VULNERABILITY ANALYSIS OF INDUSTRIAL RC PRECAST BUILDINGS DESIGNED ACCORDING TO MODERN SEISMIC CODES

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11 Abstract

Seismic performance-based design approach is currently implemented in modern building codes. Design requirements and provisions ensure an adequate structural performance under different intensity levels of seismic action. However, the probability of attainment of a performance level is implicitly considered in the code design approach (provisions and requirements); for instance, the minimum requirements in concrete structures cannot be simply correlated to the probability of collapse of the building as well as to its overall structural response.

The aim of this work is to assess the vulnerability with respect to the collapse limit state of industrial 18 19 single-story RC precast buildings designed according to the current Italian seismic code. The 20 comparison between the Italian code and the Eurocodes is provided throughout the paper. A 21 parametric study is performed by investigating the safety against the collapse of 40 RC single-story 22 precast structures. Multi-stripe analyses are performed by non-linear dynamic analyses at 10 intensity 23 levels. The fragility of the structures is defined by means of the incremental N2 method, which has 24 been demonstrated to be a suitable method for evaluating the collapse capacity of single-story precast 25 buildings. The results demonstrate that the buildings are safe against the collapse mainly because of the structural overstrength with respect to seismic actions. The modelling assumptions are also 26 validated in order to demonstrate the negligible influence of the cracking on the collapse as well as 27 28 the importance of the geometrical nonlinearities for precast buildings.

- 29
- 30 **Keywords:** precast structures; seismic safety; fragility curves; incremental N2 method; multi-stripe 31 analysis; building collapse.
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1 1 Introduction

2 The current approach of modern building codes, such as European Eurocodes [1] and Italian 3 building code [2], is based on the performance-based design approach. In the case of the seismic 4 design, the structures have to achieve/show a defined performance under a given intensity level of 5 the seismic action. A semi-probabilistic approach is adopted for the definition of both actions and 6 strength (materials) by means of safety factors and combination coefficients. Moreover, code 7 requirements and provisions (e.g., capacity design rules and seismic details) implicitly allow 8 obtaining an adequate safety against the occurrence of limit states and brittle collapse mechanisms. 9 In the last decades, many authors investigated the efficiency of modern codes for different structural 10 typologies. For instance, some studies have been performed in order to define the effects of the 11 design approach on the structural vulnerability. Most of them investigated existing [3, 4] and new 12 RC frame structures [5]. The current codes significantly improved the design provisions with respect 13 to past laws and regulations for RC precast structures. However, the code improvements have not 14 been fully investigated as well as their influence on the global seismic vulnerability. Moreover, 15 some recent seismic events in Europe have brought into sharp relief the vulnerability of precast 16 buildings [6, 7], opening a scientific debate on the safety of this structural typology. Several 17 experimental tests were performed on new buildings and connection systems [8-10]. On the 18 contrary, few studies have been performed in terms of seismic assessment [11, 12] and risk study of 19 precast buildings [13, 14]. Ercolino et al. [11] assessed the seismic performance of an existing 20 precast structure in Emilia-Romagna (Italy), which was not designed for seismic actions. The 21 modelling approach was validated by comparing the results of nonlinear dynamic analysis to the 22 actual damage of the structure after the earthquakes on May 2012. The seismic assessment 23 demonstrated the high vulnerability of existing buildings because of the poor detailing as well as 24 the absence of adequate connection systems. Casotto et al. [13] developed a set of fragility curves 25 for existing precast RC industrial buildings at different limit states. The buildings were designed

1 essentially for static horizontal loads and with simply supported beam-to-column connections. 2 Kramar et al. [14] performed a systematic seismic risk study on a set of precast structures. The 3 nonlinear model consisted of one equivalent column and the parametric study was defined by 4 varying the seismic masses as well as the column size. The structures were designed for seismic 5 actions according to Eurocode 8 for one value of the peak ground acceleration (0.25 g). The results 6 of the nonlinear analyses demonstrated that that the seismic risk is low if all EC8 requirements 7 (including minimum longitudinal reinforcement requirement) are considered. An extensive 8 parametric study was performed by Palanci et al. [12]. The authors defined the fragility curves of 98 9 existing buildings in Turkey, designed and built from 1990 and 1998. The study results 10 demonstrated that the older buildings can be defined as "low quality structures" whereas the newer 11 buildings are the "good quality structures".

Most of these past research studies investigated the seismic performance of either existing buildings or structures designed by considering only the seismic actions. The combination of nonseismic actions is usually not considered in the design of the structural elements, even if these actions can influence the safety of the buildings. Moreover, nonlinear analyses were performed on single degree of freedom system by neglecting the presence of the eccentricity at the connection levels between the structural elements. Such an approach can influence the feasibility of the results in case of large vertical actions on the buildings.

This paper aims to define the seismic safety in terms of collapse of single-story RC precast buildings, designed according to the Italian building code. An extensive parametric study is performed on several configurations of single-story precast buildings, defined by varying some geometrical features. A rigorous design procedure is adopted in order to simulate real industrial RC precast structures and its results are discussed. A comparison between Eurocode and Italian code requirements is also performed, to extend the obtained outcome. The safety of the analysed buildings with respect to the collapse is investigated through both multi-stripe analyses and the incremental N2 method. In the final part of the paper, some modelling assumptions are discussed, in order to validate
 the study results as well as to define reliable models for future studies.

3 2 Typical structural layout

The investigated structures are single-story RC precast buildings, typically hosting industrial and 4 5 commercial activities in Europe. Their geometrical features are selected in order to represent the most 6 common buildings in Italy. A wide-ranging database was obtained by collecting data of Italian reports 7 about the typology classifications and post-earthquakes assessment surveys [6, 15-17]. Figure 1 8 shows common beam typologies and typical bay spans in Emilia-Romagna region (Northern Italy). 9 The adopted geometrical features are also typical of other seismic-prone countries in Europe, such as 10 Slovenia and Turkey. In Turkey the precast RC members are used commonly for the construction of 11 industrial facilities. Typical spans in these facilities varies between 15 m and 25 m and the typical 12 height of these precast structures ranges between 6 m and 8 m [18]. Babic and Dolsek [19] define the 13 typical geometrical features of one-storey precast buildings in Slovenia: median value of the height 14 is 6.5m with variation of 0.25, the length of the beam is 14.9m (with the dispersion equal to 0.3) and 15 the distance between portals is typically equal to 6.8 (with the dispersion equal to 0.28).



