusion model are given in Table 3. The two linear ranges in the shape of the intraparticle diffusion plot of q_t versus $t^{1/2}$ indicate that two steps occur in the adsorption process. The first, sharp linear range can be ascribed to the external surface adsorption or instantaneous adsorption stage of RB19 on the sorbent. When the adsorption onto the external surface reaches saturation, the second linear range begins, which represents the gradual adsorption stage, where the intraparticle diffusion is rate-controlled [57]. The first step is very fast, finished in about 1 min, while the second step is very slow, and after the first minute, the change of amount of sorbed dye is negligible. The intraparticle diffusion rate constant k_{i2} is much lower than k_{i1} , which confirms that the rate-limiting step is intraparticle diffusion through the boundary layer.

The results which show that both reaction models have very good agreement with experimental data and that the intraparticle model shows that the sorption process ends quickly (very small slope of the second linear part which starts after 1 min) prove enormous rate of sorption process with mixed control by surface reactions and diffusion.

336 Adsorption isotherms

The isotherm models were used for investigation of adsorption equilibrium 337 between the ECBBN sorbent and textile dye RB19. Adsorption isotherms meas-338 urements were carried out by varying the RB19 concentration between 100.0 and 339 700.0 mg dm⁻³ at pH 2.0. Several adsorption isotherms, such as Langmuir [58], Fre-340 undlich [59], Redlich-Peterson [60] and Brouers-Sotolongo [61, 62], were applied 341 to simulate the experimental data. Langmuir model assumes monolayer adsorption 342 at specific homogeneous surfaces on uniformly energetic adsorption sites, with no 343 lateral interaction between adsorbed molecules. Freundlich model was applied to 344 multilayer adsorption at a heterogeneous surface with non-uniform distribution of 345 adsorption heat and affinities over the heterogeneous surface. The Redlich-Peterson 346 isotherm is a combined form of Langmuir and Freundlich equations and assumes 347 that adsorption does not follow ideal monolayer adsorption. Brouers-Sotolongo iso-348 therm model predicts adsorption at the heterogeneous surface. These adsorption iso-349 therms can be expressed in a nonlinear form by the following equations: 350 351

$$q_{\rm e} = \frac{q_{\rm m} K_{\rm L} c_{\rm e}}{1 + K_{\rm L} c_{\rm e}} \tag{7}$$

352

$$q_{\rm e} = K_{\rm F} c_{\rm e}^{\frac{1}{n}} \tag{8}$$

353

$$q_{\rm e} = \frac{K_{\rm RP}c_{\rm e}}{1 + \alpha_{\rm RP}c_{\rm e}^{\beta}} \tag{9}$$

$$q_{\rm e} = q_{\rm m} \left(1 - \exp\left(-K_{\rm W} c_{\rm e}^{\alpha}\right) \right) \tag{10}$$

where $q_e \text{ (mg g}^{-1}\text{)}$ is the amount of RB19 sorbed by the sorbent at equilibrium time; $c_e \text{ (mg dm}^{-3}\text{)}$ is the concentration of RB19 at equilibrium time in solution; q_m (mg g⁻¹) is the maximum sorption capacity of sorbent; $K_L \text{ (dm}^3 \text{ mg}^{-1}\text{)}$ is Langmuir constant related to the energy of sorption, $K_F \text{ ((mg g}^{-1}\text{)} \text{ (dm}^3 \text{ mg}^{-1}\text{)}^{1/n})$ is Freundlich equilibrium constant, *n* is Freundlich exponent related to the intensity of sorption, $K_{\text{RP}} \text{ (dm}^3 \text{ g}^{-1}\text{)}$ is the Redlich–Peterson isotherm constant, α_{RP} is also a constant having unit of dm³ mg⁻¹, β is an exponent varied between 0 and 1, $K_W \text{ (dm}^3 \text{ mg}^{-1}\text{)}$ is Brouers–Sotolongo isotherm constant and the dimensionless exponent α is a measure of the width of the sorption energy distribution and therefore of the energy heterogeneity of the surface.

