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Original Research Paper

Tensile strength of cohesive powders $\stackrel{\star}{\sim}$

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ABSTRACT

Measurement and prediction of cohesive powder behaviour related to flowability, flooding or arching in silos is found to be very challenging. Previous round robin attempts with ring shear testers did not furnish reliable data and have shown considerable degrees of scatter and uncertainty in key measurements. Thus studies to build a reliable experimental database using reference materials, are needed in order to evaluate the repeatability and effectiveness of shear testers and the adopted methodologies. In this paper, first we study the effect of particle size on the yield locus for different grades of limestone (calcium carbonate). We use the nonlinear Warren Spring equation to obtain the values of cohesion C, tensile strength *T*, and the shear index *n*. We recover linear (n = 1) yield loci for $d_{50} > 70 \,\mu\text{m}$ with respectively small *C*. For smaller fractions ($d_{50} = 2.2 \,\mu\text{m}$), the powder is strongly cohesive with considerable non-linearity (1 < n < 2). Then we compare the values of the parameters *C*, *T* and *n* obtained from two different shear testers (Schulze and Brookfield PFT), thereby demonstrating the validity of the Warren Spring equation. The differences encountered are fortunately not leading to a great deviation in terms of cohesion C and tensile strength, T although further experiments with a variety of cohesive powders are needed to confirm or rebut this point. Finally, we compare the values of the tensile strength obtained by a tranverse experimental method using the Ajax tensile tester and found a very good agreement. © 2019 The Society of Powder Technology Japan. Published by Elsevier B.V. and The Society of Powder

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49 1. Introduction

Granular materials underpin the performance of a vast array of everyday products. They are omnipresent in our daily life and widely used in many industries such as food, pharmaceuticals, paints, agriculture, plastics, mining, 3D printing, batteries, cosmetics or personal care products. During storage, flow or transportation in powder processing industry, the material faces various stress conditions and deformation, due to compression or shear.

Quality control in manufacturing (production plant) as well as
manipulating the form and functionality of these industrially vital
materials (R&D lab) is essential for commercial success and relies
on a sound understanding of their properties. Linking particle
properties to powder performance in the process plant is essential.
A lack of this can cause serious difficulties in aspects associated

with flow, storage or handling, leading to lower productivity and dramatically affecting the performance of solids processing units.

Modern processing and formulation requirements have also led to a multi-scale approach to understand the failure of powders by means of mapping the necessary information from the particle level or primary particles to particle clusters (mesoscale) and finally towards the bulk behaviour. To characterize a small particulate sample by e.g. element tests or particle analysis and subsequently predict the bulk behaviour on the unit operation or process scale is of immense value.

Fascinating granular phenomena are: *yielding*, when the shear loads become extremely large the material fails in shear; *jamming*, when a dense stream of particles flows through an orifice, and they clog or jam, i.e. stop flowing, [1–4]; *dilatancy*, when they experience a volume change if subjected to shear deformations [5–7]; *shear* – *band* – *localization* when dilatant granular materials are sheared continuously under uniform stresses and strains [8,9]; *history* – *dependence* including direct time-dependent consolidation effects and load history-dependent cohesion [10]; or *anisotropy* when sheared systems show direction-dependent distributions of both the contact network and the contact forces

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σ_0	isostatic tensile strength (Pa)	σ	pre-consolidation normal stress (Pa)
F_H	adhesion force (N)	τ	shear stress (Pa)
d_s	Sauter mean diameter (m)	$\sigma_{ m n}$	normal stress (Pa)
ϵ_{o}	void fraction of the bed of particles ([–])	$\sigma_{ m pre}$	pre-shear normal stress (Pa)
$\rho_{\rm p}$	particle density (kg/m ³)	Ċ	cohesion or cohesive strength (Pa)
ρ_0	initial bulk density (kg/m ³)	Т	tensile strength (Pa)
$\rho_{\rm b}$	bulk density (kg/m^3)	п	shear index
w	moisture content (%)	μ	friction coefficient
d_{10}	particle diameter where 10% of distribution is below	ϕ_i	internal friction angle
	this value (µm)	σ_{c}	cohesive characteristic consolidation (Pa)
d_{50}	particle median size where 50% of distribution is below	n _C	cohesion index
	this value (µm)	σ_T	tensile characteristic Consolidation (Pa)
d_{90}	particle diameter where 90% of distribution is below	n_T	tensile strength index
	this value (μm)		
Ψ	roundness ([–])		

[11–13] have attracted significant scientific interest over the past decades [14–22].

The mechanical behavior of cohesive powders depends on prestressing history [23]. Various laboratory testers to study the shear stress necessary for the failure of consolidated powder beds can be found in the literature to evaluate the bulk behaviour of granular materials [24,25]. These testers are also a valuable tool to understand the influence of particle properties, e.g. density, sizedistribution and shape, on the macroscopic bulk response. Moreover, such shear testers are commonly used for the industrial design of silos and hoppers. Although this is in many cases still empirical, the design methods are based on fundamental engineering principles and follow norms and established sample preparation procedures [26–29].

Element tests are (ideally homogeneous) macroscopic tests in which the force (stress) and/or displacement (strain) path are controlled. The most widely performed element test in both industry and academia is the shear test, where a granular sample is sheared until failure is reached and the material starts to flow.