Figure 1 Emilia Romagna database: (a) typology of beams; (b) distribution of bay spans
The investigated structural typology is defined as "isostatic columns" (Figure 2), i.e., single-story
structures with cantilever columns. These RC precast buildings usually consist of the following

elements: isostatic columns, prestressed principal and secondary beams pinned to the columns, roof
 elements pinned to the beams and vertical/horizontal cladding panels connected to the
 beams/columns.

4 Figure 2 shows the frontal view of the case studies in Y direction (a) and the plan view (b). The 5 structure consists of 4 bays in X direction and 1 bay in Y direction. In this study the structural elements 6 have the following features: monolithic precast columns, rectangular-shaped beams along X 7 direction; prestressed principal beams with variable cross-section along Y direction; prestressed TT 8 roof elements along X direction and vertical cladding panels. The columns have a fork (or corbel) at 9 the top and a socket foundation at the base. The fork of the columns is adopted in order to restraint 10 the torsional and lateral rotation of the beams. The principal/secondary beams are connected to the 11 columns by steel dowels. The dowel connection consists of steel threaded bars inserted in both the 12 beams and the columns (Figure 3). Such connection systems can be assumed as a pinned connection 13 because of the limited rotational strength under horizontal loads [20, 21]. Panel-to-structure 14 connections consist of steel elements and they are designed in order to support the weight of the 15 panels and the seismic actions in the out of plane direction. This connection system should allow the 16 relative displacement between the panel and the structure. Recent seismic events demonstrate that the 17 panel can interact with the main structural elements under seismic actions because of either 18 construction errors or limited space in the connection elements. However, the strength of the panel-19 to-structure connection under seismic loads is very small and it fails at very low intensity without 20 significantly influencing the global seismic performance [9].

Four geometrical configurations are assumed in this study by varying the height of the columns (H in Figure 2(a)) and the width of the bays (L_1 and L_2 in Figure 2(b)). Table 1 shows the geometrical features of the investigated case-studies. The presence of a crane is assumed in the case studies since single-story precast structures usually host industrial activities. The crane is supported by a bracket, placed on the column at 4.5m for the geometries 1 and 2 and at 7.5m for the geometries 3 and 4 (H₁ in Table 1).







Figure 3 Typical beam-to-column dowel connection

Constrained configuration (Coo)	L_1	L_2	Н	\mathbf{H}_{1}
Geometrical configuration (Geo)	[m]	[m]	[m]	[m]
1	15.00	6.00	6.00	4.50
2	20.00	8.00	6.00	4.50
3	15.00	6.00	9.00	7.50
4	20.00	8.00	9.00	7.50

Table 1 Geometrical configurations of the case studies

4 **3** Prototype structures: design and modelling

5 The study investigates several single-story precast structures. This section describes the adopted 6 design approach as well as the nonlinear numerical model. The main features of all the buildings will 7 be presented in terms of dimensions of structural elements and reinforcement details.

8 The described buildings are designed according to the Italian building code [2] in five sites in Italy

9 (Table 2). Two typologies of soil are considered: type A (the average velocity of S waves in the upper

10 30 m, $V_{s,30}$, is larger than 800m/s) and type C ($V_{s,30}$ is in the range: 180m/s - 360m/s). Therefore, the

11 parametric study consists of 40 case studies. In the following sections, each case study is identified

1

by an ID, defining the geometrical configuration, the site and the soil type: for instance ID "Geo1CA-soilA" refers to the case study with the geometrical configuration 1 ("Geo 1") and located in
Caltanissetta (CA) on a rigid soil (A).

Site (S)	Latitude	Longitude	ag [g]-TR=50years	a _g [g]-
L'Aquila (AQ)	13.399	42.349	0.104	0.261
Napoli (NA)	14.268	40.854	0.060	0.168
Roma (RM)	12.479	41.872	0.055	0.123
Caltanissetta (CA)	14.060	37.480	0.034	0.073
Milano (MI)	9.186	45.465	0.024	0.050

4 **Table 2 Sites of the case studies**

5 **3.1 Design approach**

6 The case studies are designed according to the Italian building code [2]. The design of precast 7 buildings takes into account several actions: permanent actions (self-weight and permanent non-8 structural weights), non-seismic variable actions loads (e.g., imposed load, wind and snow) and 9 seismic actions (both vertical and horizontal components). Two limit states are considered under 10 seismic loads: the Damage Limitation (DL) Limit State (LS) and the Ultimate (U) Limit State (LS).

11 Table 3 shows the considered actions for the main structural elements. The design of both the 12 secondary beams and the cladding panels is not performed in this study. Constant geometrical features 13 are assumed for these elements in all the case studies: the secondary beams have rectangular-shaped cross-section (30cm x 60cm); the vertical panels have a self-weight of $4kN/m^2$ and their height is 14 15 assumed equal to the sum of the column height, the maximum height of the principal beam at the mid 16 span and the height of the roof elements. This simplified approach does not jeopardize the reliability 17 of the study because in real structures the geometry of these elements does not significantly change 18 in different geometrical configurations.

19 The connection systems are not designed in this study and their seismic behavior is not modelled in 20 the numerical analyses; they are assumed strong and stiff enough to avoid their brittle/premature 21 failures. Both Italian code and Eurocodes give specific design provisions for the connections in 22 precast structures. They should be designed according to the capacity design principle by adopting 23 large safety factors. Moreover, other design guidelines as well as past research studies recommend detailing of the connected elements in order to avoid any brittle failure of the connection. The above
cited provisions/guidelines ensure that the connection strength is large enough with respect to the
yielding capacity at the column base. Such statement was also justified by past experimental tests
[21].

5 The foundation system is not designed; in the numerical analyses a fixed constraint is assumed at the 6 base of the columns. The column fork is constant in all the buildings: the height is equal to 60cm and 7 the thickness is 15cm. The structural materials are constant for all the case studies: the concrete has 8 a cubic cylinder compressive strength of 45N/mm² and the reinforcement steel has a characteristic 9 yielding strength of 450N/mm².