These isotherms were characterized by parameters, which express affinity and surface properties of sorbents. All parameters of these isotherms models were determined by nonlinear regression analysis using OriginPro 2016, and the results are given in Table 4.

Applicability of these models was determined by determination coefficients and 369 relative mean deviations. The Langmuir, Redlich-Peterson and Brouers-Sotolongo 370 sorption isotherms have very high r^2 values (higher than 0.98), while the Freun-371 dlich model has significantly lower determination coefficient (0.72) than these three 372 models. In addition, *RMD* for the Freundlich model (16.57%) is the highest, which 373 confirms that the sorption process does not follow the Freundlich isotherm. The 374 other three models have much lower values of RMD, 3.14%, 3.19% and 3.85% for 375 Langmuir, Redlich–Peterson and Brouers–Sotolongo, respectively. The obtained q_m 376 for Langmuir model (1049.19 mg g^{-1}) is in slightly better agreement with experi-377 mental data (1046.24 mg g⁻¹) in comparison with q_m for Brouers–Sotolongo model 378 (1014.86 mg g⁻¹). Based on r^2 , *RMD* and results for maximum sorption capac-379 ity, it can be concluded that among of all above-mentioned models Langmuir, 380 Redlich-Peterson and Brouers-Sotolongo models can be used to describe sorption 381 of RB19 on ECBBN sorbent, and for the nuance, Langmuir model has better match-382 ing with experimental results than the other models. The Redlich-Peterson exponent 383 β is close to 1, and for that value these isotherm model is effectively reduced to the 384 Langmuir model, which means that Langmuir will be preferable isotherm in com-385 parison with Freundlich. Brouers–Sotolongo exponent α , which is in relation with 386 the heterogeneity of the surface, is also close to 1 and indicates that adsorption sites 387 of ECBBN sorbent are homogenous. Based on the applied isotherm models, it can 388 be inferred that the sorption has homogenous character, which confirms good agree-389 ment with the Langmuir type of isotherm. 390

 $R_{\rm L}$ is a dimensionless constant (commonly known as separation factor) derived from the Langmuir isotherm, which can be expressed as follows [63]:

Table 4Isotherm parametersfor RB19 sorption onto ECBBN	Adsorption isotherm	Parameter	Values	r^2	RMD (%)
sorbent	Langmuir	K _L	0.91	0.9895	3.14
		$q_{\rm m}$	1049.19		
	Freundlich	$K_{\rm F}$	515.14	0.7596	16.57
		п	6.37		
	Redlich-Peterson	K _{RP}	929.68	0.9872	3.19
		α_{RP}	0.86		
		β	1.01		
	Brouers-Sotolongo	$K_{\rm W}$	0.65	0.9851	3.85
		$q_{\rm m}$	1014.86		
		α	0.93		

$$R_{\rm L} = \frac{1}{1 + K_{\rm L} c_0} \tag{11}$$

It describes the adsorption nature, which can be defined as unfavourable $(R_L > 1)$, linear $(R_L = 1)$, favourable $(0 < R_L < 1)$ or irreversible $(R_L = 0)$. The R_L values were found to be from 0.0108 to 0.0016 as the initial concentration of dye increases from 100 to 700 mg dm⁻³. This means that the reaction is more favourable for high RB19 concentrations. The value of Freundlich exponent (1/n < 1) confirms that adsorption is favourable.