Shear testers are usually classified into two groups: direct and indirect methods [25,27]. In direct shear testers, the shear zone is pre-defined by the device design, and the shear failure is forced in a specific physical location. On the contrary, in the indirect devices, the shear zone develops according to the applied state of stress. The most common indirect devices are the uni-axial compression tester [10,30,31] and the bi-axial shear box [32,33].

Direct devices can be further categorised into two sub-groups: translational and rotational. Typical translational shear testers include the direct shear tester [34–36] and the Jenike shear tester [37], while torsional or rotational shear testers include the FT4 powder rheometer [38], the Schulze ring shear tester [39] and the Brookfield powder flow tester [40].

A similar classification can be established attending to the movement of the shear cell elements and distinguishing between four main categories: the rotational cells, parallel plate cells and upper or lower movable shear cells. Detailed reviews of testers have been presented by several authors [25,41,42], and more (non-commercial) shear testers with higher complexity can be found in literature [43–45].

All shear testers have in common that they measure the shear stress necessary to make a sample yield under a given finite compressive normal stress.

On the other hand, the tensile strength can be defined as the tensile normal stress required to fracture a specimen of compacted powder when no shear forces are applied. It represents the tendency of a sample of compacted powder to resist separation from a particle bed under the influence of a tensile stress and it is the external macroscopic manifestation of attractive forces between the constituent particles.

The magnitude of these forces depends on the closeness of particles in the packing, like the yield stress the tensile strength is related to the present state due to stress history of the particulate solid.

For cohesive powders, the tensile strength increases with increasing packing density due to the increase in the number and intensity of interparticle forces (adhesion, cohesion, van der Waals, interfacial, bridging and interlocking) [46–48].

The direction and module of compacting stresses must be defined in relation to the alignment of the plane in which failure takes place.

Co - axial tensile strength relates to failure stress in the direction opposite to the compacting stress. *Transverse* tensile strength relates to failure stress at 90° to the orientation of the compacting stress. *Ultimate* tensile strength is a measure of the failure stress of a triaxially compacted sample. (A theoretical, rather than a practical test). *Isostatic* tensile strength in the absence of deformation (unconsolidated particle contacts) represents the characteristic cohesive nature of a powder.

The isostatic tensile strength σ_o can be related to the adhesion force, F_H using the pioneer approach of Rumpf (1962) [49]:

$$\sigma_o = \frac{(1 - \epsilon_o)F_H}{(\epsilon_o d_e^2)} \tag{1}$$

where d_s represents the mean Sauter diameter of the particles and ϵ_o is the void fraction (porosity) of the bed of particles with $(1 - \epsilon_o)/\epsilon_o$ being the inverse void ratio.¹ Capece (2015) [50] investigated the fundamental relationship between interparticle cohesion and powder flowability making use of the Bond number as a dimensionless quantification of the cohesion between particles. A model to study the effect of physical properties on cohesion and unconfined yield strength of pharmaceutical powders considering particle size and compressibility index was presented by Garg (2018) [51].

Quality and reproducibility of results are key aspects for proper material characterization. Although shear testing technologies have been developed and studied extensively, significant scatter in measurements is still common when testing powder flowability using different devices in different labs/environments [38–40,52–

¹ The inverse void ratio increases with decreasing the porosity and thus that increases the isostatic tensile strength.

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P. García-Triñanes et al. / Advanced Powder Technology xxx (xxxx) xxx

54]. Previous studies have been focusing on this problem by performing round-robin experimental studies on the Jenike tester
[55], the Schulze ring shear tester [52] and the Brookfield powder
flow tester [40] as well as comparing different devices [56,57].

175 The earliest round-robin study [55] resulted in a certified material (CRM-116 limestone powder) and a common standard experi-176 mental testing procedure for determining the yield locus. Schulze 177 (2011) [52] has collected 60 yield loci obtained using the small 178 Schulze shear tester RST-XS (21 labs) and 19 yield loci using the 179 large Schulze shear tester RST-01 (10 labs) on one limestone pow-180 der (CRM-116). Results have been compared among them as well 181 182 as with the results from a reference Jenike tester. While results from RST-01 and RST-XS are in good agreement, a considerable 183 deviation (up to 20 %) was observed when comparing results from 184 185 the Schulze ring shear tester to the lenike shear tester.

Similar results are found by other researchers [40,56,58], where
 yield loci from the Brookfield powder flow tester, the Schulze ring
 shear tester, the FT4 powder rheometer and the Jenike shear tester
 are compared. The Brookfield powder flow tester and the FT4 pow der rheometer show systematically lower shear resistance in com parison to the other two shear testers.

Other studies have compared different industrially relevant powders but only in a single device [59,60]. Moreover, these comparative studies have been limited to relatively low stresses. A deeper understanding of the reasons for the differences in measured flow behaviour of powders in several shear devices over a wide stress range is still missing and remains a huge challenge for the particle technology community.

This article aims to shed light on the measurement and the 199 200 importance of the tensile strength of cohesive powders and it is structured as follows: In Section 2, we provide information on 201 the limestone samples/materials, before we describe in Section 3, 202 the experimental devices and the test procedures. Section 4 is 203 devoted to the description of the Warren Spring model for tensile 204 205 and cohesive strength and in Section 5 we discuss the experimen-206 tal results with focus on the measurement of powder failure prop-207 erties, while conclusions and outlook are presented in Section 6.