10 **Table 3 Loads for the designed structural elements**

Structural element	Permanent actions	No-seismic variable actions	Seismic horizo	ontal action	Seismic vertical action
Roof elements	Self-weight	Live load Snow	None		Negligible
Principal beams	Self-weight	Live load Snow	None		ULS
Columns	Self-weight	Live load Snow Wind Crane Imperfections	DLLS	ULS	None

11 3.1.1 Roof elements

12 The roof of the structures consists of TT prestressed elements (Figure 4). These elements are 13 connected to the principal beams by means of dowel connections. At the top they are connected to 14 each other by means of metallic systems as well as by a cast-in-situ concrete slab (with a thickness 15 of 5cm). According to the Italian code [2], this connection system (i.e., connected roof elements and a concrete slab thicker than 4cm) ensures that the roof behaves as a rigid body in its own plane. In 16 17 Eurocode 8 [1], the rigid diaphragm hypothesis is not related to either geometrical limits or 18 connection systems; it should be verified in terms of in-plane flexibility by means of structural 19 analyses. However, the assumed hypothesis is valid, as broadly recognized in past studies [22].

1 The roof is designed for the following actions: the live load is equal to 0.5kN/m² (roof of an industrial 2 building) and the snow is evaluated as a distributed vertical load, according to the site. The Italian 3 code requests to consider the vertical component of the seismic action in the design of a prestressed 4 horizontal element if: 1) the building is located in a medium-high seismic zone (e.g., the peak ground 5 acceleration, a_g , of the site is larger than 0.150g for a return period of 475 years); 2) the span of the 6 roof element is larger than 8m. Therefore, the vertical component of the seismic action is neglected 7 for the design of the roof elements in all the investigated case studies. In Eurocode 8, the vertical 8 component of the seismic action is considered if the peak ground acceleration is larger than 0.25g 9 (e.g., L'Aquila) and the horizontal or nearly horizontal elements are pre-stressed (there are no limits 10 on the span width). However, this difference does not significantly influence the design results for 11 the two codes; the demand due to the non-seismic actions is usually larger than the seismic one for 12 these horizontal elements. Table 4 shows the dimensions of the TT roof elements in all the case 13 studies: B is the width of the roof element and H_{roof} is the height. The details about the reinforcement 14 bars are not reported in this paper since they are not required to perform the nonlinear analyses (see 15 Section 4).



Figure 4 Layout of the roof: TT elements and cast in-situ slab

1 abit + Dimensions of the 1 1 root cienterus	Ta	ble	4	Dimensions	of	the	TT	roof	elements
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В	Hroof	Site	Soil	Configuration
[cm]	[cm]	[-]	[-]	[-]
160	40	All	A, C	1, 3
240	40	All	A, C	2, 4

16 3.1.2 Principal beams

17 The principal beams are prestressed RC elements with variable cross-section: a T-shaped section at 18 the connection to the column and an I-shaped section close to the mid-span. The principal beams are 19 designed under two combinations of actions: 1) the combination of vertical actions (self-weight, 20 live/imposed loads and snow) and 2) the combination of the seismic vertical component. For these

elements the vertical component is considered for the structures located in AQ and NA (when a_g is
larger than 0.15g at the ULS) with all the geometrical configurations (the span of the beams is always
larger than 8m).

Table 5 shows the dimensions of a rectangular-shaped section, equivalent to the principal beams in terms of area and mass: B_{mean} is the mean value of the beam base and H_{mean} is the mean value of the beam height. The principal beams are pinned to the columns and they do not contribute to the lateral response under seismic actions. The details about the reinforcement are not reported in this paper since they are not used in the numerical analyses (see Section 4).

9 Table 5 Mean dimensions of the principal beams for all the case studies

B _{mean}	H _{mean}	Site	Soil	Geometry
[cm]	[cm]	[-]	[-]	[-]
19	114			1
19	150	A 11		2
19	114	All	A, C	3
33	140			4

10 3.1.3 Columns

11 The columns are precast square-shaped elements; both the cross-sections and the reinforcement 12 ratios are constant in each structure. As anticipated in Table 3, the design of the columns should take 13 into account several actions and, therefore, several combinations. A tri-dimensional elastic model 14 (Figure 5) is implemented in OpenSees program [23] in order to evaluate the demand on the structures 15 under both vertical and seismic actions. The accidental eccentricity is defined for the centre of mass 16 according to the provisions in both the Italian code and Eurocode 8 in order to take account for 17 uncertainties in the location of masses. The dimensions of the structures are given in Table 1. The 18 model consists of elastic one-dimensional elements: 1) elastic columns with a 50% reduced stiffness, 19 2) elastic principal beams with an equivalent rectangular-shaped section (Table 5) and 3) elastic 20 secondary beams. The use of an equivalent section for the principal beams does not influence the 21 final results of the paper since the main goal is the assessment of the seismic safety of the structure 22 by considering the failure at the column base only. If some failure modes of the beams should be

taken into account, the modelling approach of the beam should consider the actual torsional and
lateral stiffness of the elements.

3 Concerning the connection systems, the following modelling assumptions are considered.

- 4 The columns are fixed at the base and the height is equal to the values in Table 1 (H).
- The principal beams are connected to the columns (Figure 5(a)) by hinges, simulating the dowel
 connections. The eccentricity between the column and the beam axis (e_{pr} in Figure 5(b)) is assumed
 equal to half of the mean beam height (Table 5).
- 8 The secondary beams are connected to the column forks by hinges. Horizontal and vertical
 9 eccenticities are considered (Figure 5(b)):

10
$$e_{sec,h} = B/2 - t/2$$
 (1)

$$11 \qquad e_{sec,v} = h_f + H_{sec}/2 \tag{2}$$

In Eq. (1) $e_{sec,h}$ is the horizontal eccentricity, B is the column dimension and t is the fork/corbel thickness (15cm). In Eq. (2) $e_{sec,v}$ is the vertical eccentricity, h_f is the fork/ corbel height (60cm) and H_{sec} is the height of the secondary beams.

15 - The crane is applied to the column by means of a bracket. This bracket is assumed as a rigid element
16 with a breadth of 60cm (e_b in Figure 5(a)).