400 The mechanism of sorption of RB19 onto ECBBN sorbent

According to all the results described in the manuscript, it can be concluded that 401 the mechanism of RB19 sorption on ECBBN sorbent is complex, and the possible 402 mechanism can be presented as follows. From the results of the influence of pH, 403 it can be seen that the sorption capacity is the highest at pH 2 and it continually 404 decreases with increasing pH to 9. However, at pH 9, the sorption capacity is still 405 very high. Thus, it is obvious that electrostatic interactions, which mainly occur at 406 low pH values, are not the only mechanism of the sorption process: the complexa-407 tion also affects the sorption process. Since sulphonic acids are very strong acids 408 (their pK_a values are low), sulphonic groups of the RB19 dye will be dissociated 409 (-SO₃⁻) in the entire investigated range of pH. So, chemical interaction of sulphonic 410 group of RB19 with polycation $[Bi_6O_5(OH)_3]^{5+}$ of ECBBN occurs in the whole 411 range of pH. In contrast, the contribution of physical sorption is small due to the 412 small specific surface area of ECBBN, and therefore, mechanism of the sorption 413 process is the most likely combination of electrostatic and chemical interactions 414 between RB19 and ECBBN sorbent. 415

416 Treatment of a model solution of polluted Nišava River water

In order to investigate the applicability of ECBBN in the purification of real pol-417 luted water, treatment of a model solution of river water contaminated with RB19 418 was done. The river water samples were collected from Nišava River and were used 419 without further treatment, except the filtration through 0.45 µm regenerated cellu-420 lose membrane filter. The river water was used as the matrix of the solutions used 421 in the experiments. A model solution of polluted river water was made by adding 422 500.0 mg dm³ of RB19 to the matrix. According to the previous results, experiments 423 were done at optimal conditions by using a sorbent dose of 500.0 mg dm³ and at pH 424 2.0. Results (Fig. 11) show that the removal efficiency of RB19 from model solution 425 of contaminated river water is also high, but the sorption capacity, as expected, is 426 slightly lower than in model solution made with deionized water. Sorption capacity 427 in the model solution of polluted river water was 838.25 mg dm³, which is 19.88% 428 lower in comparison with the deionized water model solution. This may be attrib-429 uted to the presence of organic matter in the river water, which can be also sorbed 430 at the active sites of ECBBN sorbent. The high sorption capacity of ECBBN for the 431



Fig. 11 Effect of contact time on the removal efficiency of RB19 in the model solution of polluted river water. c_{RB19} 500.0 mg dm⁻³, c_{sorbent} 500.0 mg dm⁻³, temperature 25.0±0.5 °C, pH 2.0

removal of RB19 from the river water indicates that this material can be suitable sorbent for the textile dyes removal from real polluted water.

434 Conclusions

Pure basic bismuth nitrate [Bi₆O₅(OH)₃](NO₃)₅]·2H₂O was, for the first time, suc-435 cessfully synthesized by electrochemical deposition, followed by thermal treatment 436 at 200 °C. The chemical structure of ECBBN was ascertained by XRD, FTIR and 437 EDX analyses. The material is composed of small crystals forming high aggre-438 gates; the crystallite size is 11.3 ± 0.2 nm. Sorption of RB19 by electrochemically 439 synthesized sorbent (ECBBN) is very fast (above 95% of the total sorption at equi-440 librium was reached in 1 min). Sorption kinetics shows that both surface reaction 441 and diffusion were rate-limiting steps. Based on the determination coefficients and 442 relative mean deviations it can be deduced that the experimental data were the best 443 fitted with Langmuir isotherm. The maximum sorption capacity (1049.19 mg g^{-1}) 444 was achieved at pH 2.0. Very high sorption capacity and fast equilibration are very 445 important characteristics for the potential practical use of ECBBN, as well as high 446 sorption capacity in model solutions of contaminated river water. The removal effi-447 ciency of RB19 increases with increasing sorbent dose and decreasing dye concen-448 tration. Low cost, eco-friendly starting materials, simple and non-time consuming 449 synthesis method, high purity and repeatability of the synthesized material structure, 450 as well as very high sorption capacity, better sorption performance and lower sorp-451 tion equilibrium time than similar materials, make ECBBN sorbent a very attractive 452 system for the removal of textile dyes from polluted water. 453

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