208 **2. Material description and characterization**

209 Limestone powder is widely used in many fields ranging from construction, toothpaste to automotive industries. Following previ-210 ous work [24], we have chosen the same grades of pre-sieved lime-211 stone powders under the commercial name Eskal (KSL 212 Staubtechnik GmbH, Germany). The limestone powder has been 213 used as a reference material for standard testing [24,61,62] in pow-214 215 der technology due to the favourable physical properties: high 216 roundness, low porosity and an almost negligible sensitivity 217 towards humidity and temperature changes.

The raw Eskal granules (calcium carbonate of approx. 4 mm) are all ground passing a pin mill to reduce the particle size. Very fine particles are eliminated by a cyclone while the remaining particles pass an air classifier and in the next step are sieved to different grades of particle size distributions. The details of their physical properties are summarized in Table 1.

As previous studies indicate a non-linear yield locus is correlated to the cohesiveness of the powder, the focus here is on the most cohesive grade of Eskal. While in [24], the focus was more on their low stress response, the current study reaches out to the behaviour of fine/cohesive Eskal300 ($d_{50} = 2.22 \,\mu$ m) and coarse/ free-flowing Eskal150 ($d_{50} = 138 \,\mu$ m) at lower confining stress.

2.1. Measurements

The particle size data was obtained using laser diffraction in the dry method by means of a RODOS dispersion system with feeder VIBR/L (Sympatec GmbH). The measurements were performed under repeatability conditions (see Table 3).

Surface area measured by BET Automatic Specific Surface Analyzer Macsorb by Mountech Co.,Ltd. The initial bulk density values are provided by the manufacturer. Particle density was measured using a Helium pycnometer (UltraPyc 1200e). Note that all powders here are presented with their original commercial name (e.g. Eskal150, Eskal300), while their median particle size d_{50} will be used for future discussions for the sake of clarity.

The aspect ratio, shape and morphology of all Eskal samples are 242 analyzed by Scanning Electron Microscope (SEM) imaging (Helios 243 G4 CX, FEI Deutschland GmbH, Germany). Figs. 1 and 2 show the 244 SEM images of Eskal150 and Eskal300, respectively. In Fig. 1, we 245 see that all the Eskal150 primary particles have similar shapes 246 (left) and rough surfaces (right), and every particle can be clearly 247 distinguished from the others. But for Eskal300 in Fig. 2 (left), we 248 observe some clusters of primary particles, and the size of clusters 249 are typically around $10-20 \,\mu\text{m}$, which is about 5-10 times the 250 median particle size of Eskal300. When we zoom into smaller scale 251 focusing on only one cluster as shown in Fig. 2 (right), we see even 252 smaller fines ($<1 \mu m$) sticking on the surface of primary particles, 253 and the shape of Eskal300 particles are slightly more irregular than 254 255 the ones from Eskal150. The other Eskal samples are very similar in 256 their shapes irrespective of median particle size, with roundness 257 increasing with size, and specific surface area decreasing.

3. Experimental setup

3.1. Schulze ring shear tester - RST-01 and RST-XS

The Schulze ring shear tester (1994) is one of the most widely 260 used testers in powder flowability characterization. The Schulze 261 ring shear tester (RST-01) is connected to a computer with control-262 ling software that allows the user to obtain semi-automatically the 263 vield loci and wall vield loci. A smaller version of the ring shear tes-264 ter with exactly the same working principle is the so-called RST-265 XS, developed for both smaller specimen volumes (3.5 ml to 70 266 ml, rather than 204 ml for the RST-01) and smaller confining/pre-267

Table 1

Material parameters of the experimental samples with focus on the two samples in bold font.

Property	Eskal	Unit	300	500	15	30	80	150
Particle Size	d_{10}	μm	0.78	1.64	12	21	39	97
	d ₅₀	μm	2.22	4.42	19	30	71	138
	d_{90}	μm	4.15	8.25	28	43	106	194
Span	$(d_{90}-d_{10})/d_{50}$	[-]	1.52	1.50	0.84	0.73	0.94	0.70
Particle density	$ ho_{ m p}$	kg/m ³	2853	2868	2799	2758	2753	2761
Moisture content	Ŵ	%	0.9	0.9	0.9	0.9	0.9	0.9
Roundness (sphericity)	Ψ	[-]	0.75	0.55	0.48	0.66	0.84	0.88
Initial bulk density	$ ho_0$	kg/m ³	540	730	1110	1230	1330	1370
Specific surface area	SSA	m²/g	2.324	1.096	0.538	0.390	0.353	0.310

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P. García-Triñanes et al./Advanced Powder Technology xxx (xxxx) xxx

Table 2

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Specifications comparison of the Schulze ring shear tester RST-01 and RST-XS.

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Table 3

Specifications comparison of the Brookfield powder flow tester with normal and small cells.

	Property	Normal cell	Small cell
_	Cell volume (cm ³)	230	38
	Vane lid (cm ³)	33	5
	Cell geometry	Ring	Ring
	Wall material	Aluminium	Aluminium
	Diameter (D) (cm)	15.24	12.70
	Shear displacement limit	Unlimited	Unlimited
	(cm)		
	Test control	Computer	Computer
	Sample weighing	Offline	Offline
	Compression device	Top ring	Top ring
	Driving velocity (cm/s)	0.01 to 0.5	0.01 to 0.5
	Load for Vertical	7	7
	Axis Compression (kg)		
	Sample conditioning	Pluviation	Pluviation
	before pre-shear	(manual)	(manual)
	Yield locus test duration	18 min	18 min
	Stress measure direction	Rotational	Rotational
	Trough rotational	1 revolution/hour	1 revolution/hour
		(RPH)	(RPH)
	speed	up to 5 RPH	up to 5 RPH
_			

consolidation stresses. For both versions of the shear tester, the
bulk solid specimen are filled inside an annular bottom ring. An
annular-shaped lid is then placed on top of the bulk solid specimen
and is attached to a cross-beam (Fig. 3).