17 18



1 variable action is defined as either the main variable action or a secondary one. For instance, if the 2 snow and the wind are the two variable actions, two combinations should be defined: 1) the snow is 3 the main variable action and the wind is the secondary one; 2) the wind is the main variable action 4 and the snow is the secondary one. During the design phase all the possibile combinations of the 5 action in Table 6 are considered. The values of the actions depend on both the geometry of the case-6 studies and the site. Table 7 shows typical values (minimum and maximum) of the loads due to the 7 wind, snow and crane in all the case-studies. The number of the considered combinations increases 8 if the following conditions are taken into account: the imperfections and the wind actions are not 9 considered acting simultaneously in the two horizontal directions; different locations of both the crane 10 and the crane hook should be assumed and the temperature distorsion (15°C) can assume both positive 11 and negative values. It is worth to highlight that the demand due to non-seismic actions is amplified 12 in order to take into account the effect of the geometrical nonlinearities, if necessary.



Table 6 Loads on the columns

Actions	Symbol
Crane - hook	F ₁
Crane – Self weight	Gc
Crane – supporting beam	Qc
Crane – skewing force	Ft
Crane – acceleration force	F _b
Wind	F_{w}
Imperfections	Hi
Self-weight	G_{col}
Secondary beams – self-weight	Gsec
Secondary beams – live load	Qsec
Principal beams - self-weight	Gpr
Roof elements - self-weight	G _{roof}
Roof elements - live load	Q
Temperature	ΔT

13 Table 7 Typical values of actions for the case-studies

Actions	Typical values (minimum and maximum) [kN]
Crane - hook	100
Crane – Self weight	25
Crane – supporting beam	[4.65-12.40]
Crane – skewing force	15
Crane – acceleration force	21.43
Wind	[12.83-89.15]

1 Dynamic linear analyses are perfored by means of the above described elastic model in OpenSees in order to evaluate the seismic demand on the column. The analyses are performed in both the 2 3 horizontal directions and the seismic effects are then combined. According to the Italian code, the 4 structure should be verified for two limit states: DLLS and ULS. In this study the behavior factor is 5 assumed equal to 2.5 for all the case studies, according to the Italian code provisions for isostatic columns in ductility class "B" (medium ductility in EC8). In EC8 the investigated structures are 6 7 defined as frame structures; therefore, the behaviour factor is larger (q=4.5) than the factor used by 8 the Italian code. However, this q value can lead to an overestimation of the dissipative properties of 9 the precast industrial buildings under seismic actions [24]. In the combinations of seismic actions, 10 several cases should be defined to take into account the different locations of the crane. P- Δ effects 11 are also taken into account during the design phase according to the Italian code (and Eurocode 8) 12 provisions: 1) amplification of the effets according to the value of the stability factor, θ [25]; 2) 13 mimimum dimensions of the column section, i.e. larger than 1/10 of the shear length, if P- Δ effects 14 are not negligible (θ larger than 0.1).

15 The column dimensions are reported in Figure 7 for all the case studies: the height of the bars is the 16 cross-section dimension and the color represents the ratio of the longitudinal reinforcement.





1 Figure 7 Column dimensions and ratio of the longitudinal reinforcement

2 According to these results, some conclusions can be drawn.

Most of the case studies provide a low reiforcement ratio, about 1% (i.e., the minimum ratio
 required by the code). This minimum requirement can lead to a significant overstrength of the
 structures.

The reinforcement ratio is larger than 2% if the structure is located in a high seismic zone (e.g.,
AQ) on flexible soil ("C") and the column height is 6m (Geo1 and Geo2). In this case, the column
dimensions are smaller than the corresponding case studies with Geo3 and Geo4 because the
DLLS verification is less restrictive; hence, at the ULS a larger quantity of reinforcement is
requested.

Only in few structures the reinforcement design is influenced by the seismic action rather than
 by other actions. Figure 8 shows the limit interaction surfaces of two case studies (Geo3-AQ SoilA and Geo3-AQ-SoilC) along with the points corresponding to the demand for all the
 combinations of actions. These combinations are identified in the legend by the main variable
 action. The maximum effects are due to the seismic actions only for flexible soil; in the other
 cases, wind action gives the maximum demand on columns.

In few cases the column dimensions are larger than 1/10 the shear length (i.e., the column height
in the investigate structures); in the most of the structures the geometrical nonlinearities are
negligible (i.e., stability factors are smaller than 0.1).



Figure 8 Limit interaction surfaces for a perimetral column: (a) Geo3-AQ-A and (b) Geo3-AQ-C 3.2 Proposed modelling approach

1

2 Nonlinear dynamic analyses are performed for all the case studies in order to evalaute their seismic 3 performance. The nonlinear model is implemented in OpenSees; it consists of columns, secondary 4 beams and principal beams, as shown in Figure 2 and Figure 5. The horizontal elements (beams) are 5 elastic single-dimensional elements. The nonlinear behaviour of the structure is concentrated at the 6 columns base and it is simulated by means of a lumped plasticity approach. The columns are fixed at 7 the base in the nonlinear model. The beam-to-column connections are assumed strong pinned system. 8 The plastic hinge is defined by means of a tri-linear moment-rotation curve [26], consisting of: the 9 yielding point (green point in Figure 9), the capping point (yellow point in Figure 9) and the post-10 capping point (red point in Figure 9). The yielding moment (M_y) is defined by performing a fiber 11 analysis on the RC cross-section and it is evaluated as the minimum value between the yielding of 12 the steel reinforcement and the attainment of the maximum strenght in the concrete cover. The 13 yielding rotation (θ_v) is evaluated according to Fardis [27] and both the capping point (M_c , θ_c) and 14 post-capping rotation (θ_{pc}) are evaluated according to Haselton [28]. The hysteretic behaviour is 15 modelled according to Ibarra [29]. The seismic mass of the structure is concentrated in the geometrical 16 barycenter at the roof level.

For each case study two different plastic hinges are defined for perimetral columns and corner columns, according to the axial loads on the columns. The mean value of the material (concrete and steel) strength is used in the nonlinear analyses (Table 8). The mean strenghts are evaluated by

- 1 adopting typical exeperimental values of the coefficients of variation (COV) [30]. The model of the
- 2 structures is provided as supplementary material with this paper.



columns and range of the characteristic points

 Table 8 Mean value and COV for concrete and steel

Concre	ete	Steel		
fcm	COV	fym	COV	
$[N/mm^2]$	[%]	$[N/mm^2]$	[%]	
59.75	15	490.3	5	

4 Vulnerability assessment

3

4 The seismic response of precast buildings is investigated by means of the following steps: 1) nonlinear 5 static analyses are performed in order to define the capacity of the structures at the collapse limit state; 2) multi-stripe analyses are performed in order to define the seismic safety of the structures and 6 7 3) incremental N2 (IN2) method is also applied in order to define their seismic safety. The multi-8 stripe analyses [31] are performed at 10 intensity levels (i.e. 10 return periods in Table 9); a set of 20 9 real records is selected at each intensity level for five sites and both the soil types. A detailed 10 probabilistic hazard study has been performed in the framework of the same national project of this 11 research. The details of the study are presented in [32]. The records were selected by means of the 12 Conditional Spectrum (CS) approach [33-35] at a reference period of 2.0 seconds, given the structural 13 typology. Figure 10 shows the response spectra of the selected records for Caltanissetta on Soil A. 14 The colours show the intensity levels.



Figure 10 Spectra of the records for Caltanissetta on soil A

Table 9 Return periods for 10 intensity levels

IM [-]	1	2	3	4	5
T _R	10	50	100	250	500
[years]					
IM [-]	6	7	8	9	10
T _R	1000	2500	5000	10000	100000
[years]					

1 4.1 Numerical results

The capacity of the structures is evaluated at the collapse limit state by means of pushover analyses. The capacity point (collapse force and displacement) is evaluated on the pushover curve (red point in Figure 11) at 50% reduction of the peak strength (green point in Figure 11). Table 10 shows the capacity drift of the structures. The values of the collapse drift are almost constant with the site and the geometry. The collapse of the structures occurs at an average reduction value of the maximum moment equal to 36%.



Table 10 Capacity in terms of drift [%] Soil Geo 1 Geo 2 Geo 3 Geo 4 Site (S) Drift Drift Drift Drift Type 12.8 10.9 10.0 9.8 L'Aquila С 12.6 13.9 10.6 10.6 11.0 12.5 10.0 9.9 A Napoli С 13.0 9.9 11.5 10.0 10.8 12.4 10.0 9.9 А Roma С 11.0 12.8 10.0 9.9 12.4 A 10.8 10.0 9.9 Caltanissetta С 10.8 12.4 10.0 9.9 11.3 12.4 9.5 9.6 A Milano С 11.3 12.4 9.5 9.6

8 The multi-stripe analyses are performed on all the case studies and the results are reported in terms 9 of demand/capacity (D/C) ratios along with the reference (T=2.0sec) spectral acceleration at each 10 intensity level (Figure 12). The ratio is evaluated as the maximum of the ratios in the two horizontal 11 directions. The square markers are the cases of dynamic instability; for these points, a fictitious 12 displacement is plotted since they correspond to very large demand in terms of drift in the structures. 13 According to the results of the nonlinear dynamic analyses, the following conclusions can be found.

By changing the seismic hazard of the site, the safety of the structure significantly changes. This
 can be justified by the adopted design approach. The column cross-sections and the reinforcement
 ratios do not change in most of the structures (Figure 7) because of the code minimum
 requirements in seismic prone areas.

The geometry does not significantly influence the seismic behaviour of the structure. The higher
 structures (H=9m) are safer in L'Aquila (high seismic hazard): the design code provides severe
 requirements for high flexible structures (minimum section of columns because of P-Δ effects).

- The soil type influences the structural response in terms of number of collapse cases (e.g. Geo2AQ). This means that the increment of design reinforcement and section dimensions due to the
 soil C with respect to the soil A is not able to guarantee the same safety against the collapse.

11 **4.2 Vulnerability**

12 According to the results of the multi-stripes analysis, very few collapses (D/C>1) are recorded for the 13 investigated case studies. The multi-stripe analysis can be adopted for defining the fragility curves if 14 there is a wide range of spectral accelerations at the collapse and a larger number of collapses. Therefore, this analysis method has been used only for four case studies (Geo3-AQ-SoilA, Geo3-AQ-15 16 SoilC, Geo4-AQ-SoilA and Geo4-AQ-SoilC) by amplifying the last IM level (10) up to achieve the 17 collapse for 50% of the records (due to either the attainment of the collapse displacement or the 18 dynamic instability). The maximum adopted record amplification factor is equal to 1.6 for all the case 19 studies. The fragility curves for the four case-studies are presented in Figure 13.

A different method is needed to assess the vulnerability with respect to the collapse limit state of the other case studies, such as the incremental N2 (IN2) method [36]. In order to verify the reliability of such method for precast single-story structures, the IN2 curves can be compared to the fragility curves obtained by the multi-stripe analyses in terms of mean collapse acceleration. These curves are obtained by multi-stripe analyses, according to the maximum likelihood method [37].



1 Figure 12 Results of the multi-stripe analysis: D/C ratios along with the spectral accelerations (T=2sec)

1 Figure 14 shows the IN2 curves for the case studies by adopting the relationships R-µ-T for bare structures [36]. The final point of the IN2 curves corresponds to the attainment of the collapse 2 3 displacement. In the case of fragility curves, the median value of Sa is assumed as the collapse spectral acceleration. For the two case studies on soil A the values of the collapse Sa in the two methods are 4 5 very similar (the maximum difference between the two methods is equal to 10%), while in the case 6 of the structures on soil C the differences are about 29%. The results of the IN2 method are consistent 7 with the fragility study; moreover, the method outcomes are consistent with the overall behaviour of 8 the structures in terms of influence of both the geometry and the soil type. Therefore, the IN2 method 9 is adopted in the following in order to define the fragility of the case studies at the collapse limit state, 10 in terms of PGA (Table 11) and S_a.



Figure 13 Fragility curves for Geo 3 (red line) and Geo 4 (black line) on soil A (solid line) and soil C (dashed line)



Figure 14 IN2 curve for Geo 3 (red line) and Geo 4 (black line) on soil A (solid line) and soil C (dashed line)

Since the reliability of the IN2 method has been proved in the previous comparison (Figures 12 and
 13), this method is performed to assess the safety of all the case-studies with respect to the collapse.
 Table 10 shows the following parameters:

- PGA_c is the capacity of the structures evaluated by the IN2 method at the collapse
 displacement.
- PGA_d is the seismic demand, defined as the peak ground acceleration providing the collapse
 displacement.