A normal force, F_N , is exerted on the cross-beam perpendicular to the rotational plane and transmits through the lid onto the specimen. In order to allow small confining stress, the counterbalance force, F_A , is introduced. It acts in the centre of the cross-beam, 275 directed vertically upwards, counteracting the gravitational force 276 of the lid, the hanger and the cross-beam. By rotating the bottom 277 ring with an angular velocity ω and keeping the cross-beam sta-278 tionary with two tie-rods, the sample is sheared effectively. Each 279 of the tie-rods is fixed at a load beam, so that the forces, F_1 and 280 F_2 , can be measured. The bottom of the shear cell and the lower 281 side of the lid are rough in order to prevent sliding of the bulk solid 282 on these two surfaces. Through this shearing the bulk solid is 283 deformed, and a shear stress τ develops, proportional to the forces 284 acting on the tie-rods $(F_1 + F_2)$. In addition to the shear forces 285 (F_1, F_2) , the ring shear tester also measures the vertical position 286 of the lid. If a bulk solid is compressible, its bulk density, ρ_b , will 287 increase with the normal load applied. Thus, also the volume of 288 the bulk solid specimen can be deduced from the known vertical 289 position of the lid. All the tests performed here follow the ASTM 290 standard [64]. 291

3.2. Brookfield powder flow tester – PFT

The Brookfield tester (Fig. 4) has been designed to minimise the operator involvement in the shear testing process [40]. The apparatus is computer controlled via a USB link to reproduce the sequences of normal stresses and the shear movement necessary to define the yield loci using the Powder Flow Pro software. It is possible to obtain in one single measurement: Unconfined failure strength, major principal consolidating stress, time consolidation, angle of internal friction, cohesion and bulk density.

The Brookfield Powder Flow Tester allows in a separate test to 301 investigate the evolution of wall friction with increasing shear dis-302 tances over the wall. This shear tester operates by applying a nor-303 mal compression on to the powder sample sandwiched in the 304 annular space between the trough and the vane lid. The standard 305 vane lid has 18 small compartments which trap the powder parti-306 cles and cause them to shear against the powder particles in the 307 trough. When the standard trough is filled to level, it holds 230 308 cm³ of sample material with an external annulus diameter of 309 15.24 cm. When used with the standard vane lid, the additional 310 volume required for the lid increases to 263 cm³ of material. The 311 axial speed of the lid approach movement and rotational speed 312 can be set by the user. The underside of the trough has recessed 313 vanes or a perforated screen to grip the powder sample. A small 314 volume shear cell kit version of this tester with exactly the same 315 working principle was developed for smaller specimen volumes. 316 The small trough requires 38 cm³ of sample when filled to level 317 with an external annulus diameter of 2.7 cm. When used with 318 the small vane lid, the total sample size increases to 43 cm³. Other 319 important parts of the PFT are the inner and outer catch trays and 320 the shaping blade to level the powder sample. 321



Fig. 1. SEM topography images of Eskal150 (d₅₀ = 138 µm) in two different scales: 400 µm (left) and 100 µm (right), as indicated by the scale bar.

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P. García-Triñanes et al./Advanced Powder Technology xxx (xxxx) xxx



Fig. 2. SEM topography images of Eskal300 (d_{50} = 2.2 μ m) in two different scales: 30 μ m (left) and 4 μ m (right), as indicated by the scale bar.



Fig. 3. (a) The Schulze ring shear tester RST-01 and (b) the working principle of the Ring shear cell set-up. The difference between RST-XS and RST-XS is the shear cell size. For technical details see Table 2. (b), reprinted with permission from author [63]. Copyright: Dietmar Schulze.



Fig. 4. Brookfield powder flow tester highlighting the two different trough sizes. Copyright: Brookfield AMETEK. Developed in association with The Wolfson Centre for Bulk Solids Handling, University of Greenwich, UK.

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P. García-Triñanes et al./Advanced Powder Technology xxx (xxxx) xxx

The powder sample is initially consolidated by continuously shearing it under the chosen compacting load and it is then sheared to failure under reduced normal loads. This process starts with the lowest load and is repeated with increasing normal loads until a complete locus can be plotted. Note that the Brookfield PFT operates over a lower normal stress range (0.3 to 5 kPa) than the RST although 13 kPa can be reached when using the small cell.