8 By applying the IN2 method, the safety of all the case studies is demonstrated with respect to the 9 collapse. The values of capacity in terms of PGA at the collapse are significantly influenced by the 10 seismicity of the site; the value at L'Aquila is always 40% larger than the PGA at Milano. This 11 difference is larger for the highest structures (H=9m) and for soil C.

The large capacity over demand ratios are consistent with some experimental evidences as well as recorded damage during recent seismic events. The good seismic performance of precast buildings was demonstrated in Kramar et al. [14] by the stable response under seismic actions of the buildings up to large value of drift (8%). Moreover, recent seismic events showed the good performance of the most recent structures under the earthquake because of the use of modern provisions both in Turkey [38] and in Italy [39].

memo	**						
	Site	PGAc	PGAd	(۲	Site	PGAc	PGAd
il /	L'Aquila	1.09	0.26	oil (L'Aquila	1.49	0.36
S.	Napoli	1.10	0.19	S	Napoli	1.09	0.27
-	Roma	1.27	0.12		Roma	0.94	0.17
feo	Caltanissetta	0.42	0.07	ieo	Caltanissetta	0.89	0.10
9	Milano	0.64	0.05	9	Milano	0.85	0.070
	Site	PGAc	PGAd	(۲	Site	PGAc	PGAd
il /	L'Aquila	1.57	0.26	oil (L'Aquila	1.34	0.36
S.	Napoli	1.51	0.19	-So	Napoli	1.21	0.27
5	Roma	1.91	0.12	5	Roma	1.54	0.17
,e0	Caltanissetta	0.57	0.07	eo	Caltanissetta	0.53	0.10
0	Milano	0.93	0.05	Ŭ.	Milano	0.79	0.070
	Site	PGAc	PGA _d	(۲	Site	PGAc	PGAd
il A	Site L'Aquila	PGA c 0.81	PGA d 0.26	il C	Site L'Aquila	PGA _c 0.90	PGA d 0.36
- Soil A	Site L'Aquila Napoli	PGA _c 0.81 0.79	PGAd 0.26 0.19	- Soil C	Site L'Aquila Napoli	PGA _c 0.90 0.57	PGAd 0.36 0.27
3 – Soil A	Site L'Aquila Napoli Roma	PGA _c 0.81 0.79 0.94	PGA _d 0.26 0.19 0.12	3 – Soil C	Site L'Aquila Napoli Roma	PGA _c 0.90 0.57 0.67	PGA _d 0.36 0.27 0.17
reo 3 – Soil A	Site L'Aquila Napoli Roma Caltanissetta	PGA _c 0.81 0.79 0.94 0.34	PGA _d 0.26 0.19 0.12 0.07	ieo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta	PGA _c 0.90 0.57 0.67 0.29	PGAd 0.36 0.27 0.17 0.10
Geo 3 – Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano	PGAc 0.81 0.79 0.94 0.34 0.44	PGA _d 0.26 0.19 0.12 0.07 0.05	Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano	PGAc 0.90 0.57 0.67 0.29 0.35	PGAd 0.36 0.27 0.17 0.10 0.070
A Geo 3 – Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano Site	PGA _c 0.81 0.79 0.94 0.34 0.44 PGA _c	PGA _d 0.26 0.19 0.12 0.07 0.05 PGA _d	C Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano Site	PGA _c 0.90 0.57 0.67 0.29 0.35 PGA _c	PGAd 0.36 0.27 0.17 0.10 0.070 PGAd
oil A Geo 3 – Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila	PGAc 0.81 0.79 0.94 0.34 0.44 PGAc 0.82	PGAd 0.26 0.19 0.12 0.07 0.05 PGAd 0.26	oil C Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila	PGAc 0.90 0.57 0.67 0.29 0.35 PGAc 0.88	PGAd 0.36 0.27 0.17 0.10 0.070 PGAd 0.36
-Soil A Geo 3 - Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli	PGAc 0.81 0.79 0.94 0.34 0.44 PGAc 0.82 0.81	PGA _d 0.26 0.19 0.12 0.07 0.05 PGA _d 0.26 0.12	-Soil C Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli	PGAc 0.90 0.57 0.67 0.29 0.35 PGAc 0.88 0.59	PGAd 0.36 0.27 0.17 0.10 0.070 PGAd 0.36 0.27
4-Soil A Geo 3-Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli Roma	PGAc 0.81 0.79 0.94 0.34 0.44 PGAc 0.82 0.81 0.96	PGA _d 0.26 0.19 0.12 0.07 0.05 PGA _d 0.26 0.19 0.12	4 – Soil C Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli Roma	PGAc 0.90 0.57 0.67 0.29 0.35 PGAc 0.88 0.59 0.68	PGAd 0.36 0.27 0.17 0.10 0.070 PGAd 0.36 0.27
ceo 4 – Soil A Geo 3 – Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli Roma Caltanissetta	PGAc 0.81 0.79 0.94 0.34 0.44 PGAc 0.82 0.81 0.96 0.35	PGAd 0.26 0.19 0.12 0.07 0.05 PGAd 0.26 0.19 0.12	ieo 4 – Soil C Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli Roma Caltanissetta	PGAc 0.90 0.57 0.67 0.29 0.35 PGAc 0.88 0.59 0.68 0.29	PGAd 0.36 0.27 0.17 0.10 0.070 PGAd 0.36 0.27 0.10
Geo 4 – Soil A Geo 3 – Soil A	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli Roma Caltanissetta Milano	PGAc 0.81 0.79 0.94 0.34 0.44 PGAc 0.82 0.81 0.96 0.35 0.46	PGA _d 0.26 0.19 0.12 0.07 0.05 PGA _d 0.26 0.19 0.12 0.05 PGA _d 0.26 0.19 0.12 0.07 0.05	Geo 4 – Soil C Geo 3 – Soil C	Site L'Aquila Napoli Roma Caltanissetta Milano Site L'Aquila Napoli Roma Caltanissetta Milano	PGAc 0.90 0.57 0.67 0.29 0.35 PGAc 0.88 0.59 0.68 0.29	PGAd 0.36 0.27 0.17 0.10 0.070 PGAd 0.36 0.27 0.10 0.070

Table 11 Results in terms of collapse capacity (PGA_c) and collapse demand (PGA_d) by means of IN2 1 -----

3

Some considerations about modelling assumptions

In order to validate the performed study in terms of modelling approaches/assumptions, the following 4 5 results are presented for the case study Geo3-AQ-SoilA.