329 3.3. Tensile strength measurement

In this study the tensile strength, T, was directly obtained using 330 a transverse tensile tester (Ajax Equipment Ltd) that uses uniaxial 331 compaction followed by failure due to tension applied at 90° to the 332 compacting stress. The tensile strength is equal to the external ten-333 sile force per area on the Eskal sample at failure when no shear 334 force is applied. This tester is a refinement of the device developed 335 336 by Warren Spring Laboratories. The device allows for direct mea-337 surement of the force required to fracture a sample of Eskal con-338 tained in a split cell (see Fig. 5). One half of the split cylindrical 339 cell is attached to the main body of the machine whilst the match-340 ing section is mounted on a leaf spring. Twin opposing action ten-341 sion springs are each attached to screw adjusting blocks so that the moving cell can be positioned in a contact-null balance position 342 against the fixed half. An amount of Eskal to just reach the required 343 density for the test is filled in the loading cylinder and the top sur-344 345 face is carefully levelled. A plunger equivalent to a consolidating 346 stress of 3 kPa is put onto the cylinder until the shoulder sits on 347 top of the rim of the cell loading cylinder. Caution was taken not to tighten or rotate the plunger to avoid any degree of shear stress 348 on the sample, which would cause anisotropy and too complex 349 stresses. The plunger is then withdrawn and the loading cylinder 350 removed. The out balance stress applied to the cell is then mea-351 sured on the loading screw. The tensile strength is given by the 352 extension and the value at tensile failure in conjunction with a cal-353 ibration graph. A minimum of six tests were undertaken to ensure 354 reliable results with good reproducibility. 355

4. Warren-spring model

The shape of the yield locus, $\tau(\sigma_n)$, the shear stress needed to cause failure at the applied normal stress, σ_n , can be approximated by the Warren Spring equation [46,47]: 359

$$\tau(\sigma_n) = C \left(\frac{\sigma_n}{T} + 1\right)^{\frac{1}{n}}$$
(2) 362

which incorporates the tensile strength, *T*, the cohesion, *C*, and the exponent, *n*, named curvature or shear index, that takes values between 1 and 2.

The model agrees with the Coulomb Yield Criterion, if and only if, shear index equals 1 since then the friction coefficient μ of the powder equals C/T.

$$\tau = \mathbf{C} + \mu \sigma_n \tag{3} \quad \mathbf{371}$$

where $\mu = \tan \phi_i$ is related to the internal friction angle.



Fig. 5. (a) Ajax Equipment full volume cell illustrated. (b) Eskal300 sample springing apart.

P. García-Triñanes et al. / Advanced Powder Technology xxx (xxxx) xxx



Fig. 6. Yield locus of different size limestone powders using the RST-01: shear stress τ , plotted against normal stress, σ_n . The pre-shear normal stress σ_{pre} is set to 5 kPa but not shown here. Different symbols represent limestone samples with different median particle size as explained in the legend and each point represents three measurements.

373 Previous authors [46,65] claimed that the parameter *n* charac-374 terizes the flowability of the powder sample but to date the 375 micro-mechanical origin and the physical meaning of this param-376 eter could not be explained. The extrapolation of a curved line 377 through limited data with a high variation or uncertainty has gen-378 erated controversy over the years and a number of researchers have proposed different empirical equations to describe the shapes 379 380 of yield loci [66–68]. Here, we do not refer to the other models for the sake for brevity because Eq. (2) fits our data pretty well. 381

382 5. Results and discussion

383 In this section, we use different size limestone powders and we compare the measurement from different shear devices to give a 384 general overview on the repeatability and reproducibility of the 385 test results. In order to compare the yield loci from different tes-386 ters, two limestone powders were chosen as reference powders 387 for device comparison as described in Table 1: cohesive Eskal300 388 389 $(2.22 \ \mu m)$ and free flowing Eskal150 (138 μm). The shear measure-390 ments with the Schulze ring shear tester and the Brookfield pow-391 der flow tester were conducted independently by the authors in 392 two different countries.

Finally, we examine the quality of the Warren-Spring model by fitting the model on the raw data from both shear devices.

395 5.1. Yield Loci of Limestone powders using RST and PFT

As first step, we look at the raw yield loci of RST-01 using all the above mentioned materials as shown in Fig. 6.

398 We observe that the yield loci are almost linear when the median particle size is larger than 140 µm, and this linear locus is not 399 400 helpful on our main focus in this study, therefore, we decide to take them out when using the Brookfield powder flow tester. As 401 expected, the size increase in powders leads to a lower resistance 402 during shearing, thus a lower yield locus. The yield loci of 30, 71 403 404 and 138 µm are almost collapsing on each other which was already 405 reported in a previous study [24].

Although the semi-automated shear RST device is giving selfreproducible measurements, it is still worth to evaluate the raw yield loci data of PFT using the different size limestone powders also with the Brookfield PFT tester as shown in Fig. 7. The global



Fig. 7. Yield locus of different size limestone powders as in Fig. 6 using Brookfield PFT. The pre-shear normal stress $\sigma_{pre} = 4.8$ kPa is not shown here.

trends of the yield loci measured by PFT is consistent with the trends from Fig. 6, which confirms the good qualitative agreement of both devices.

Furthermore, we have tested the two reference powders using both devices at the same pre-shear stress levels as shown in Fig. 8. The mean values are stable for both devices and all the standard deviations stay within the symbol size range (not shown) confirming self-repeatability. For the free flowing Eskal150, the yield loci demonstrate a very good agreement and the fitted curve matchs all the data points. For the cohesive Eskal300, data from the PFT are lower than that from the RST-01, but with similar nonlinear curvature.

We can speculate about two reasons for the differences in the values we obtain for the shear stress with the Eskal300. The first one would be that the powders measured with the RST could be slightly more wet. This would increase the stickiness due to capillary forces. Therefore the yield locus would be higher [69].

The samples used were collected directly from original sealed bags, eliminating the possibility of being affected by humidity in



Fig. 8. Yield locus of two reference limestone powders: Eskal150 (138 µm) and Eskal300 (2.2 µm) using both RST-01 and Brookfield PFT. The pre-shear normal stresses σ_{pre} are set to 5 kPa for both devices. The nonlinear lines (2.2 µm) are the fitting to the raw data using Warren-Spring model with *C* = 1.29 kPa, *T* = 0.58 kPa, *n* = 1.69 for RST and *C* = 1.02 kPa, *T* = 0.58 kPa, *n* = 1.60 for PFT.

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P. García-Triñanes et al./Advanced Powder Technology xxx (xxxx) xxx

429 such a short time. The reason for this difference would be in the 430 geometry of the cells as explained by Schmitt and Feise (2004) 431 [70]. In a later study, Berry (2007) [71] also reported that the value 432 of the unconfined failure stress σ_c is strongly affected by the test protocol and the procedure of calculation used. Tim Bell (2012) 433 also presented work for BCR-116 limestone and TiO₂ on this issue 434 435 and observed a difference in the geometry of the cells especially the narrow edge and curved (dome-like) cross-section of the PFT 436 lid versus the Schulze tester. He also found differences in the soft-437 ware analysis of the yield locus and steady-state shear [72]. 438

Regarding the protocol, the Brookfield tester measures the 439 440 steady state shear after several (normally above 5) pre-shears but the Schulze ring shear tester determines that in one or two 441 pre-shears. This could result in a slightly different pre-shear his-442 443 tory, the more pre-shear cycles, the weaker the sample is expected 444 to be. It is worth noting that the bed heights for the Brookfield tes-445 ter and for the Schulze tester differed (15 mm and 24 mm, respectively). The distribution of the applied normal force through the 446 sample, and therefore at the shear plane, could also potentially 447 448 impact the results.

449 Berry [40] reported disparity between the Schulze ring shear 450 tester and the PFT in his round robin study with CRM-116 limestone powder. These differences are usually attributed to the shear 451 cell geometry (as mentioned above the annular lids of the two cells 452 453 are different). The Schulze has open pockets (flat lid with vertical 454 vanes) whilst the Brookfield PFT uses closed pockets. Schmitt and Feise [70] found that the standard Peschel cell which featured a flat 455 lid with a knurled contact surface "to grip the powder" measured 456 lower shear stresses than the same lid when fitted with "open 457 458 pocket" vanes of the same dimensions used on the Schulze RST lid.

459 5.2. Non-linearity of Yield Locus at low pre-shear stress levels

The median particle size of powders affects cohesion that will
influence the non-linearity of the yield locus as well as the powder
flow behaviour. The smaller the particle size, the more cohesive the
sample, therefore finer powders typically show higher yield stress
and higher non-linearity. However, the role of the pre-shear stress
is still unclear.

466 In Fig. 9, we look at the raw shear failure points of free-flowing Eskal150 (138 µm) at different pre-shear stress levels between 0.2 467 and 4 kPa. For all the pre-shear stress levels, all the shear failure 468 points collapse on a linear curve, only few points at 3 kPa are devi-469 470 ating slightly from the curve, but within the standard deviation range. This indicates that the free-flowing powder is insensitive 471 472 to the pre-shear stress change, and thus has both cohesion and ten-473 sile strength near zero.

474 However, when we look at the shear failure points of cohesive 475 powders at different pre-shear stress levels as shown in Fig. 10, 476 the shear failure points are separate from each other. With increas-477 ing the pre-shear stress levels, the failure shear stresses also increase, like cohesion and tensile strength, which is due to the 478 pre-consolidation applied. Unlike the free-flowing powder, whose 479 480 bulk density is not sensitive to the pre stress in this change. For 481 the cohesive limestone powder the pre-shear stress leads to considerable compaction and thus the bulk density increases to form 482 483 a stronger bulk solid.

After confirming the repeatability and reproducibility of our raw data from both Schulze RST-01 and Brookfield PFT, we fitted the Warren-Spring model on the raw yield loci of cohesive Eskal300 at different pre-shear stress levels.

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The first important parameter is cohesion, *C*, which is the intercept of fitted non-linear yield locus to the τ -axis. In Fig. 11, we plot the cohesion against the pre-consolidation normal stress for cohesive Eskal300 using both RST-01 and PFT. For RST-01, with increasing the pre-shear stress from 0.2 kPa to 35 kPa, the cohesion



Fig. 9. Shear failure points of Eskal150 (138 μ m) at pre-shear stress levels up to 5 kPa using RST-01. The line is the linear regression fitting to the raw data and pre-shear points are not shown here.



Fig. 10. Shear failure points of Eskal300 ($2.2 \mu m$) at pre-shear stress levels up to 5 kPa using RST-01. Lines are the fitting using the Warren-Spring model as shown in Eq. (2) with only 0.6, 2 and 5 kPa for the sake of clarity. The pre-shear points are also not shown here.

increases from 0.06 kPa to 3.31 kPa. While for PFT, we only tested a narrower range of pre-shear stress from 1 kPa to 4.8 kPa, due to the device limit on the high stress levels when using the normal cell. The cohesion increases from 0.31 kPa to 1.02 kPa. The cohesion values from PFT scatter to slightly lower values than the ones obtained from RST-01, which scatter to larger values but the trend of cohesion agrees very well between the two devices.

The values obtained using the Ajax tensile tester expressed in Pa for Eskal300 are given in Table 4. Note that the standard deviation fluctuates since it is not easy to determine the point of fracture of the bed.