6 Figure 15 shows the fragility curves obtained for this case study with (blue curve) and without (red 7 curve) modelling the cracking point in the plastic hinge. In this case, the influence of the modelling 8 assumption is negligible and the median value at the collapse limit state does not change. This 9 happens for all the analyzed cases, because in ductile structures the collapse behavior is not much 10 influenced by the cracking behavior. Figure 16 shows the influence of P- Δ effects on the seismic 11 response of the same case-study. In this case, the geometrical nonlinearities influence the behavior: 12 the median value of the spectral acceleration at the collapse limit state with P- Δ effects is 11% smaller 13 than the value without these effects. This conclusion can be generally extended to all the other 14 analyzed cases.

2



Figure 15 Comparison between fragility curves with and without modelling cracking (AQ-SoilA-Geo3)



Figure 16 Comparison between fragility curves with and without P- Δ effects (AQ-SoilA-Geo3)

1 5 Conclusions

The seismic performance of industrial single-story RC precast buildings is evaluated by means of nonlinear dynamic and static analyses on a set of buildings, designed according to modern building codes. According to the results of the design, it is found that most of the structures are influenced by the seismic details required by the code; in many cases the seismic action does not give the largest demand on the structural elements.

7 By analysing the seismic performance of the structures, the following conclusions can be drawn.

- The capacity of the structures is quite constant with the geometry and it is lightly influenced
 by the seismicity of the site because of the seismic details and the design overstrength.
- The results of the multi-stripe analyses show a large overstrength of the structures, which
 decreases as the site seismicity increases; in the case of low seismicity, the seismic demand
 on structures can be very low even for an intensity measure with a return period of 100000
 years. Only for the case studies in L'Aquila on soil C at the maximum intensity level some
 collapses occurred.

The overstrength has a fundamental role in the seismic response of the structures. The minimum provisions and the wind and static loads significantly influence the final strength. The capacity of the structures is quite constant with the geometry and it is lightly influenced by the seismicity of the site because of the wind and static loads, the seismic details and the design overstrength. The results of the multi-stripe analyses show a large overstrength of the structures, which decreases as the site seismicity increases; in the case of low seismicity, the seismic demand on structures can be very low even for an intensity measure with a return period of 100000 years. Only for the case studies in L'Aquila on soil C at the maximum intensity level some collapses occurred.

5 The IN2 method is defined as the most feasible analysis method for assessing the capacity of precast 6 one-story buildings at ultimate limit states. The large overstrength of the structures require very large 7 intensities in order to achieve the collapse of the columns. Such intensities cannot be simulated with 8 real records and the amplification factors become unrealistic.

9 The modelling approach is also validated: 1) the cracking of the section can be neglected in the 10 assessment of the seismic safety at ultimate limit states and 2) the geometrical nonlinearities 11 significantly influence the seismic response of precast structures, given the flexibility of the slender 12 columns as well as the pinned connections to the beams.

13 The study results are valid for structures with strong connection between the structural elements. Such

14 hypothesis is guaranteed by the capacity design approach provided by the modern codes. The

15 influence of the cladding panels is not considered in the structural model and, moreover, the failure

16 of these non-structural elements is not considered in the definition of the attainment of the limit state,

17 i.e. by limiting the maximum drift capacity of the columns.

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21 **References**

22 [1] CEN. Design of structures for earthquake resistance, part 1. Eurocode 8. 2005;Brussels.

23 [2] D.M. 14/01/2008. Norme tecniche per le costruzioni. Roma, Italia: G.U. n. 29 04/02/2008; 2008.

24 [3] Kosic M, Fajfar P, Dolsek M. Approximate seismic risk assessment of building structures with

25 explicit consideration of uncertainties. Earthq Eng Struct D. 2014;43:1483-502.

[4] Fiore A, Porco F, Raffaele D, Uva G. About the influence of the infill panels over the collapse
mechanisms actived under pushover analyses: Two case studies. Soil Dyn Earthq Eng. 2012;39:1122.

- 29 [5] Ercolino M, Ricci P, Magliulo G, Verderame GM. Influence of infill panels on an irregular RC
- 30 building designed according to seismic codes. Earthq Struct. 2016;10:261-91.