The second parameter in the model is the tensile strength, *T*, which is the intercept of the fitted non-linear yield locus to the σ_n -axis. The tensile strength normally comes in negative sign, which indicates the direction difference to the compressive stresses, e.g. pre-consolidation normal stress. For the sake of convenience, we present T in positive sign as shown in Fig. 12 for the same data as in Fig. 11. Similar to cohesion, the tensile strength increases from 0.01 to 1.70 kPa for RST-01 and from 0.12 to 0.58 kPa for PFT with increasing the pre-shear stress. The relative

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Fig. 11. Unconfined cohesion, *C*, plotted against pre-consolidation normal stress σ for cohesive Eskal300 (2.2 µm) using RST-01 and Brookfield PFT. The line is the fit to both RST and PFT data with the cohesive characteristic consolidation $\sigma_c = 4.52$ kPa, and the slope $n_c = 0.60$.

513 change of T is thus larger than that of C, almost in proportion to the variation of σ_n . The values from the two shear devices agree quite 514 well, with similar scatter as C-data. On the same figure, we have 515 516 also added the tensile strength directly measured from the Ajax tensile tester for three different levels of consolidation (3, 9 and 517 518 27 kPa). The results are based on appearance of a crack that builds 519 up and propagates through the sample and there is plausible agreement with the results from the shear testers and validates 520 the values obtained from Warren Spring model by non-linear 521 522 extrapolation to negative stresses.

523 The last, but also the most interesting parameter in the model is the shear index, n, which indicates the degree of non-linearity of 524 the yield locus. In Fig. 13, the shear index is plotted against the 525 pre-consolidation stress the same data as Figs. 11 and 12. In con-526 trast to cohesion and tensile strength, the shear index decreases 527 528 from 2.05 to 1.41 for RST-01 and from 1.95 to 1.61 for PFT, with 529 increasing pre-shear stress. This means lower pre-shear stress leads to higher non-linearity of the yield locus of Eskal300. In other 530 531 words, with increasing in pre-shear stress, the yield locus becomes more linear but is still far from n = 1 in the stress range tested here. 532 In addition, the shear index seems to saturate around 2 when σ_n 533 tends to zero and around value 1.4 at the high end (> 20 kPa). This 534 might be related to possible lowest/highest bulk density for cohe-535 sive powder, where the bulk density determines the non-linearity 536 537 of the yield loci. Applying a compresive stress to a loose powder is expected to result in a decrease in the void fraction of the powder. 538 Thus in Fig. 14 an increase in the preshear normal stress produces 539 540 an increase in bulk density. In this plot values for RST and PFT 541 agree quite well.

The behaviour of powders subjected to shear at different consolidation stresses can be characterized using the extrapolated values of the tensile strength T to normalize the stress relative to the maximal tensile strength (Fig. 15). The powder with smallest median particle size and strongest interparticle forces appears top left



Fig. 12. Tensile strength, *T*, plotted against pre-consolidation normal stress σ for cohesive Eskal300 (2.2 µm) using RST-01, PFT and Ajax tensile tester with the tensile characteristic consolidation $\sigma_T = 14.26$ kPa, and the slope $n_T = 0.67$.



Fig. 13. Shear index, *n*, plotted against pre-consolidation normal stress σ for cohesive Eskal300 (2.2 µm) using RST-01 and PFT. The line is the fit to only RST data with $\sigma_N = 6.71$ kPa, $n_{min} = 1.39$ and $n_{max} = 2.08$.

in the diagram (2.2 μ m) and the other powders are placed lower and further right with increasing median particle size and normal stress. The descending trend offers a distinctive option for the classification of flowability from very poor (2.2 μ m) to easy flowing (138 μ m).

We can now define the Warren-Spring dimensionless number WS in Eq. (4) as the ratio of the (effective) compression-totension stress difference scaled which has been made dimensionless by the tensile strength.

$$WS = \frac{\sigma_n + T}{T} \tag{4}$$

Table 4

Values obtained for the tensile	strength using the Ajax Tester
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Consolidation	1.1 kPa	3 kPa	9 kPa	28 kPa
Average	131.3	262.5	619.8	1380.6
Standard deviation	61.7	58.3	64.7	89.1

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P. García-Triñanes et al./Advanced Powder Technology xxx (xxxx) xxx



Fig. 14. Steady state bulk density ρ_b plotted against preshear normal stress σ_n for Eskal300 including both RST-01 and PFT. The line is the fit to the data up to 10 kPa pre-shear stress with $\rho_0 = 79 \text{ kg/m}^3$ and $\sigma_\rho = 0.0002 \text{ kPa}$.



Fig. 15. Shear Stress τ plotted against the ratio between normal stress and tensile strength $\sigma/T + 1$ for different size limestone powders including only RST-01.

Fig. 16(a) depicts the influence of the pre-shear stresses in this classification plot for the most cohesive powder Eskal300 (2.2 μ m) obtained by both RST and PFT, with their slightly different results. When the shear stress is normalized by cohesion, C, as shown in Fig. 16(b), the relationship deduced from the Warren-Spring model in Eq. (2), namely:

$$\left(\frac{\tau}{C}\right)^n = \frac{\sigma_n}{T} + 1 \tag{5}$$

is confirmed by the good data-collapse. The evident difference is the dimensionless shear index, n, with value 2 for RST and 1.82 for PFT, indicating that n is sensitive to the device and/or the procedure used.