- [6] Magliulo G, Ercolino M, Petrone C, Coppola O, Manfredi G. The Emilia Earthquake: Seismic
 Performance of Precast Reinforced Concrete Buildings. Earthq Spectra. 2014;30:891-912.
- 3 [7] Belleri A, Brunesi E, Nascimbene R, Pagani M, Riva P. Seismic Performance of Precast Industrial
- 4 Facilities Following Major Earthquakes in the Italian Territory. Journal of Performance of
- 5 Constructed Facilities. 2015;29:04014135.
- 6 [8] Toniolo G. SAFECAST project: European research on seismic behaviour of the connections of
- precast structures. 15th World conference on earthquake engineering (15WCEE), Lisbon, Portugal.
 2012.
- 9 [9] Biondini F, Dal Lago B, Toniolo G. Role of wall panel connections on the seismic performance 10 of precast structures. Bulletin of Earthquake Engineering. 2013;11:1061-81.
- 11 [10] Zoubek B, Fischinger M, Isaković T. Cyclic response of hammer-head strap cladding-to-12 structure connections used in RC precast building. Engineering Structures. 2016;119:135-48.
- [11] Ercolino M, Magliulo G, Manfredi G. Failure of a precast RC building due to Emilia-Romagna
 earthquakes. Eng Struct. 2016;118:262-73.
- 15 [12] Palanci M, Senel SM, Kalkan A. Assessment of one story existing precast industrial buildings
- 16 in Turkey based on fragility curves. Bulletin of Earthquake Engineering. 2017;15:271-89.
- 17 [13] Casotto C, Silva V, Crowley H, Nascimbene R, Pinho R. Seismic fragility of Italian RC precast
- 18 industrial structures. Engineering Structures. 2015;94:122-36.
- 19 [14] Kramar M, Isakovic T, Fischinger M. Seismic collapse risk of precast industrial buildings with 20 strong connections. Earthq Eng Struct D. 2010;39:847-68.
- 21 [15] Bellotti D, Casotto C, Crowley H, Deyanova MG, Germagnoli F, Fianchisti G et al. Capannoni
- monopiano prefabbricati: distribuzione probabilistica dei sistemi e sottosistemi strutturali dagli anni
 sessanta ad oggi. Progettazione sismica. 2014;3.
- 24 [16] Ferrini M, Lucarelli E, Baglione M, Borsier S, Bortone G, Ginori R et al. DOCUP Toscana 2000-
- 25 2006 Azione 2.8.3: "Riduzione del rischio sismico nelle aree produttive Esiti dell'indagine di
 26 primo livello". 12th Conference of Seismic Engineering in Italy2007.
- 27 [17] DPC/RELUIS, ASSOBETON. Progetto triennale 2005/08 Linea di ricerca 2: Valutazione e
- riduzione della vulnerabilità degli edifici esistenti in c.a Obiettivo 2.9: Comportamento e rinforzo di
 strutture industriali prefabbricate. 2008.
- [18] Sezen H, Elwood KJ, Whittaker AS, Mosalam KM, Wallace JW, Stanton JF. Structural
 Engineering Reconnaissance of the August 17, 1999, Kocaeli (Izmit), Turkey, Earthquake. Pacific
 Earthquake Engineering Research Center. 2000.
- Babic A, Dolsek M. Seismic fragility functions of industrial precast building classes.
- 34 Engineering Structures. 2016;118:357-70.
- 35 [20] Magliulo G, Ercolino M, Cimmino M, Capozzi V, Manfredi G. FEM analysis of the strength of
- 36 RC beam-to-column dowel connections under monotonic actions. Constr Build Mater. 2014;69:27137 84.
- [21] Zoubek B, Isakovic T, Fahjan Y, Fischinger M. Cyclic failure analysis of the beam-to-column
 dowel connections in precast industrial buildings. Engineering Structures. 2013;52:179-91.
- 40 [22] Belleri A, Torquati M, Riva P. Seismic performance of ductile connections between precast
 41 beams and roof elements. Mag Concrete Res. 2014;66:553-62.
- 42 [23] McKenna F, Fenves G. OpenSees Manual <u>http://opensees.berkeley.edu</u>. Pacific Earthquake
 43 Engineering Research Center. 2013.
- 44 [24] Ferrara L, Colombo A, Negrp P, Toniolo G. Precast vs. cast-in-situ reinforced concrete industrial
- buildings under earthquake loading: an assessment via pseudodynamic tests. 13th World Conference
 on Earthquake Engineering. Vancouver, B.C., Canada2004.
- 47 [25] MacRae GA. P- Δ Effects on Single- Degree- of- Freedom Structures in Earthquakes. Earthq
 48 Spectra. 1994;10:539-68.
- 49 [26] Fischinger M, Kramar M, Isaković T. Cyclic response of slender RC columns typical of precast
- 50 industrial buildings. Bulletin of Earthquake Engineering. 2008;6:519-34.

- 1 [27] Fardis MN, Biskinis D. Deformation capacity of RC members, as controlled by flexure or shear.
- University of Tokyo: International Symposium on Performance-based Engineering for Earthquake
 Resistant Structures; 2003.
- 4 [28] Haselton C. Assessing Seismic Collapse Safety of Modern Reinforced Concrete Moment-Frame
- 5 Buildings. Department of Civil Engineering California State University, Chico: PEER Report; 2006.
- 6 [29] Ibarra LF, Medina RA, Krawinkler H. Hysteretic models that incorporate strength and stiffness
- 7 deterioration. Earthq Eng Struct D. 2005;34:1489-511.
- 8 [30] Galasso C, Maddaloni G, Cosenza E. Uncertainly Analysis of Flexural Overstrength for Capacity
- 9 Design of RC Beams. Journal of Structural Engineering. 2014;140.
- 10 [31] Jalayer F, Cornell CA. A special application of non-linear dynamic analysis procedures in 11 probability-based seismic assessments in the region of global dynamic instability. Applications of
- 12 Statistics and Probability in Civil Engineering, Vols 1 and 2. 2003:1493-500.
- 13 [32] Iervolino I, Spillatura A, Bazzurro P. RINTC project: assessing the (implicit) seismic risk of
- 14 code-conforming structures in Italy. Compdyn 2017, 6th ECCOMASS Thematic Conference on
- Computational Methods in Structural Dynamics and Earthquake Engineering. Rodhes Island,Greece2017.
- 17 [33] Jayaram N, Lin T, Baker JW. A Computationally Efficient Ground-Motion Selection Algorithm
- 18 for Matching a Target Response Spectrum Mean and Variance. Earthq Spectra. 2011;27:797-815.
- 19 [34] Lin T, Haselton CB, Baker JW. Conditional spectrum-based ground motion selection. Part I:
- Hazard consistency for risk-based assessments. Earthq Eng Struct D. 2013;42:1847-65.
 [35] Lin T, Harmsen SC, Baker JW, Luco N. Conditional Spectrum Computation Incorporating
- 21 [55] Lin T, Harmsen SC, Baker JW, Luco N. Conditional Spectrum Computation Incorporating
 22 Multiple Causal Earthquakes and Ground-Motion Prediction Models. B Seismol Soc Am.
 23 2013;103:1103-16.
- 24 [36] Dolšek M, Fajfar P. Simplified non-linear seismic analysis of infilled reinforced concrete frames.
- 25 Earthquake Engineering & Structural Dynamics. 2005;34:49-66.
- 26 [37] Baker JW. Efficient Analytical Fragility Function Fitting Using Dynamic Structural Analysis.
- 27 Earthq Spectra. 2015;31:579-99.
- [38] Saatcioglu M, Mitchell D, Tinawi R, Gardner NJ, Gillies AG, Ghobarah A et al. The August 17,
- 29 1999, Kocaeli (Turkey) earthquake damage to structures. Can J Civil Eng. 2001;28:715-37.
- 30 [39] Toniolo G, Colombo A. Precast concrete structures: the lessons learned from the L'Aquila 31 earthquake. Struct Concrete. 2012;13:73-83.
- 32 33