A failure surface of Eskal300 superimposed involving the consolidation stress σ_n , the void fraction and the shear stress τ , similar to the Hvorslev surface [73] is depicted in Fig. 17. This typical 3D diagram is a graphical representation of the failure criteria including a family of curves for over consolidated states showing the mechanical properties of Eskal300.

The plot includes the critical state line and its projection considering the values of shear stress and the consolidation line when a



Fig. 16. (a) Shear stress, τ , (b) shear stress normalized by cohesion, τ/C , plotted against the ratio between normal stress and tensile strength $\sigma/T + 1$ for Eskal300 at different preshear stresses including both RST-01 and PFT.

powder is sheared in a shear cell under different normal stresses 580 that lead to different void fractions. Failure is characterized by a 581 critical value of void fraction. Consideration of different case studies shows that powder flow through a given process hardware remains the biggest uncertainty with respect to unexpected flow problems with single components or new formulations. Knowing this surface for a certain powder can tell us if it will flow. Between cohesive materials that suffer flow issues, the biggest parametric change is tensile strength. The line showing the variation of tensile strength at different packing densities of the bulk powders which affects the number and strength of particle contacts is also depicted in Fig. 17. This can be linked to inter-particle forces by a Rumpf-type approach, however, the effect of consolidation stress is critical.

The full function which could describe the Hvoslev surface

$$\tau(\sigma_n, \epsilon) = C(\sigma) * \left(\frac{\sigma_n}{T(\sigma)} + 1\right)^{1/n(\sigma)}$$
(6)

with $C(\sigma) = (\sigma/4.6)^{0.6}$, $T(\sigma) = (\sigma/14)^{0.67}$, $n(\sigma) = 1.4 + 0.7 * exp(-\sigma/6.7)$ and $\sigma(\epsilon) = 1/2200 * exp(\frac{1-\epsilon}{35}).$

The surface obtained using the analytical solution described in Eq. (6) is shown in Fig. 18 as well as a family of curves for over consolidated states and tensile strength values for Eskal300.

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Fig. 17. Hvorslev diagram of the Eskal300 data measured using RST-01 at different preshear stresses.



Fig. 18. The Eskal300 data measured using RST-01 at different preshear stresses and the analytical prediction of the Hvorslev surface using Eq. (6).

603 6. Conclusions

This study focused on the tensile strength of cohesive particulate solids, where we used a range of limestone fractions of varying size and thus cohesion and tensile strength. All powders used in this study were dry (mostly insensitive to humidity); their properties were analysed by means of two shear testers, the Schulze Ring Shear tester and the Brookfield Powder Flow Tester.

610 In particular, the sample Eskal300, with $d_{50} = 2.2 \ \mu$ m, was used 611 as the reference cohesive fine powder and stretched for detailed 612 measurements. The shear testers were operated in the region of 613 reduced stresses, with special focus on values under 5 kPa, and to 614 complement these data the Eskal300 was also analysed by directly 615 measuring the tensile strength with the Ajax tensile tester.

Analysing the results, we observe that the Warren-Spring model is a very good description and allows to extract the unconfined cohesion, *C*, the extrapolated tensile strength, *T*, and the shear index, *n*, which characterizes the non-linearity of cohesive powder yield loci. These characteristic quantities depend strongly on the inter-particle forces as established during pre-shearing and preconsolidation.

623 Comparing the results from different shear testers, we find 624 overall very good qualitative agreement with small quantitative differences, since both testers follow similar procedures with625regards to sample preparation and differ slightly with respect to626measurement protocol and geometry. These differences are fortu-627nately not leading to a great deviation in terms of tensile strength,628*T*, although further experiments with a variety of cohesive powders629are needed to confirm or rebut this point.630

As major contribution, for the first time to our knowledge, the tensile strength, *T*, which must be extrapolated from shear tester data, was measured directly for the same fine, cohesive sample, Eskal300, for three different consolidation stress levels (3, 9 and 27 kPa), using the Ajax tensile tester. The tedious direct measurements match very well (within 10% margin) with the results from the shear testers, confirming that the non-linear extrapolation using the Warren-Spring model is valid and that the tensile strength is thus correlated closely to the cohesion of this powder. This observation requires further confirmation for many more powders.

From our results, for one powder so far, we conclude that the standard shear testers can very well be used to predict (by nonlinear extrapolation, using the proper model) the tensile strength in the negative stress range. This is also supported by the perfect data-collapse we observe when plotting them against the "dimensionless effective tensile strength", $\sigma_n/T + 1$, for a wide range of

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APT 2393

P. García-Triñanes et al./Advanced Powder Technology xxx (xxxx) xxx

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648 data, confirming that the Warren-Spring dimensionless number: 649 WS, is nicely combining the interplay between tensile strength 650 and confining stress.

The data necessary to analyse and interpret the effect of preconsolidation and pre-shear of a powder on its mechanical properties based on the expansion failure, void fraction and the consolidation failure could be displayed in a 3-D diagram. A fashion model of the so-called Hvorslev surface is being actively developed based on the values obtained from the Warren Spring model, considering several yield loci at different consolidation stress levels.

The effect of particle size, shape, bulk density and surface energy on all the key model parameters is the ideal outcome of our investigations, which can then be used in the prediction of failure of single powder systems and formulations, or for continuum mechanical modeling of flow.

Such a model with predictive capability to directly quantify the response of powders to external stresses is a particularly valuable since it can directly impact manufacturing performance and efficiency.

Declaration of Competing Interest 667

The authors declare that there is no conflict of interest.

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